Stellar flare oscillations: evidence for oscillatory reconnection and evolution of MHD modes


Published in:
Monthly Notices of the Royal Astronomical Society

Document Version:
Publisher's PDF, also known as Version of record

Queen's University Belfast - Research Portal:
Link to publication record in Queen's University Belfast Research Portal

Publisher rights
© 2018 The Author(s) This work is made available online in accordance with the publisher's policies. Please refer to any applicable terms of use of the publisher.

General rights
Copyright for the publications made accessible via the Queen's University Belfast Research Portal is retained by the author(s) and / or other copyright owners and it is a condition of accessing these publications that users recognise and abide by the legal requirements associated with these rights.

Take down policy
The Research Portal is Queen's institutional repository that provides access to Queen's research output. Every effort has been made to ensure that content in the Research Portal does not infringe any person's rights, or applicable UK laws. If you discover content in the Research Portal that you believe breaches copyright or violates any law, please contact openaccess@qub.ac.uk.
Stellar flare oscillations: evidence for oscillatory reconnection and evolution of MHD modes


1 Armagh Observatory and Planetarium, College Hill, Armagh BT61 9DG, UK
2 Department of Astronomy, Faculty of Physics, St Kliment Ohridski University of Sofia, 5 James Bourchier Boulevard, 1164 Sofia, Bulgaria
3 Centre for Fusion, Space and Astrophysics, Department of Physics, University of Warwick, Coventry CV4 7AL, UK
4 Department of Physics, Indian Institute of Technology (Banaras Hindu University), Varanasi 221005, Uttar Pradesh, India
5 INAF-OAR National Institute for Astrophysics, 00078, Monte Porzio Catone, I-00078 RM, Italy
6 Inter-University Centre for Astronomy and Astrophysics, Post Bag-4, Ganeshkhind, Pune 411007, Maharashtra, India
7 Astrophysics Research Centre, School of Mathematics and Physics, Queen’s University Belfast, BT7 1NN, UK

ABSTRACT

Here, we report on the detection of a range of quasi-periodic pulsations (20–120 s; QPPs) observed during flaring activity of several magnetically active dMe stars, namely AF Psc, CR Dra, GJ 3685A, GL 65, SDSS J084425.9+513830, and SDSS J144738.47+035312.1 in the GALEX NUV filter. Based on a solar analogy, this work suggests that many of these flares may be triggered by external drivers creating a periodic reconnection in the flare current sheet or an impulsive energy release giving rise to an avalanche of periodic bursts that occur at time intervals that correspond to the detected periods, thus generating QPPs in their rising and peak phases. Some of these flares also show fast QPPs in their decay phase, indicating the presence of fast sausage mode oscillations either driven externally by periodic reconnection or intrinsically in the post-flare loop system during the flare energy release.

Key words: MHD – waves – stars: activity – stars: flare – stars: late-type – ultraviolet: stars.

1 INTRODUCTION

Flare light curves often show an oscillatory pattern, referred to as quasi-periodic pulsations (QPPs). More specifically, some QPPs exhibit periodic and decaying variation of the flux in a particular waveband after the flare peak, while others are only present in the impulsive phase. For solar flares, these range from milliseconds to a few minutes, while stellar flares can have oscillations of up to several tens of minutes (Welsh et al. 2006; Simões, Hudson & Fletcher 2015; Cho et al. 2016). If QPPs are generated by quasi-periodic processes, then this provides information on the ongoing physical processes during the flare, e.g. evolution of Magnetohydrodynamic (MHD) mode(s) or periodic reconnection and thus associated energy release as well as modulation of emission (Mitra-Kraev et al. 2005; Nakariakov 2007; Van Doorsselaere, Kupriyanova & Yuan 2016). Some authors, e.g. Russell & Fletcher (2013), have even suggested that MHD waves may be responsible for energy transport from the reconnection region to the flare foot-points contradicting the conventional thick-target model. Three possible mechanisms exist: the oscillations are excited by the external flare trigger, within the flare itself, or in post-flare loops (Mathioudakis et al. 2003, 2006; Pandey & Srivastava 2009; McLaughlin et al. 2012; Srivastava, Lalitha & Pandey 2013; Pucci, Onofri & Malara 2014). The signature of QPPs is a very important tool, allowing us to gain an insight into the physical conditions within the stellar atmospheres. Recent observations have detected superflares in the lower atmosphere of magnetically active stars (Maehara et al. 2012; Anfinogentov et al. 2013). Balona et al. (2015) performed a study of QPPs in the white light emission from stellar flares based on Kepler data. Multi-periodic QPPs are also detected in many flares (Pugh, Nakariakov & Broomhall 2015). Although the modulation in the white light emissions gives information about the physical processes occurring in the stellar flares near the surface of the star, similar QPPs observed in X-ray or UV describe the localized physical conditions higher in the atmosphere, e.g. chromosphere or corona. Recently, Srivastava et al. (2013) observed the presence of multiple harmonics of slow magneto-acoustic oscillations in an X-ray flare on Proxima Centauri, and performed MHD seismology. They measured the density scale height of its corona to be smaller than the typical hydrostatic scale height, and indicated the presence of non-equilibrium conditions there.

