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Ion acceleration by superintense laser-plasma interaction

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Ion acceleration driven by superintense laser pulses is attracting an impressive and steadily increasing effort. Motivations can be found in the applicative potential and in the perspective to investigate novel regimes as available laser intensities will be increasing. Experiments have demonstrated, over a wide range of laser and target parameters, the generation of multi-MeV proton and ion beams with unique properties such as ultrashort duration, high brilliance, and low emittance. An overview is given of the state of the art of ion acceleration by laser pulses as well as an outlook on its future development and perspectives. The main features observed in the experiments, the observed scaling with laser and plasma parameters, and the main models used both to interpret experimental data and to suggest new research directions are described.

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I. INTRODUCTION

More than half a century ago, Veksler (1957) introduced the concept of “coherent acceleration” of particles as a mechanism in which the accelerating field on each particle is proportional to the number of particles being accelerated,
in contrast to traditional techniques. Additional elements in Veksler’s vision of future accelerators included the automatic synchrony between the particles and the accelerating field, the localization of the latter inside the region where the particles are, and the production of quasineutral groups with large numbers of energetic particles.

These features are realized in the acceleration of ions from plasmas produced by intense laser pulses. In this case, as a very general description, strong electric fields are generated by a collective displacement of a large number of electrons, and such electric fields accelerate ions until charge neutrality is restored and ions move together with electrons in a ballistic way.

Before the year 2000, ions having energies up to several MeVs had been observed in several high-intensity laser-matter interaction experiments and for different targets, including thick solid foils (Gitomer et al., 1986; Fews et al., 1994; Beg et al., 1997, and references therein), gas jets (Krushelnick et al., 1999; Sarkisov et al., 1999, and references therein) and submicrometric clusters (Ditmire et al., 1997, 1999, and references therein). Common to these experiments was the rather isotropic ion emission and the resulting low brilliance, making these configurations unattractive as ion accelerators for applications.

In 2000 three experiments (Clark et al., 2000a; Maksimchuk et al., 2000; Snavely et al., 2000) independently reported the observation of an intense emission of multi-MeV protons from solid targets, either metallic or plastic (CH), of several microns thickness irradiated by high-intensity laser pulses. The basic setup of these experiments is shown in Fig. 1. The laser intensity, number of protons, and maximum ion energy observed for the three experiments were \(3 \times 10^{18} \text{ W cm}^{-2}\), \(\geq 10^9\) and 1.5 MeV (Maksimchuk et al., 2000), 5 \(\times 10^{19} \text{ W cm}^{-2}\), \(\sim 10^{12}\) and 18 MeV (Clark et al., 2000a), and 3 \(\times 10^{20} \text{ W cm}^{-2}\), \(\sim 2 \times 10^{13}\), and 58 MeV (Snavely et al., 2000), respectively. Figure 2 shows the spectrum of protons observed by Snavely et al. (2000). The protons were detected at the rear side of the target, opposite to the laser-irradiated surface and were emitted, as a rather collimated beam, along the target normal direction.

The emission of protons from metallic targets whose chemical composition does not include hydrogen may sound surprising, but it was already clear from previous experiments that protons originated from impurities, i.e., thin layers of water or hydrocarbons which are ordinarily present on solid surfaces under standard experimental conditions. In experiments performed with both “long” nanosecond pulses (Gitomer et al., 1986, and references therein) and “short” (sub)picosecond, high-intensity pulses (Fews et al., 1994; Beg et al., 1997; Clark et al., 2000b), protons and heavier ions were commonly detected in the backward direction (i.e., toward the laser) with a broad angular distribution, and their origin was interpreted in terms of acceleration during the expansion of the hot laser-produced plasma at the front (laser-irradiated) side of the target. The characteristics of the forward proton emission in the new experiments, such as the high degree of collimation and laminarity of the beam, were much more impressive.

These findings generated an enormous interest both in fundamental research and in the possible applications. In an applicative perspective, the most relevant and peculiar feature of multi-MeV ions is the profile of energy deposition in dense matter. Different from electrons and x rays, protons and light ions deliver most of their energy at the end of their path (see Fig. 3), at the so-called Bragg peak (Ziegler, Biersack, and Ziegler, 2008; Knoll, 2010). The physical reason is that the energy loss is dominated by Coulomb collisions for which the cross section strongly grows with decreasing energy, so that the stopping process becomes progressively more and more efficient. This property makes protons and ions very suitable for highly localized energy deposition. The applications that were proposed immediately after the discovery of multi-MeV proton acceleration included ion beam cancer therapy, laser triggering and control of nuclear reactions, production of warm dense matter, “fast ignition” of inertial confinement fusion targets, and injectors for ion accelerators. These foreseen applications are reviewed in Sec. V. As a particularly innovative and successful application, ultrafast probing of plasmas by laser-driven proton beams is described in Sec. V.A.

While the potential for applications was apparent, the details of the physics behind proton acceleration were not clear. A debate arose on the actual location of the region where the

FIG. 1 (color online). Artist’s view of a typical experiment on proton emission from laser-irradiated solid targets.
protons were accelerated and, consistently, on the mechanism driving the acceleration. Clark et al. (2000a) and Maksimchuk et al. (2000) suggested that protons were accelerated at the front side of the target, crossing the latter and being detected on the opposite side. In contrast, Snavely et al. (2001) proposed that protons were accelerated at the front surface, crossing the target bulk, and reaching the rear surface of the target by highly energetic electrons accelerated at the rear side [see also Hatchett et al. (2000)]. To support the interpretation of these latter experiments (performed at the petawatt facility of Lawrence Livermore National Laboratory, USA) the so-called target normal sheath acceleration (TNSA) model was introduced by Wilks et al. (2001). Briefly, TNSA is driven by the space-charge field generated at the rear surface of the target by highly energetic electrons accelerated at the front surface, crossing the target bulk, and attempting to escape in vacuum from the rear side. The basic theory of TNSA and related models is described in detail in Sec. III. Most of the experiments investigating proton acceleration by laser interaction with solid targets have been interpreted in terms of the TNSA framework (see Secs. III.A and III.B) but the energy spectrum is ordinarily broad and thus not optimal for most applications.

A major requirement for several of the foreseen applications is an increase of the energy per nucleon up to hundreds of MeV and beyond. The next generation of laser facilities should allow intensities higher than the current record of $\sim 10^{22}$ W cm$^{-2}$ (Yanovsky et al., 2008), but at present it is not guaranteed that the ion energy scaling observed so far will be maintained at such extreme intensities nor that TNSA will still be effective. An analysis of proton acceleration experiments performed up to 2006 suggests a $\sim (I\lambda^2)^{1/2}$ scaling of proton energy up to values of $I\lambda^2 = 3 \times 10^{20}$ W cm$^{-2}$ $\mu$m$^{-2}$ (Borghesi et al., 2006; Fuchs et al., 2006b), where $I$ and $\lambda$ are the laser intensity and wavelength, respectively. Figure 4 summarizes such data, together with more recent results obtained with Ti:Sa-based, ultrashort (tens of fs) pulses, exhibiting a $\sim I\lambda^2$ scaling. Measurements by Robson et al. (2007) at energies up to 400 J, pulse durations between 1 and 8 ps, and intensities up to $6 \times 10^{20}$ W cm$^{-2}$ suggested a slower scaling. It is also of crucial importance to establish the most relevant scaling parameters as well as to improve or optimize beam emittance, brilliance, and monoenergeticity for specific applications. For instance, TNSA-generated proton beams are highly laminar and have very low emittance (see Sec. III.B) but the energy spectrum is ordinarily broad and thus not optimal for most applications.