Cho et al. (2016) looked at QPPs in solar flares with RHESSI and stellar flares using XMM data. Typical periods derived from stellar flares are 16.2 ± 15.9 min with a damping time of 27.1 ± 28.7 min, while for solar flares the QPPs period was 0.9 ± 0.6 min with a
damping time of 1.5 ± 1.1 min. The interesting finding of this work was that the ratio of the damping time (τ) to period (P) was 1.59 for stellar flares and 1.74 for solar events. In fact, a straight line fit of τ = 1.62P^{0.09} fitted QPPs ranging in period from ~20 s to 60 min, suggesting a similar mechanism. Here, we extend work first presented by Welsh et al. (2006) which used data from GALEX. The GALEX satellite (Martin et al. 2005) was launched in 2003 and operated for just over 10 yr. Although its primarily mission was to study galaxies, it proved to be an excellent observatory for the serendipitous detection of stellar flares. It operated in two ultraviolet wavebands: the far-UV (FUV: 1350–1750 Å) and/or near-UV (NUV: 1750–2800 Å) and was capable of providing sub-second time resolution data of flares. In addition to looking again at the oscillations reported by Welsh et al. (2006), we include additional objects, plus we searched for evidence of additional periods in the data as done by Van Doorsselaere et al. (2011). For this, we used two different techniques, wavelet transformation plus the empirical mode decomposition addressing different issues; how many of these UV flares on M dwarfs show oscillations, when during the flare do we see them, do we see more than one period during the flare and is there evidence for period evolution during the flare?

Welsh et al. (2006) looked at the line and continuum contribution in the NUV filter (for a non-flaring atmosphere). The dominant line emitters were Mg II, Fe II, Al III, C III, etc. For example, Mg II has ~10 per cent contribution, the region from 2320 to 2530 Å contributes ~17 per cent (mostly Fe II), while the line around 2290 ± 20 Å supplies ~14 per cent. The remaining NUV flux contribution arises from the various continuum processes. Thus, emission observed in this filter originates mostly in the upper chromosphere/lower transition region.

2 OBSERVATIONS

The flares were identified and light curves were produced using the gPhoton data base and modules (Million et al. 2016). gPhoton is a GALEX data calibration and extraction pipeline that allows easy access to time-tagged photon events. After identifying the available exposures for a number of M dwarfs, we generated count maps for each star and epoch. We used these to find flare events and determine the coordinates, aperture and background annulus size, and position, the latter to make sure that a contaminating source was not present. These parameters were used to obtain the calibrated time-tagged data with a time resolution of 1 s. In the following sections, we present the results and analysis of the brightest flares found. Light curves were obtained for flares from AF Psc, CR Dra, GJ 1167A, GJ 3685A, GI 65, SDSS J084425+513830, and SDSS J144738.47+035312.1 in the NUV filter and are shown in Fig. 1. Since gPhoton is still experimental, we compared these flare light curves with those published in Welsh et al. (2006), using the same aperture (10 arcsec aperture) and background annulus (extending from ~15 to 20 arcsec from the central position of the star). Excellent agreement was obtained for AF Psc, CR Dra (epoch 5), and SDSS J084425+513830, while GJ 3685A differed by ~20 per cent.

3 ANALYSIS AND OBSERVATIONAL RESULTS

We extracted the periods using two different methods, a boxcar de-trending followed by wavelet and the empirical mode decomposition.