These issues motivate the search for other ion acceleration mechanisms. These include concepts which have been explored previously in different contexts (e.g., astrophysics), such as radiation pressure acceleration (RPA) and collisionless shock acceleration (CSA). Other proposed schemes exploit the potential of both advanced target engineering and nonlinear “relativistic” optical effects in plasmas, such as ion acceleration in ultrathin solid targets which become transparent to intense laser pulses [break-out afterburner (BOA)], or involving low-density targets. The basic physics of these mechanisms and the related experimental work, still in a preliminary stage with respect to TNSA, will be described in Sec. IV. The development of advanced acceleration schemes is sustained by the continuous trend toward laser pulses of higher intensity and energy. A detailed account of the many active projects and facilities under development based on optical and infrared lasers ($\lambda \sim 1$ $\mu$m) is given in Sec. II of Di Piazza et al. (2012). Progress toward CO$_2$ lasers ($\lambda \sim 10$ $\mu$m) having multiteraWatt power (Haberberger, Tochitsky, and Joshi, 2010) is also of growing interest for ion acceleration, as discussed in Secs. IV.A.1 and IV.B.

On the theoretical side, the interpretation of experiments has revitalized classic and often controversial problems of plasma physics such as plasma expansion into vacuum and...
the formation of collisionless sheaths, at the basis of most of the TNSA models, as well as other general physics models such as the motion of relativistic moving mirrors, a concept already discussed in the original work on special relativity by Einstein (1905), which serves as a model for RPA. Simple, analytically affordable models are extremely useful to understand the basic acceleration mechanisms and, in particular, to provide scaling laws which may give directions for further developments. Reference models also highlight the several connections with other fields, such as the physics of discharges, of ultracold plasmas, and of particle acceleration in astrophysics. The theoretical discussions in Secs. III and IV are, to a significant extent, based on this approach.

Beyond simple modeling a rich and complex dynamics of laser-plasma interaction and ion acceleration, involving collective and self-organization effects, is apparent. Unfolding such dynamics requires the use of self-consistent electromagnetic (EM), kinetic simulations. To this aim, the particle-in-cell (PIC) method (see Sec. II.D) is by far the most commonly used approach. Large-scale, multidimensional PIC simulations running on parallel supercomputers are an effective support for the design and interpretation of laser-plasma acceleration experiments, although fully “realistic” simulations in three spatial dimensions and for actual laser and target parameters are most of the time still beyond computational capabilities. These limitations further motivate the development of complementary, reduced simulation models. These issues are further discussed in Secs. II.D and III.C.4.

A comprehensive description of laser-plasma dynamics is far beyond the scope of this work and can be found in recent books and reviews (Gibbon, 2005b; Mourou, Tajima, and Bulanov, 2006; Mulser and Bauer, 2010). In Secs. II.A and II.B we describe only a few basic issues of relevance to the understanding of ion acceleration mechanisms. The main mechanisms are first introduced in a compact form in Sec. II.C, leaving a detailed discussion to the following Secs. III and IV.

II. LASER ION ACCELERATION IN A NUTSHELL

A. Laser interaction with overdense matter

In this work we mostly refer to ion acceleration occurring in the interaction with solid targets, where the electron density $n_e$ greatly exceeds the so-called critical or cutoff density,

$$n_{e,c} = \frac{m_e \omega_p^2}{4 \pi e^2} = 1.1 \times 10^{21} \text{ cm}^{-3} \left( \frac{\lambda}{1 \mu\text{m}} \right)^{-2}. \quad (1)$$

The condition $n_e = n_{e,c}$ is equivalent to $\omega_p = \omega$, where $\omega_p = (4 \pi n_e e^2/m_e)^{1/2}$ and $\omega = 2 \pi c / \lambda$ are the plasma and laser frequencies, respectively. Since the linear refractive index of the plasma is $n = (1 - \omega_p^2/\omega^2)^{1/2} = (1 - n_{e,c}/n_e)^{1/2}$, in the $n_e > n_{e,c}$ “overdense” region $n$ has imaginary values and the laser pulse cannot propagate. All the laser-plasma interaction occurs either in the “underdense” region where $n_e < n_{e,c}$ or near the “critical” surface at which $n_e \approx n_{e,c}$.

Relativistic effects make the refractive index nonlinear. Qualitatively speaking, the relativistic refractive index describing the propagation of a plane wave with vector potential $\mathbf{A} = \mathbf{A}(x,t)$ is obtained from the linear expression by replacing the electron mass with the quantity $m_e \gamma$, where the relativistic factor $\gamma$ is given by

$$\gamma = \sqrt{1 + (\alpha^2)} = \sqrt{1 + a_0^2/2}, \quad (2)$$

where $\alpha = e\mathbf{A}/m_e c^2$, and the angular brackets denote an average over the oscillation period. The parameter $a_0$ is the commonly used “dimensionless” amplitude related to the laser intensity $I$ by

$$a_0 = 0.85 \left( \frac{I A_{\mu m}^2}{10^{19} \text{ W cm}^{-2}} \right)^{1/2}. \quad (3)$$

where we used $I = c(\mathbf{E}^2)/4\pi$ to relate the electric field $\mathbf{E} = -(1/c)\partial\mathbf{A}/\partial t$ to the laser intensity $I$.

The nonlinear, relativistic index $n_{e,nl} = (1 - n_e/\gamma n_{e,c})^{1/2}$ becomes imaginary when $n_e > n_{e,c}$, showing an increase of the cutoff density for a plane monochromatic wave: this effect is known as relativistic self-induced transparency or, briefly, relativistic transparency. However, the problem of laser penetration inside a plasma is not trivial (Cattani et al., 2000; Golovizin and Schep, 2000; Shen and Xu, 2001) because of both the nonlinearity in the wave equation and the self-consistent modification of the plasma density profile due to radiation pressure effects. These latter may be described via the ponderomotive force (PF).\(^2\) In an oscillating, quasimonochromatic electromagnetic field described by a dimensionless vector potential $\mathbf{a}(\mathbf{r},t)$ whose envelope is sufficiently smooth in space and time, the relativistic PF is [see, e.g., Bauer, Mulser, and Steeb (1995) and Mulser and Bauer (2010)]

$$\mathbf{f_p} = -m_e c^2 \nabla(1 + \langle \alpha^2 \rangle)^{1/2}. \quad (4)$$

For a plane wave impinging on an overdense plasma, the resulting PF, more effective on the lightest particles, is in the inward direction and tends to push and pull electrons inside the plasma. Ponderomotive effects will be further discussed below (see Secs. II.B and II.C).

In a multidimensional geometry, a laser pulse of finite width may produce a density depression around the propagation axis also because of the ponderomotive force pushing the electrons in the radial direction. Jointly with the relativistic effect and target expansion driven by electron heating, this mechanism may lead to a transition to transparency as soon as the electron density drops below the cutoff value (Fuchs et al., 1999). Investigations of ion acceleration in the transparency regime are described in Sec. IV.C.

\(^1\)Consistently with our definitions, given the value for $I$, the peak value of the dimensionless vector potential of the plane wave will be given by $a_0$ for linear polarization and by $a_{00}/\sqrt{2}$ for circular polarization.

\(^2\)Throughout this review we refer to the ponderomotive force as the slowly varying, effective force describing the cycle-averaged motion of the “oscillation center” of a charged particle in an oscillating nonuniform field, over a time scale longer than the oscillation period. “Fast” oscillating components are not included in the definition of ponderomotive force here adopted.
The penetration of the laser pulse depends not only on the electron density but also on the target size when the latter becomes close to or smaller than one wavelength. As a simple but useful example, the nonlinear transmission and reflection coefficients can be calculated analytically for a sub-wavelength foil modeled as a Dirac delta-like density profile (Vshivkov et al., 1998; Macchi, Veghini, and Pegoraro, 2009), obtaining a transparency threshold

\[ a_0 > \frac{\pi n_e \ell}{n_c \lambda} = \xi, \]  

where \( \ell \) is the thickness of the foil. Equation (5) has some interest for the interaction with ultrathin foil targets (see Secs. IV.A.2–IV.C).

**B. Hot electrons**

Since the laser pulse cannot penetrate into solid-density regions, the absorbed energy is transported to these regions mostly by energetic (commonly named either hot or fast) electrons which may be generated during the interaction through several mechanisms. By hot electrons in the present context one typically refers to relativistic electrons whose energy is of the order of the cycle-averaged oscillation energy in the electric field of the laser in vacuum,

\[ E_p = m_e c^2 (\gamma - 1) = m_e c^2 \left(1 + \frac{a_0^2}{2} - 1\right), \]  

where Eq. (2) has been used. Equation (6) is also called the “ponderomotive” energy (Wilks et al., 1992). Hot electrons penetrating into solid targets have been observed and characterized in several experiments at very high intensities and for different interaction conditions and play a fundamental role in applications such as laser-driven photonuclear physics and fast ignition of fusion targets. Moreover, as discussed in Sec. III, in most of the experiments reported so far, acceleration of protons and heavier ions is driven by hot electrons.

The process of hot electron generation turns out to be complex and, possibly, not yet completely understood. A review of past and ongoing research on the topic can be found in recent books (Gibbon, 2005b; Mulser and Bauer, 2010). Here we give a basic discussion at a qualitative level, focusing on those aspects which are most essential and relevant to ion acceleration.

At the surface of an overdense plasma, electrons are driven by the Lorentz force \( \mathbf{f}_e = -e(\mathbf{E} + \mathbf{v} \times \mathbf{B}/c) \) which includes both the fields of the incident and reflected laser pulses and self-generated fields. As a necessary condition for the efficient generation of hot electrons near the critical surface \( \mathbf{f}_L \) must have an oscillating component directed along the density gradient \( \nabla n_e \). This is the case for the well-known resonance absorption where the condition \( \mathbf{E} \cdot \nabla n_e \neq 0 \) is necessary to drive resonant plasma oscillations which in turn accelerate electrons. In a plane geometry such condition requires oblique incidence and \( P \) polarization of the laser pulse. This absorption mechanism is sensitive to the density scale length \( L_n = n_e/|\nabla n_e| \) because the driving force is evanescent in the resonance region.

In a sharp-boundary plasma where \( L_n \ll \lambda \), absorption and heating may arise because electron motion is not adiabatic, as electrons are driven from the region of strong fields to the evanescent region in a time shorter than \( 2\pi/\omega_e \) so that the cycle average \(-e(\mathbf{E} \cdot \mathbf{v})\) may not cancel out. Thus, short duration and high-intensity laser pulses favor electron heating because the hydrodynamic expansion does not have sufficient time to wash out sharp density gradients nor is it dominated by the strong ponderomotive force that steepens the density profile.

At this point it is worth mentioning that in most high-intensity experiments the main interaction pulse is preceded by prepulses which cause early plasma formation and expansion, so that the short-pulse interaction does not occur with a sharp-boundary, solid-density plasma. However, profile steepening at the critical surface is still effective; thus one may expect the interactions to still occur with a sharp density profile, having a lower density jump with respect to a solid interface. Occasionally, “preplasma” formation may also allow additional electron acceleration mechanisms to take place in the underdense plasma region (Esarey, Schroeder, and Leemans, 2009), possibly leading to electron energies much higher than given by Eq. (6). In more recent experiments, advanced pulse cleaning techniques allow minimizing prepulse effects (see Sec. III.E).

### 1. Heating models

A popular electrostatic model of electron heating at a step-boundary plasma was proposed by Brunel (1987). In this model, electrons are dragged out of the surface of a perfect conductor by an oscillating “capacitor field,” extending on the vacuum side, and representing the \( P \) component of the incident plus reflected laser electric field. Electrons are considered to be “absorbed” when, after having performed about half of an oscillation on the vacuum side, they reenter the target, there delivering their energy, which is of the order of the oscillation energy in the external field. The model thus accounts in a simplified way for the pulsed generation (once per cycle) of hot electrons directed into the target and having an energy, roughly speaking, close to the “vacuum” value (6). This simple model is not self-consistent because, for instance, the capacitor field is assumed to vanish inside the target, implying the presence of a surface charge density. Nevertheless, following Mulser, Ruhl, and Steinmetz (2001) it is possible to provide a “minimal” 1D model, still in the capacitor approximation, where the electrostatic field is calculated self-consistently and an acceleration of electron bunches similar to that inferred by Brunel is apparent.

We consider the electric field as the sum of the electrostatic and driver fields, e.g., \( \mathbf{E}_e = \mathbf{E}_e + \mathbf{E}_d \), where \( \mathbf{E}_d = \mathbf{E}_d(t) \sin \omega_0 t \) with \( \mathbf{E}_d(t) \) a suitable temporal envelope, a step-boundary density profile \( n_i = n_0 \Theta(z) \) (\( Z = 1 \) for

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3See, e.g., Key et al. (1998), Wharton et al. (1998), H. Chen et al. (2009), Tanimoto et al. (2009), and Nilson et al. (2010), and references therein.

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4In general the main pulse is preceded both by short pulses of duration similar to the main pulse and by a much longer pedestal due to amplified spontaneous emission.

5This effect is also commonly referred to as “vacuum heating.” See Gibbon (2005b) for a discussion on the origin of the name.
and III.C.1). For circular polarization and normal incidence we thus expect electrons, equals the total radiation pressure on the target surface.

\[
\frac{d^2 \xi}{dt^2} = \left\{ -\omega_p^2 \xi - eE_d/m_e \right\} (x_0 + \xi > 0), \quad \left\{ +\omega_p^2 \xi - eE_d/m_e \right\} (x_0 + \xi < 0).
\]

(10)

From Eq. (10) we see that electrons crossing the boundary \((x = x_0 + \xi < 0)\) feel a secular force \(\omega_p^2 x_0\) leading to dephasing from \(E_d\) and acceleration (Mulser, Ruhl, and Steinmetz, 2001). Equation (10) can be solved numerically for a discrete but large ensemble of electron “sheets” (corresponding to a set of values of \(x_0 > 0\)), with the prescription to exchange the values of \(x_0\) for two crossing sheets to avoid the onset of singularity in the equations. Representative trajectories of electrons moving across the interface are found as in Fig. 5. Electrons whose trajectory extends in vacuum for half or one period of the driving field and then reentering at high velocity inside the plasma are observed. Similar trajectories are found in electromagnetic and self-consistent simulations (see Sec. II.B.2).

Note that the cold plasma assumption is consistent with the requirement that the external field should be strong enough to overcome the potential barrier which, in an equilibrium state, confines warm electrons inside a bounded plasma (such a barrier corresponds to a Debye sheath; see also Secs. II.C.1 and III.C.1). For \(\omega_p \gg \omega\) and nearly total reflection, the laser field component normal to the surface has an amplitude \(E_\perp \approx 2E_0 \sin \theta\), with \(E_0 = (4\pi I/c)^{1/2}\) the amplitude in vacuum. The sheath field is \(E_s \approx T_e/eA_D = (4\pi n_0 T_e)^{1/2}\), so that the condition \(E_\perp > E_s\) may be rearranged as \(4(I/c)\sin^2 \theta > n_0 T_e\). This implies (at nongrazing incidence) that the radiation pressure should exceed the thermal pressure and thus counteract the thermal expansion and steepen the density profile, making the assumption of a steplike plasma more self-consistent.