3.1 Wavelet

Before using the wavelet, the light curves were de-trended using a running mean. We tested values ranging from 40 s to 60 s, but no difference was apparent in the resulting de-trended light curve. The signal is a time series of length t consisting of data points spanning over an interval δt and the total length as Nδt. The output of the wavelet procedure is a relation between the Fourier Frequency τ^{-1} to the time-step (2δt)^{-1}. For such a time series, the Morlet wavelet consisting of a plane wave modulated by a Gaussian is given by Torrence & Compo (1998)

$$\Psi_\eta(t) = \pi^{-1/4}e^{i\omega_0 t}e^{-\eta^2/2},$$

where \(\omega_0\) is a non-dimensional frequency. A continuous wavelength transform for a discrete time series \(x_n\) is derived by convolution of \(x_n\) with \(\delta t\). Here, we use scaled and translated version of \(\Psi_\eta(t)\). The waveform is given by

$$W_n(s) = \sum_{n'=0}^{N-1} x_n \Psi^*[\frac{(n'-n)\delta t}{s}],$$

where \(s\) is the wavelet scale, \(n\) is localized time, and \(\Psi^*\) is a complex conjugate of \(\Psi\). Further, the convolution discussed in equation (2) is carried out for \(N\) number of points in the time series. We carry these \(N\) convolutions simultaneously in Fourier space using a discrete Fourier transform given by

$$\hat{x}_k = \frac{1}{N} \sum_{n=0}^{N-1} x_n e^{-2\pi i kn/N},$$

where \(k = 0\) to \(N - 1\) is the frequency index (in a continuous case, the Fourier transform of a function \(\Psi(t/s)\) is given by \(\hat{\Psi}(s(\omega))\)). Thus, the wavelet transform is

$$W_n(s) = \sum_{k=0}^{N-1} \hat{x}_k^* \hat{\Psi}^*(s(\omega_k))e^{i\omega_0 k \delta t}.$$  

The angular frequency is given by \(\omega_k\) and has limits \(\pm 2\pi k/N\delta t\). Thus, a continuous wavelet transform can be computed using equation (4) and a standard Fourier transform routine.

Wavelet plots for some of these flares were shown in Welsh et al. (2006); below, we summarize the results for each flare based on both analyses (see Fig. 2).

**CR Dra (epoch 5):** From the wavelet, a period of 30 s is apparent in the late-rise phase/flare peak, plus a longer period of ~120 s throughout the flare. There was no evidence of additional periods in the decay phase.

**CR Dra (epoch 12):** From the wavelet, this flare showed two periods, 43 s in the rise phase followed by a period of 20 s in the decay phase.

**CR Dra (epoch 25)** There are two periods in the impulsive/flare peak of 60 s and ~100 s.

**GJ 3685A:** This star produced two flares separated by a few minutes. From the wavelet, three periods were apparent in the data; a period of 110 s throughout both flares, a period of 60 s during the first flare, and a period of 36 s during the early part of the second flare.

**GJ 65:** Again, this flare showed two periods based on the wavelet, 46 s in the rise phase to late in the decay phase with a weak ~25 s period around flare maximum.

**SDSS J084425+513830:** From the wavelet, this flare showed two periods of 40 s and 120 s around flare peak.
Figure 1. The flare light curves for AF Psc, CR Dra, GJ 1167A, GJ 3685A, Gl 65, SDSS J0844+5138, and SDSS J144738.47+035312.1 as seen in the NUV/GALEX filter. The ‘0’ on the x-axis corresponds to start time given in Table 1. We show three flares from CR Dra which we label epoch 5, 12, and 25. For each flare, we overplot the overall trend in the flare light curve as estimated using a running mean and the empirical mode composition.

**SDSSJ144738.47+035312.1**: This flare had a 48 s period throughout its short decay phase based on the wavelet.

### 3.2 Empirical mode decomposition (EMD)

Born as a preconditioning technique for the Hilbert transform, the EMD method moves from the assumption that a time series, representing a physical process, is the superposition of many active time-scales, and decomposes the signal into a series of intrinsic mode functions (IMFs). Unlike other techniques (e.g. based upon fast Fourier transform), this decomposition basis is not set a priori but locally defined starting from the signal itself. This fact makes the technique suited to the study of non-stationary and non-linear processes. Each IMF is obtained by estimating the upper and lower envelopes of a signal $I(t)$, calculating their average $e(t)$, and defining a new time series as the difference $I(t) - e(t)$. The first IMF contains...
Figure 2. Wavelet intensity spectrum of the flares for AF Psc, CR Dra, GJ 3685A, GI 65, SDSS J084425.9+513830, and SDSS J144738.47+035312.1 based on the boxcar de-trended data, showing dominant periodicities with the global wavelet.

the high-frequency content of the original signal, while the last few IMFs contain the low-frequency part. This feature can be used to filter out the low-frequency part of a signal. Indeed, by summing up several of the higher order IMFs, one obtains a de-trended version of the original signal. The number of IMFs considered depends on the specific needs. Here, we have used a different number of IMFs for each flare. This number is found by a visual inspection of the filtered time series.