For \(S\) polarization or normal incidence there is no component of the electric field perpendicular to the surface. However, for high intensities the magnetic force term becomes important and may drive electron oscillations along the density gradient also for normal incidence. This effect is commonly named “\(J \times B\)” heating (Kruer and Estabrook, 1985). By considering the driving capacitor field as a model for the magnetic force component, the related electron dynamics may still be described using the above outlined models, but with two significant differences. First, to lowest order the magnetic force oscillates at peak amplitude \(0.5n_0 w_c/c\) in vacuum and a \(\sin^2(\pi/2\tau)\) rising front with \(\tau = 5 T\) where \(T = 2\pi/\omega\). A density \(n_e/n_c = (\omega_p/\omega)^2 = 5\) is assumed.

\[
\mathbf{A}(x, t) = \frac{A(x)}{\sqrt{1 + \epsilon^2}}(\hat{y} \cos \omega t + \hat{z} \sin \omega t)
\]

(11)

with \(0 \leq \epsilon \leq 1\). Using \(\mathbf{B} = \nabla \times \mathbf{A}\) and \(\mathbf{p}_L = e\mathbf{A}/c\) for the transverse momentum of electrons, the \(-e(\mathbf{v} \times \mathbf{B})/c\) force can be written as

\[
-e \frac{\Sigma}{c} \times \mathbf{B} = -\hat{x} \frac{\epsilon^2 \partial A^2(x)}{4m_e \gamma c^2} \left( 1 + \frac{1 - \epsilon^2}{1 + \epsilon^2} \cos^2 \omega t \right).
\]

(12)

showing that the oscillating component vanishes for circular polarization (\(\epsilon = 1\)).

The integral over \(x\) of \(n_e f_{px}\), where \(f_{px} = \langle f_x \rangle = \langle -e(\mathbf{v} \times \mathbf{B}/c)_x \rangle\) is the steady ponderomotive force density on electrons, equals the total radiation pressure on the target surface. For circular polarization and normal incidence we thus expect radiation pressure to push the target while electron heating is quenched. These conditions have been investigated in order to optimize radiation pressure acceleration of ions versus other mechanisms driven by hot electrons; see Sec. IV.A.

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6This numerical implementation basically corresponds to the pioneering, elementary model of plasma simulation formulated by Dawson (1962).

7A more detailed analysis shows that electron heating is quenched when the parameter \(\epsilon\) exceeds some threshold value; see Rykovanov et al. (2008) and Macchi, Liseikina et al. (2009).
2. Simulations, multidimensional effects, and simple estimates

A more quantitative description of laser absorption and hot electron generation requires numerical simulations. To address electromagnetic effects in his model Brunel (1988) performed two-dimensional (2D) PIC simulations in a plane wave, oblique incidence geometry. Several later studies using 1D simulations with the “boosted frame” technique (Bourdier, 1983) are summarized and reviewed by Gibbon et al. (1999). The absorption degree of a P-polarized laser pulse is quite sensitive to the incidence angle and the density scale length, with the latter varying on the time scale of ion motion (Gibbon, 1994) yielding a time-dependent absorption. Experimental attempts (Flacco et al., 2008; McKenna et al., 2008; Batani et al., 2010) have been made to vary the density scale length in order to increase absorption in hot electrons and consequently to enhance ion acceleration (see Sec. III.E).

Hot electron generation tends to become more efficient for lower plasma densities and, particularly, close to the critical density \( n_c \), as it is observed that stronger coupling and volumetric heating occurs near the transmission threshold. A “near-critical” plasma may be produced either by the laser prepulse or by using a special target material, e.g., a low-density foam (see Sec. IV.D).

2D simulations reveal additional effects, as for instance the deformation of the plasma surface due to “hole boring” (HB) driven by radiation pressure (see also Sec. IV.A.1), which changes the local incidence angle (Wilks et al., 1992), leading to increased absorption and providing a dynamic “funnel” effect collimating the electron flow inside the target (Ruhl et al., 1999). A similar dynamics occurs in nanocones targets which have proved to be effective in enhancing hot electron generation (Sentoku et al., 2004; Nakamura et al., 2009; Gaillard et al., 2011, and references therein).

Absorption is also sensitive to small-scale surface deformations, either self-generated or preimposed, so that the use of microstructures on the front target surface has also been suggested as a way to enhance hot electron generation; see, e.g., Klimo et al. (2011), and references therein. Another possible approach is the use of grating surfaces where the resonant excitation of surface plasma waves can also lead to very high absorption (Raynaud et al., 2007; Bigongiari et al., 2011).

The high sensitivity of hot electron generation to laser and plasma parameters partly accounts for data scatter and differences observed in the many experimental investigations reported in the literature, with the above mentioned prepulse effects bringing additional complexity. For these reasons, absorption values and characteristics of the hot electron distribution are often taken into account in a phenomenological way. It has often been considered acceptable to assume the hot electron distribution to be Maxwellian with a temperature \( T_h \) given by Eq. (6) as a function of the laser irradiance. Figure 6 presents a collection of temperature measurements obtained for subpicosecond pulses up to the year 2000 (Gibbon, 2005b); these data broadly support a scaling of \( T_h \) as \( (I X^2)^{1/2} \). The total fractional absorption in hot electrons \( \eta_h \) is usually estimated to be in the 10%–30% range, with experimental indications of possibly quite higher values at ultrarelativistic intensities (Ping et al., 2008).

An energy flux balance condition such as \( \eta_h I \approx n_h v_h T_h \) (with \( v_h \approx c \) at ultrahigh intensities) may then be used to estimate the “initial” density of hot electrons \( n_h \), which usually is not larger than \( n_c \), consistently with the argument that \( n_h \) cannot exceed the density of the region where hot electrons are generated.

Inside the target, the effective density may become different from the above estimate for \( n_h \) under particular conditions due to, e.g., the angular divergence of the electron flow or to electron refluxing effects depending on the electron time of flight and recirculation and thus on the target thickness (Mackinnon et al., 2002). Still one can roughly estimate the total number of hot electrons \( N_h \) by an energy balance relation \( N_h \sim \eta_h U_L / T_h \), where \( U_L \) is the energy of the laser pulse. The angular divergence \( \theta_{div} \) is also estimated from experiments to range between 20° and 60° and to increase with irradiance (Green et al., 2008, and references therein), although such estimates might depend on the accuracy of the sheath field modeling (Ridgers et al., 2011).

3. Hot electron transport in solid matter

Transport of hot electrons in solid matter has been extensively investigated also because of its relevance to the electron-driven fast ignition (FI) scheme in inertial confinement fusion (ICF) [see Freeman et al. (2006) for a survey]. Key issues characterizing this regime are the very high values of the currents and the effect of self-generated fields. From the above estimates it can be inferred that near the front surface of the target the current density \( j_h = -e n_h v_h \) associated to hot electrons may reach values up to \( j_h \sim e n_c c \approx 4.8 \times 10^{12} \text{ A cm}^{-2} \), corresponding to a total current of \( \sim 15 \text{ MA} \) over a circular spot of 10 μm radius. This large current must be locally neutralized by a return current \( j_r \) such that \( j_h + j_r \approx 0 \); otherwise, either the electric field generated by the charge imbalance or the magnetic field generated by the free flowing current \( j_h \) would be strong enough to stop the...
hot electrons (Davies et al., 1997; Passoni et al., 2004). The free, cold electrons contributing to the return current are either present as conduction electrons in metals or produced by field and collisional ionization in insulators (Tikhonchuk, 2002). Additional complexity is introduced by effects such as target heating and hot electron refluxing, which have been inferred in several experiments (Bellei et al., 2010; Nilson et al., 2011; Quinn et al., 2011, and references therein). Filamentation instabilities and dependence on the target material have also been extensively studied (Fuchs et al., 2003; Manclossi et al., 2006; McKenna et al., 2011, and references therein). Simulation models accounting for both collisional effects and self-consistent generation of quasistatic fields are needed for quantitative investigations. Finally, it is noticeable that at least a fraction of hot electrons propagates coherently through the target conserving the temporal periodicity of the driving force, i.e., as bunches with $\omega$ or $2\omega$ rate depending on incidence angle and polarization, as inferred by optical transition radiation measurements (Popescu et al., 2005).