For the EMD, we considered all the signals as a combination of a smooth trend (flare itself), statistically significant oscillation plus randomly distributed background. The latter is represented by coloured noises characterized by the power-law index alpha in the dependence of their Fourier spectral power $S$ upon the frequency $f$, $S \sim 1/f^\alpha$. In the context of the EMD approach, it is re-written as $E \times P(1-\alpha) =$ constant, where $E$ is the EMD modal energy, and $P$ is the main modal period. For instance, $\alpha = 0$ corresponds to the case of white noise (with constant Fourier power $S$ and $E \times P =$ constant), $\alpha = 1$ is the pink (flicker) noise. Kolotkov, Anfinogentov & Nakariakov (2016) developed the EMD technique in the presence of coloured noise, allowing for clear distinguishing between quasi-periodic oscillatory phenomena in the solar atmosphere and superimposed random background processes; these results are given below with the derived periods given in the final plot for each flare.

It is a standard practice to distinguish several phases of a typical solar flare according to the timing of the emission recorded in different bands, e.g. see Benz (2008). Consequently and based upon the
analogy between solar and stellar flares, one may naturally expect
different physical mechanisms to dominate during different phases
of a stellar flare too, e.g. coronal loop oscillations before and after
the flare and (repetitive) reconnection during it. These processes are
entirely different and hence may have substantially different peri-
odicities, which can mix up and produce meaningless results in a
spectral analysis if an entire flare is considered. The latter justifies
the split of a flare light curve into a number of phases. In our anal-
ysis, we split the light curves into pre-flare, impulsive, and decay
phases. The start and end time of each phase have been chosen
manually and empirically according to the general behaviour of the
light curve (i.e. of their gradients/local slopes). More specifically,
the pre-flare phase is the light curve prior to a flux increase due
to the flare, the impulsive phase is from flare onset to an apparent
break in the gradient of a light curve after flare maximum (accord-
ing to the empirical template proposed by Davenport et al. 2014),
and flare decay is the rest of a light curve until the end of the flux
increase as shown in Fig. 1. On the other hand, simultaneous multi-
frequency stellar flare observations are generally unavailable, so we
have nothing to compare with for a more rigorous comparison. Such
a split leads to a reduction of the length of the analysed time series,
however, it does not corrupt the results of an EMD analysis and
does not contradict common sense, as the method operates locally
and self-adaptively and thus does not care about the length of the
analysed signal.

We found the signal to consist of the superposition of the white
(Fourier spectral energy is constant) and pinkish (Fourier spectral
energy is proportional to \(1/f\)) noises (see Figs 3–9), as well as oscil-
latory modes with statistically significant properties. The significant
level was set to 99 per cent.

**AF Psc:** The light curve consists of the overall flare trend, a
combination of the white (at shorter periods) and pink (at longer
periods) noisy components (with breaking point in the vicinity
of 15 s), and three statistically significant oscillations in the pre-flare,
impulsive, and decay phases, respectively. In the impulsive phase,
the mode has a stable period of 25 s with a growing amplitude. In
the pre-flare phase, we found a period of \(\sim 80\) s, while in the decay
phase the period was 120 s, decreasing with amplitude (see Fig. 3).
This could be the reason why we did not detect the latter using the
wavelet. The confidence intervals (given in the right-hand panel)
of the combined effect of the white and pink noise are given by
the blue lines. We also show in this figure the detected oscillations
overplotted on the observational data.

**CR Dra (epoch 5):** It is well described by the model of white
noise \(\alpha \approx 0\), see the corresponding confidence intervals in the
spectrum plot, shown in blue in Fig. 4), smooth trends (two points
in the top right corner of the spectrum plot), and two statistically
significant oscillations in the impulsive (50 s) and decaying (40 s)
phases (the other two points are above the noise confidence interval
in the spectrum plot).

**CR Dra (epoch 12):** Same as for the previous case: white noise,
trends, and two periodicities in the impulsive (70 s) and decaying
(80 s) phases with statistically significant properties (see Fig. 5).
However, the signal-to-noise ratio in the impulsive phase of this
flare seems to be lower than that of CR Dra epoch 5. There are two
additional periods in the impulsive phase of 20 s and 40 s which are
just on the significance level.