### C. Ion acceleration mechanisms

In this section we give an overview of ion acceleration mechanisms including both those proposed to explain early experimental results in solid targets and those investigated later, either following inspiration from theoretical work or testing novel target designs. Some of the mechanisms described and the target regions where they are active are indicated in Fig. 7. Ion acceleration models will be described more in detail in Secs. III and IV along with the most relevant experiments.

#### 1. Rear surface acceleration

As outlined in Sec. II.B, a very intense current of high-energy hot electrons may be generated at the front side of the target and eventually reach the rear side. There, as the hot electrons cross the rear side boundary and attempt to escape in vacuum, the charge unbalance generates a sheath field $E_s$, normal to the rear surface. Since $E_s$ must backhold electrons with a typical “temperature” $T_h$, the typical spatial extension of the sheath $L_s$ will be related to $E_s$ by

$$eE_s \sim \frac{T_h}{L_s}. \quad (13)$$

From dimensional arguments, assuming a steep interface and $n_h$ and $T_h$ as the only parameters, $L_s$ may be roughly estimated as the Debye length of hot electrons, $L_s \sim \Lambda_{h} = \left(\frac{T_h}{4\pi e^2 n_h}\right)^{1/2}$. Assuming the simple scalings of Sec. II.B for $T_h$, taking a laser irradiance $I_A^2 = 10^{20}$ W cm$^{-2}$ $\mu$m$^{-2}$ and a fractional absorption $\eta_h = 0.1$, we find $T_h \approx 5.1 m_ec^2 = 2.6$ MeV, $n_h \approx 8 \times 10^{20}$ cm$^{-3}$, $\Lambda_{h} = 4.2 \times 10^{-5}$ cm, and $E_s \approx 6 \times 10^6$ V cm$^{-1}$. This large field will backhold most of the escaping electrons, ionize atoms at the rear surface, and start to accelerate ions. As a rough estimate, a test ion crossing the sheath would acquire the energy $\mathcal{E}_i \sim Z e E_s L_s = Z T_h$, resulting in MeV energies and a scaling as $1^{1/2}$ if $T_h \approx \mathcal{E}_p$ given by Eq. (6) holds. Protons from a thin layer of hydrogen-containing impurities on the surface will be in a very favorable condition for acceleration because of both their initial position, located at the maximum of the field, and their highest charge-to-mass ratio so that they will be more rapid than heavier ions in following electrons and screening the sheath field. This is the qualitative scenario for TNSA of protons as introduced by Wilks et al. (2001) to explain their experimental results on proton acceleration (Hatchett et al., 2000; Snayevly et al., 2000).

The essential features of the TNSA mechanism have been supported by several experiments and TNSA has become the reference framework to interpret observations of multi-MeV protons from the target rear side. Various schemes for beam optimization and control have been designed on the basis of TNSA. Detailed discussions of main experimental findings are reported in Secs. III.A, III.B, and III.E.

From a theoretical viewpoint, there are two main categories of models which describe TNSA, namely, “static” and “dynamic” models which, depending on the starting assumptions, allow one to provide simplified analytical descriptions useful for interpreting experimental data. These models and related numerical investigations are presented in Sec. III.C.

#### 2. Front surface acceleration

Already in the first measurements of proton acceleration in the forward direction, the possibility of a contribution originating at the front surface of the target was conceived (Clark et al., 2000a; Maksimchuk et al., 2000). As a consequence, mechanisms leading to ion acceleration in such a region have also been extensively investigated.

At the front surface, the intense radiation pressure of the laser pulse pushes an overdense target inward, steepening the density profile and bending the surface; this process is commonly named hole boring. The recession velocity $v_{1HB}$ of the plasma surface...
may be estimated by balancing the electromagnetic and mass momentum flows $I/c \sim n_e (m_i v_{th}) v_{th}$. This corresponds to an energy per nucleon $E_i = m_i v_{th}^2 / 2 \sim I / m_i c$. The scaling with the laser intensity $I$ is more favorable than the $1/2$ scaling for TNSA and suggests that RPA effects should become more important for higher intensities. More accurate, relativistic, and dynamic modeling is presented in Sec. IV.A.1 along with related experimental indications.

Radiation pressure action and hot electron temperature may also lead to the generation of collisionless shock waves (Tidman and Krall, 1971) with high Mach number $M$. Such waves are associated with the reflection of ions from the shock front, resulting in a velocity $v_t = 2 M c_e$, and an energy per nucleon $E_i = 2 m_p c^2 c_s^2 = 2(Z/A) M^2 T_{th}$, being $c_s = \sqrt{Z T_{th}/A m_p}$ the ion sound velocity. Such a CSA scenario and related experiments are discussed in Sec. IV.B.

Finally, the possibility of front side (or bulk) acceleration being favored by resistivity effects is discussed in Sec. IV.E.

3. Acceleration schemes using innovative targetry

Both TNSA and RPA can have different features in targets having peculiar geometrical and physical properties, if compared to the solid targets used in the 2000 experiments (Clark et al., 2000a; Maksimchuk et al., 2000; Snively et al., 2000) which had thickness in the 1–100 $\mu$m range and were much wider than the laser spot diameter. Experimental investigations of “ultrathin,” submicrometric targets require extremely “clean,” prepulse-free pulses to avoid early target evaporation and thus became possible only recently thanks to the development of advanced pulse cleaning techniques (see Sec. III.E). The use of “mass-limited” targets which also have limited lateral dimensions (in the sub-mm range) allows the refluxing and concentration of hot electrons in a small volume and may lead to higher ion energies via TNSA. These studies are presented in Sec. III.E.

For RPA, a sufficiently thin foil target is expected to be accelerated as a whole. Assuming the foil to be a perfect mirror of thickness $\ell$, its nonrelativistic motion may be simply described by $m_i \ell dV/dt = 2 I/c$ from which we obtain an energy $E_i = m_i V^2/2 = (2/m_i) (F/n_e c^2)$, where $F = \int \vec{F} \, dt$ is the laser pulse fluence. This is the basis of the “light sail” (LS) regime of RPA (see Sec. IV.A.2) which seems very promising in view of the foreseen fast scaling and the intrinsic monoenergeticity.

For extremely thin (a few nm) targets, the breakthrough of the laser pulse through the foil due to relativistic transparency may stop LS-RPA, but at the same time lead to additional strong heating of electrons. This effect opens up a regime of possible enhanced acceleration (BOA), which will be discussed in Sec. IV.C.

In general, reducing the effective size of the target allows for laser pulse penetration, volumetric heating, and energy confinement, which can lead to efficient ion acceleration even at low laser pulse intensities. As a well-known example, the interaction of ultrashort, moderate intensity ($\approx 10^{16}$ W cm$^{-2}$) pulses with subwavelength clusters allowed acceleration of ions up to energies sufficient to produce nuclear fusion reactions (Ditmire et al., 1997, 1999). A limitation on the use of such clusters as ion sources is the isotropic ion emission and the resulting low brilliance. “Droplet” targets with size of the order of one wavelength have been investigated as a trade-off approach, as discussed in Sec. III.E.2.