**CR Dra (epoch 25):** Both peaks are well described by the white
noise and smooth trends, with NO significant oscillations, although
there is a 30 s oscillation just below the 99 per cent significant level.
for the second flare. This lack of a period is in disagreement with the wavelet.

**GJ 3685A**: Both flare peaks have smooth trends and a reddish ($\alpha \approx 1.5$) noisy component which dominates at longer periods, with a 30 s oscillation in the second flare, see Fig. 6. We do not detect the longer periods as seen in the wavelet.

**Gl 65**: Here, we have pink ($\alpha \approx 1$) noise plus a smooth trend, and one statistically significant oscillation of $\sim 40$ s, see Fig. 7.

**SDSS J084425.9+513830**: In addition to the white noise, plus the smooth trend, we have two significant oscillations in the impulsive (35 s) and decay (120 s) phases (see Fig. 8).

**SDSS J144738.47+035312.1**: Again, we have white noise plus a smooth trend, and two significant oscillations in the impulsive (20 s) and decay (38 s) phases (see Fig. 9). However, the significance of the oscillation in the impulsive phase is very low (i.e. low signal-to-noise ratio), it is nearly at the 99 per cent noise level.

### 4 THEORETICAL INTERPRETATION

We have chosen various flaring epochs on different magnetically active stars and clearly determine the presence of QPPs (cf., Table 1). Most of the flares show periods in the decay phase ranging from $\approx 20$ s to over 100 s. For the 30–40 s periods in the decay phase, Welsh et al. (2006) interpreted these as the sausage wave from loops of length $\sim 10^8$ cm. If we were to interpret the periods in excess of 100 s as due to sausage waves, this would imply loop
lengths a factor of 3 longer. This natural interpretation comes from the excitation of the fundamental sausage mode, possessing a definite cut-off period, in a structured cylindrical magnetic tube having appropriate density contrast with an ambient background and kept almost in a field-free region (Roberts, Edwin & Benz 1984; Edwin & Roberts 1988; Aschwanden 2004). Recently, it was pointed out analytically by Lopin & Nagorny (2015) that there exists no cut-off wavenumber for sausage modes of any transverse order if the plasma density outside the loop decreases only mildly with distance. This could be an obvious scenario in stellar flaring regions as diffused multiple post-loop-flare loop arcades may be involved. Therefore, traverse plasma structuring across these diffused post-flare loop systems, where oscillations are excited, may not be established. Such a cut-off-free environment may lead to excitation of any period related to the fundamental sausage waves. Therefore, the observed range of periods, as detected in terms of flux modulations in the post-flare phase, may be associated with the sausage mode waves.

AF Psc shows an event where the pre-flare had a decreasing period with amplitude. This could suggest that this period is globally present before the flare was triggered. The external periodic wave driver of the longer period propagates towards the flare current sheet, leading to the high-frequency QPPs which could be due to the dispersive evolution or resonant filtering (Santamaria, Khomenko & Collados 2015).

Based on the solar analogy, we describe possible mechanisms behind the generation of such QPPs. We consider only those...
powers and associated periodicities as appeared in EMD and wavelet plots as global oscillations when they repeat >3 cycles. Otherwise, we consider the evolution of the power associated with localized oscillations due to any transient activity in the flare, e.g. elementary reconnection.

Solar flares show QPPs at all energies, e.g. Nakariakov et al. (2010) reported on oscillations up to energies of 2–6 MeV. These authors suggested that the time variability was due to the charge particle acceleration process, i.e. periodic magnetic reconnection. There are two possibilities here; spontaneous reconnection due to internal plasma properties and periodically triggered reconnection by perhaps MHD waves (Nakariakov & Melnikov 2009).

In some instances, the power in these flares is highly localized indicating it is not a global distribution (<3 cycle) producing the evolution of the MHD waves. Based on the analogy suggested above, it is possible that these QPPs are triggered by a periodicity in the inflow in the flare current sheet driving the periodic reconnection leading to a periodic production of non-thermal particles during the flare rise. This further generates the quasi-periodic modulation in the observed emissions (Nakariakov et al. 2006). The external wave...
In this paper, we observe a range of fast QPPs (20–120 s) in stellar flares of various magnetically active stars (e.g. AF Psc, CR Dra, GJ 3685A, GI 65, SDSS J084425.9+513830, and SDSS J144738.47+035312.1) in the NUV filter as observed by GALEX. These QPPs provide evidence of various physical processes occurring in the observed stellar flares. Many of these flares are most likely triggered by external drivers creating a periodic reconnection in the flare current sheet and generating QPPs especially in their rising and peak phases. Some of these flares also show fast QPPs in their decay phase, indicating the presence of magnetoacoustic mode oscillations either driven externally by periodic reconnection, or intrinsically in the post-flare loop system during the flare energy release. It is possible that the oscillatory reconnection interpretation does not have to apply only to the impulsive phase as some heating is probably ongoing during the decay phase as well.