As mentioned previously, special target materials may be used to produce plasmas with density close to $n_e$ (for laser wavelengths $\lambda \sim 1 \mu$m) in order to enhance the generation of hot electrons which drive TNSA (see Sec. IV.D). Gas jet targets have also been used both with $\lambda \sim 1 \mu$m lasers to investigate ion acceleration in underdense plasmas (see Sec. IV.D) and with CO$_2$ lasers ($\lambda \sim 10 \mu$m) for studies of RPA and CSA in moderately overdense plasmas (see Secs. IV.A and IV.B). Apart from the possibility to vary the background density, using flowing gas jets as targets is of interest because they enable the interaction with a pure proton plasma and are suitable for high-repetition rate operation as needed for most foreseen applications (see Sec. V).

D. Particle-in-cell simulations

The PIC method (Dawson, 1983; Birdsall and Langdon, 1991), mentioned in the Introduction, is the most widely used approach to the kinetic simulation of plasmas. The PIC method provides a solution to the Maxwell-Vlasov system using a Lagrangian approach, with fields and currents allocated on a fixed grid and the phase space represented by an ensemble of computational particles. Thus, the PIC method is mostly appropriate to describe collisionless laser-plasma interaction dynamics, although models are available to implement either collisions [see, e.g., Fiura et al. (2011), and references therein] or ionization [see, e.g., Petrov, Davis, and Petrova (2009), and references therein].

PIC simulations of laser interaction with solid-density plasmas at peak densities typically exceeding $10^2 n_e$ are a very demanding task even when the most powerful supercomputers are used. As a minimum requirement, one has to resolve temporal scales $\sim \omega_p^{-1}$ and spatial scales $\sim c/\omega_p$ where $\omega_p \sim n_e^{1/2}$. Thus, when approaching parameters of a real experiment, relevant lengths such as the laser beam waist may correspond to thousands of grid points in each spatial direction and typical dynamic times to thousands of time steps. In addition, kinetic effects such as the generation of hot electron tails in the distribution function and large density variations need very large numbers of particles to be properly resolved. For these reasons, realistic 3D simulations with proper resolution are typically beyond computational possibilities. These constraints result, in most of the cases, in either using a reduced dimensionality or in relaxing the actual parameters to some extent, e.g., by assuming relatively low densities or short scales. For some peculiar problems, development of hybrid modeling may be appropriate, as discussed in Sec. III.C.4.

Despite the above mentioned limitations, several groups have been able to perform large-scale 3D simulations relevant to ion acceleration regimes such as, e.g., TNSA (Pukhov, 2001), RPA (Esirkepov et al., 2004; Tamburini et al., 2012), and BOA (Yin et al., 2011a). The use of parallel supercomputers has also allowed extended multiparametric studies (see Fig. 8) aimed to infer scaling laws and to provide
and focal spot diameter $D$ and Tajima, 2006.

have required either modifications of established diagnostics (e.g., broad spectrum, high flux, significant divergence) or the development of new ones.

Typically, RCFs are used in a stack arrangement, so that information on the flux of particles directed at the layer. Against the dose released in the film, and therefore provide a consequent change in optical density can be calibrated.

ebrochromic film (RCF) (McLaughlin et al., 1996) is a detector which is favored by many experimenters, since the early work by Snavely et al. (2000), mainly due to simplicity of use. This is a high-dose, high-dynamic range film, widely used in medical context for x-ray dosimetry (Hiroomand-Rad et al., 1998). The films consist of one or more active layers containing a microcrystalline monomeric dispersion buried in a clear plastic substrate. Typical examples are the MDV3 and EBT2 Gafchromic varieties. After interaction with ionizing radiation, the active material undergoes polymerization and the film changes its color from nearly transparent to blue. The consequent change in optical density can be calibrated against the dose released in the film, and therefore provide information on the flux of particles directed at the layer. Typically, RCFs are used in a stack arrangement, so that each layer acts as a filter for the following ones in the stack. The signal in a given layer will be due only to ions having energy $E \geq E_B$, where $E_B$ is the energy of the ions which reach their Bragg peak within the layer (see Fig. 9). In the first approximation, for an exponential-like spectrum such as those typically produced by TNSA, the dose deposited in a layer can be taken as proportional to the number of protons with $E \sim E_B$, allowing a rough spectral characterization of the beam. Various, more refined procedures have been developed for deconvoluting the spectral information (either integrated across the beam or angularly resolved) in multilayer RCF data (Breschi et al., 2004; Hey et al., 2008; Nuernberg et al., 2009; Kirby et al., 2011).

E. Ion diagnostics

The specific properties of laser-driven ion beams (e.g., broad spectrum, high flux, significant divergence) have required either modifications of established diagnostics techniques or the development of new ones.

Radiochromic film (RCF) (McLaughlin et al., 1996) is a detector which is favored by many experimenters, since the early work by Snavely et al. (2000), mainly due to simplicity of use. This is a high-dose, high-dynamic range film, widely used in medical context for x-ray dosimetry (Hiroomand-Rad et al., 1998). The films consist of one or more active layers containing a microcrystalline monomeric dispersion buried in a clear plastic substrate. Typical examples are the MDV3 and EBT2 Gafchromic varieties. After interaction with ionizing radiation, the active material undergoes polymerization and the film changes its color from nearly transparent to blue. The consequent change in optical density can be calibrated against the dose released in the film, and therefore provide information on the flux of particles directed at the layer. Typically, RCFs are used in a stack arrangement, so that each layer acts as a filter for the following ones in the stack. The signal in a given layer will be due only to ions having energy $E \geq E_B$, where $E_B$ is the energy of the ions which reach their Bragg peak within the layer (see Fig. 9). In the first approximation, for an exponential-like spectrum such as those typically produced by TNSA, the dose deposited in a layer can be taken as proportional to the number of protons with $E \sim E_B$, allowing a rough spectral characterization of the beam. Various, more refined procedures have been developed for deconvoluting the spectral information (either integrated across the beam or angularly resolved) in multilayer RCF data (Breschi et al., 2004; Hey et al., 2008; Nuernberg et al., 2009; Kirby et al., 2011).

Plastic track detectors such as CR39 (Enge, 1995), which have the advantage of being insensitive to x rays and electrons, have been widely used also in multistack arrangements, e.g., by Clark et al. (2000a). CR39 layers (typically 0.25–1 mm in thickness) require etching in a NaOH solution after exposure to ions, so that the damage tracks created by the particles can be revealed thanks to the different etching rate in the track compared to the undamaged bulk (Ségui et al., 2003). After etching, the single tracks can be counted, which provides a direct measurement of the number of protons hitting the detector. CR39 works better for low particle fluxes, as at high flux (typically above $10^8$ particles cm$^{-2}$) or for long etching times the tracks start to overlap, leading to saturation (Gaillard et al., 2007).

The interaction of laser-driven high-energy ions with secondary targets can initiate a number of nuclear reactions (see Sec. V.E), which can be used to diagnose the beam properties with the ability to provide absolute particle numbers with a linear response and virtually no saturation at high flux. The $^{65}$Cu$(p, n)^{65}$Zn reaction in copper stacks has been used to quantify the proton numbers through measurement of $\beta^+$ decay of $^{65}$Zn nuclei, using a NaI detector-based coincidence counting system (Santala et al., 2001; Spencer et al., 2001). Techniques employing a single Cu layer, in which a range of isotopes resulting from proton-induced nuclear reactions is analyzed in order to reconstruct the proton spectrum, have also been used (Yang et al., 2004b). Spectral resolution is provided by a combination of filtering and known thresholds for the considered reaction. The above described approaches provide particle flux integrated over the whole beam cross section. Contact radiography of $(p, n)$-generated isotopes in activation samples (where the activated foil is placed in contact with RCF) has been
developed (Clarke et al., 2008; Offermann et al., 2010) as a way to achieve 2D images of the beam profile with high spatial resolution and extremely high-dynamic range. Neutron spectra produced through fusion reactions of the type \( \text{D}(d, n)^3\text{He} \) have been used as a diagnostic of laser-driven deuterium ions inside a laser-irradiated target (Habara et al., 2003, 2004a, 2004b).

Obtaining spectra with high-energy resolution requires the use of magnetic dispersion techniques. In simple magnetic spectrometers [see, e.g., H. Chen et al. (2008)] the ions, spatially selected by an entrance slit or pinhole, are dispersed along one spatial direction according to their energy by a \( \sim 1 \) T magnetic field \( \mathbf{B} \). This arrangement, which discriminates particles according to their energy but not to their charge-to-mass ratio, is adequate for diagnosing the high-energy proton spectrum in “standard” TNSA experiments in which protons are the dominant accelerated species (Hegelich et al., 2002).

A more complete spectral characterization of multicomponent ion beams can be obtained with Thomson parabola spectrometers, based on the principle for mass spectrometry introduced by Thomson (1911). A schematic of the device is shown in Fig. 10(a). Ions are deflected by parallel \( \mathbf{E} \) and \( \mathbf{B} \) fields [with \( E \sim 10^4 \text{ V/m} \) (Sakabe et al., 1980)] resulting in a characteristic deflection pattern in which species with different charge-to-mass ratio form separated parabolic traces in the detector plane, as shown in the typical image of Fig. 10(b). Modified magnetic and Thomson spectrometers, having imaging and angular resolution capability, have also been developed (Ter-Avetisyan et al., 2009; Chen et al., 2010; Jung et al., 2011a).

The detectors used in conjunction with these spectrometers are typically either CR39, image plates (IP), scintillating plates, or microchannel plates (MCPs). Photostimulable IPs are filmlike radiation image sensors, developed for x-ray medical imaging, which are composed of specially designed phosphors that trap and store radiation energy in metastable excited states and can be absolutely calibrated in terms of particle flux (Manić et al., 2008; Freeman et al., 2011). Scintillating plates (Green et al., 2010) or MCPs (Ter-Avetisyan, Schnrer, and Nickles, 2005) are favored in situations where online detection is required (e.g., high-repetition laser systems), as the scintillator screen or the MCPs phosphor are imaged on a charge-coupled device (CCD) and the detector does not require replacing after exposure. Scintillators can also be used for beam profiling (Sakaki et al., 2010), with potential for energy range selection (Green et al., 2011).

A different approach also allowing online beam monitoring is the use of time-of-flight (TOF) techniques, where the broadband ions are left to propagate over a given distance and then detected employing scintillating plates coupled to a photomultiplier (Nakamura et al., 2006), Faraday cups, or semiconductor detectors (Margarone et al., 2011). The time-varying signal produced by the detectors maps the ion energy spectrum, although the finite response time of the detector and realistic propagation distances limits the energy range over which these measurements can be applied. State-of-the-art TOF-MCP detectors allow for measurements of protons with a kinetic energy up to \( \sim 20 \) MeV/nucleon (Fukuda et al., 2009).

### III. TARGET NORMAL SHEATH ACCELERATION

#### A. TNSA scenario: Main experimental observations

As anticipated in Sec. II.C the TNSA process (Wilks et al., 2001) is a consequence of the large charge separation generated by hot electrons reaching the rear side of the target. There, a cloud of relativistic electrons is formed, extending out of the target for several Debye lengths, and giving rise to an extremely intense electric field, mostly directed along the normal to the surface. A consequent distinctive feature is that ions are accelerated perpendicularly to the surface, with high beam collimation. The electric field generated at the rear surface depends on parameters of the electron distribution (temperature, number, divergence) as well as of the surface (mostly its density profile as detailed below).

The acceleration is most effective on protons, which can be present either in the form of surface contaminants or among the constituents of the solid target as in plastic targets. The heaviest ion populations provide a positive charge with much more inertia, thus creating the charge separation which generates the accelerating field. Part of the heavy population can also be effectively accelerated, on a longer time scale, if the proton number is not high enough to balance the charge of the escaping hot electrons, and especially if impurity protons are removed before the interaction, for example, by preheating the target (Hegelich et al., 2002). In this way, ions of several different species may be accelerated (Hegelich et al., 2005).

Several observations strongly supported the TNSA scenario taking place at the rear side. Already Snavely et al.
(2000) gave clear evidence that the emission was normal to the rear surface using wedge targets which effectively have more than one rear surface. Two separate proton beams were observed in the directions normal to the two rear surfaces of the wedge (see Fig. 11).

Mackinnon et al. (2001) reported experimental observations of the interaction of ultraintense laser pulses using targets with and without preformed plasmas on the rear surface of the foil. The peak and mean energies of the proton beam were found to strongly depend on the plasma scale length at the rear of the target. While an energetic proton beam was obtained with an unperturbed rear surface, no evidence of high-energy protons was recorded when a large local scale length in the ion density at the rear surface was induced, consistently with the dependence of the accelerating field on the scale length in Eq. (13).

Hegelich et al. (2002) used Al and W foils as targets, resistively heated to remove hydrogen contaminants and coated on the rear side with thin C and CaF$_2$ layers, respectively. The observation of high-energy C, Ca, and F ions from these prepared source layers proves the existence of an effective rear surface acceleration mechanism (see Fig. 12). Further evidence was provided by Allen et al. (2004) who showed that removing contamination from the back surface of Au foils strongly reduced the total yield of accelerated protons, while removing contamination from the front surface of the target had no observable effect on the proton beam.

Further proof that ions are accelerated at the rear side was given by the observation that a structuring (i.e., grooving) of the rear surface produced modulations in the proton beam (Cowan et al., 2004). This effect also evidences the high laminarity of the beam and allows one to measure its emittance, as discussed in Sec. III.B.

Direct experimental evidence of the generation of an initial intense sheath field at the rear surface and a late time field peaking at the beam front was provided by Romagnani et al. (2005) using the proton imaging technique (see Sec. V.A). In this case, TNSA itself provided a unique diagnostic which allowed direct experimental confirmation of the nature of the acceleration process. Figure 13 shows a temporal series of “proton images” in which the propagation of the bell-shaped front of ion expansion can be observed.

More recent developments have shown the possibility to significantly control and optimize the TNSA process by acting on the detailed properties of both the laser pulse and the irradiated target. These developments have also highlighted the capability of achieving interesting and promising variations of the main scheme, also in light of possible specific applications. These topics will be presented in Sec. III.E.

B. Characterization of beam properties

Several experiments have investigated in detail the properties of the TNSA ion beams. The energy spectrum of the beams is typically broadband, up to a cutoff energy (see Fig. 2). The particle number per MeV can be roughly approximated by a quasithermal distribution with a sharp cutoff at a maximum energy (Kaluza et al., 2004; Fuchs et al., 2005) which scales with the laser parameters as discussed in Sec. III.D. Many experiments have reported spectral observations for a wide range of laser and target parameters, and partial surveys have been provided in a
A number of experimental studies have been devoted to the investigation of the spatial and angular characteristics of the emitted beams. These are closely dependent on the electron sheath spatial distribution, and consequently on the target properties (resistivity, surface roughness, etc.) affecting the electron propagation.

It was observed early on that the use of conducting targets leads to smooth proton beam profiles with a sharp boundary, as detectable, for example, in RCF data (Snavely et al., 2000; Fuchs et al., 2003), while using dielectric targets creates nonhomogeneities in the proton density across the beam section. In the latter case, the transport of the electron current is prone to electromagnetic instabilities, which break the hot electron flow into filaments. This leads to an uneven electron sheath at the target rear (Manclossi et al., 2006) and consequently to a modulated proton beam cross section (Roth et al., 2002; Fuchs et al., 2003). The close correlation between proton beam properties and electron beam transport characteristics has indeed been exploited in a number of experiments, which have used the proton beam as a diagnostic for the electron beam behavior inside the target, revealing, beside the aforementioned differences related to the target conductivity (Fuchs et al., 2003), effects of magnetic collimation on the beam transport (Yuan et al., 2010; Gizzi et al., 2011) or the role of lattice structure in dielectric targets (McKenna et al., 2011). Other factors that can lead to structured beam profiles even in conducting targets are surface roughness at the target rear, resulting in a randomized local orientation of the protons (Roth et al., 2002), and intensity modulations in the focal spot which can be coupled to the protons via structured electron beams in medium-Z thin targets (Fuchs et al., 2003).