Our analyses of multiple samples of stellar flares provide signatures about externally driven periodic reconnection, associated evolution of fast MHD pulsation, and intrinsically evolved fast MHD modes in the stellar post-flare loop system. Such physical processes are well known in the case of solar flares though, however, not very well established in stellar flares (Nakariakov & Melnikov 2009; Van Doorsselaere et al. 2016). We analysed the evolution of oscillatory powers associated with various QPPs in the observational time-domain of stellar flares, their nature, and their possible linkage with each other, if any. Additional investigations must be specifically planned to understand the various flaring epochs of an individual magnetically active star to further understand the dynamical plasma and wave processes there.

An important finding in this work is the difference between a wavelet and the EMD analysis. In many instances, similar results were obtained. Interestingly, GI 65 and GJ 3685A (and AF Psc) have the largest amplitude flares and unlike flares on the other stars they have coloured (pink and reddish) noisy components while the wavelet only has white noise included. Another interesting point is that almost all flares have two different gradients in the decay phase, which is consistent with the empirical template of a stellar flare, proposed by Davenport et al. (2014). We should also note the appearance of low-frequency peaks, followed by higher frequency modes. In addition, some of the peaks have a frequency ratio consistent with subharmonics. This is particularly evident, for instance, in the wavelet map of GI 65.

ACKNOWLEDGEMENTS

Armagh Observatory and Planetarium is a grant aided by the N. Ireland Department for Communities. JUS received short-term funding from Queens University Belfast. AKS acknowledges the RESPOND-ISRO (DOS/PAOGIA205-16/130/602) project, the SERB-DST project (YSS/2015/000621) grant, and Advanced Solar Computational & Analyses Laboratory (ASCAL). MS

Table 1. A list of the flares observed by GALEX, their start time, the flare duration in seconds, the derived period based on the wavelet, and Empirical Mode Decomposition in seconds (see the text for the timing of these different periods).

<table>
<thead>
<tr>
<th>Name</th>
<th>Sp. T.</th>
<th>Filter</th>
<th>Flare date</th>
<th>Start time</th>
<th>Duration (s)</th>
<th>Wavelet periods (s)</th>
<th>EMD periods (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>AF Psc</td>
<td>dM4.5</td>
<td>NUV</td>
<td>2004-10-12</td>
<td>19:27:33</td>
<td>1200</td>
<td>30 &amp; 120</td>
<td>25 &amp; 120 &amp; 80</td>
</tr>
<tr>
<td>CR Dra (epoch 5)</td>
<td>dM5.5</td>
<td>NUV</td>
<td>2005-05-05</td>
<td>00:59:57</td>
<td>512</td>
<td>43</td>
<td>40 &amp; 50</td>
</tr>
<tr>
<td>CR Dra (epoch 25)</td>
<td>dM5.5</td>
<td>NUV</td>
<td>2009-05-25</td>
<td>06:30:27</td>
<td>512</td>
<td>60 &amp; 100</td>
<td>30</td>
</tr>
<tr>
<td>GJ 3685A</td>
<td>dM4</td>
<td>NUV</td>
<td>2004-04-20</td>
<td>22:50:46</td>
<td>300</td>
<td>36 &amp; 60 &amp; 110</td>
<td>30</td>
</tr>
<tr>
<td>SDSS J084425.9+513830</td>
<td>dM</td>
<td>NUV</td>
<td>2005-01-09</td>
<td>22:43:22</td>
<td>200</td>
<td>40 &amp; 120</td>
<td>35 &amp; 120</td>
</tr>
</tbody>
</table>
acknowledges support from ‘Progetti di ricerca INAF di Rilevante Interesse Nazionali’ (PRIN-INAF) 2014. We also acknowledge support from the International Space Science Institute for the team ‘QPPs in Stellar Flares: a tool for studying the Solar–Stellar Connection’. AA acknowledges support from the Science Fund of Sofia University (grant no. 80-10-229/2017). DYK acknowledges the support of the STFC consolidated grant ST/L000733/1.

REFERENCES


This paper has been typeset from a \LaTeX file prepared by the author.