The existence of a sharp angular boundary in the proton angular distribution (clearer in higher-Z and thicker targets) is consistent with a bell-shaped transverse distribution of hot electrons in the rear surface sheath due to the fact that the density will naturally be higher along the laser axis and decrease with transverse radius. Protons are accelerated normal to the local isodensity contour, and the presence of an inflection point in the sheath therefore results in a maximum angle of acceleration (Fuchs et al., 2003). Comparison of experimental data with simple electrostatic models indicates that the shape of the accelerating sheath is generally Gaussian (Fuchs et al., 2003; Carroll et al., 2007) as also observed directly in sheath imaging data (Romagnani et al., 2005); see Fig. 13.

A modulation of the proton beam angular distribution can be introduced purposefully by microstructuring the target surface. A technique based on micromachining shallow grooves on the rear surface of the target, introduced by Cowan et al. (2004), has successfully been used in several experiments for diagnosing the emission properties of the beam (Nuernberg et al., 2009). From these patterned targets, a periodic modulation of the beam angular envelope arises during TNSA due to the local perturbation of the target normal direction, which causes an initial beam microfocusing at the groove locations. As the sheath expands, the local modulations are added over the global divergence of the beam (Ruhl, Cowan, and Fuchs, 2004) and are observable as a modulation of the proton dose on the detector (see Fig. 14). The modulations can be used as a spatial fiducial from which one can infer the dimensions of the area from where ions are accelerated, i.e., the proton or ion source size (Brambrink et al., 2006). Similar information has been obtained by considerations based on the projection by the ion beam of patterned objects, e.g., metal meshes (Borghesi et al., 2004) or knife edges (Schreiber et al., 2004).

A crucial property of laser-driven ion beams is their laminarity. In an ideal laminar source, there is a correlation between the location within the source from where a particle is emitted and the angle of emission. The degree of laminarity of charged-particle beams is typically expressed in terms of their transverse emittance, a quantity which is proportional to the area of the bounding ellipsoid of the distribution of particles in phase space (Humphries, 1990). The highest quality ion beams have the lowest values of transverse and longitudinal emittance, indicating a low effective transverse ion temperature and a high degree of angle space and time-energy correlation, respectively. Transverse emittance has been measured in a number of experiments. Methods based on mesh projection (which is broadly equivalent to the established “pepper-pot” method) indicate that the emittance is less than 0.1 π mm mrad (Borghesi et al., 2004; Ceccotti et al., 2008; Nishiuchi et al., 2008). The above discussed groove imaging technique allows a full reconstruction of the transverse phase space, and possibly a more precise estimation of the transverse emittance (Cowan et al., 2004; Brambrink et al., 2006; Nuernberg et al., 2009) which, for protons of up to 10 MeV, has been estimated as 0.004 mm mrad, i.e., 100-fold better than typical rf accelerators and at a substantially higher ion current (kA range).

It has also been found that the removal of the comoving electrons after 1 cm of the quasineutral beam expansion did not significantly increase the measured proton transverse...
emittance, as shown in Fig. 14 (Cowan et al., 2004). This last observation is important since, in order to take advantage of the exceptionally small proton beam emittance in future applications, e.g., to capture them into a postaccelerator, removal of the comoving electrons without significantly perturbing the protons is crucial.

The ultralow emittance stems from the extremely strong, transient acceleration that takes place from a cold, initially unperturbed surface and from the fact that during much of the acceleration the proton space charge is neutralized by the comoving hot electrons. Using the ion beam as a projection source, having a low-emittance beam is equivalent to projecting from a virtual pointlike source located in front of the target, with much smaller transverse extent than the ion-emitting region on the target surface (Borghesi et al., 2004; Nuernberg et al., 2009). As discussed in Sec. V.A, this property of laser-driven ion beams allows one to implement point-projection radiography with high spatial resolution.

C. TNSA modeling

The experimental observations and the considerations summarized in Sec. III.A suggest the following assumptions, leading to the formulation of a relatively simple system of equations which can be investigated analytically and numerically (Passoni et al., 2004). First, we assume an electrostatic approximation, so that the electric field \( \mathbf{E} = -\nabla \phi \) where the potential \( \phi \) satisfies Poisson’s equation

\[
\nabla^2 \phi = 4\pi e \left( n_e - \sum_j Z_j n_j \right), \tag{14}
\]

with the sum running over each species of ions, having density \( n_j \) and charge \( Z_j \). As a consequence of the laser-solid interaction, the electron density \( n_e \) may be described as composed of at least two qualitatively distinct populations, which will be labeled cold and hot in the following, having densities \( n_c \) and \( n_h \) such that \( n_e = n_c + n_h \). In the simplest approach, thermal effects are neglected for the cold population, while \( n_h \) is given by a one-temperature Boltzmann distribution (notice that in this section “e” indicates the mathematical constant e = exp(1) = 2.71828 · · · while e indicates as usual the elementary charge),

\[
n_h = n_0 e^{\phi/T_e}. \tag{15}
\]

This expression can be a reasonable first approximation to account for the presence of the self-consistent sheath field and has been used in many works on TNSA\(^9\) but, as discussed below, it can lead to serious problems when the main goal is the estimation of the maximum energy of the accelerated ions. Alternatively, the electron dynamics can be included via either fluid or kinetic equations. It is mostly appropriate to consider two different ion species, a light (\( L \)) and a heavy (\( H \)) population: in this way it is possible, e.g., to model the acceleration of light species present on the surfaces of a solid target made of heavy ions.

\(^9\)See, e.g., Mora (2003), Passoni et al. (2004), Albright et al. (2006), Nishiuchi et al. (2006), and Robinson, Bell, and Kingham (2006).

Depending on the description of the ion populations, two main categories of TNSA models, to be discussed in detail in Secs. III.C.1 and III.C.2, respectively, may be identified as follows. The first includes static models in which it is assumed that the light ions, or at least the most energetic ones, are accelerated in the early stage of the formation of the sheath, so that the latter may be assumed as stationary. With these conditions, the effects of the light ions on the electrostatic potential are usually neglected, while the heavy ion population of the target is considered immobile. The aim is thus to provide the most accurate description of the sheath depending on assumptions on the hot electron distributions. The second category includes dynamic models where the system is described as a neutral plasma in which the ions acquire kinetic energy in the course of the sheath evolution. In several cases a unique ion component is considered. This approach is therefore strongly connected to the classic problem of plasma expansion in vacuum, first considered by Gurevich, Parilikaya, and Pitaevskii (1966). In a cold fluid description, neglecting relativistic effects the ions are described by

\[
\frac{\partial \mathbf{u}_j}{\partial t} + \mathbf{u}_j \cdot \nabla \mathbf{u}_j = -\frac{Z_j e}{m_j} \nabla \phi, \tag{16}
\]

\[
\frac{\partial n_j}{\partial t} + \nabla \cdot (n_j \mathbf{u}_j) = 0 \quad (j = L, H), \tag{17}
\]

where \( \mathbf{u}_j = \mathbf{u}_j(\mathbf{r}, t) \) is the fluid velocity. If the ions are described kinetically, their Vlasov equation for the phase-space distribution \( f_j = f_j(\mathbf{r}, \mathbf{v}, t) \) is

\[
\frac{\partial f_j}{\partial t} + \mathbf{v} \cdot \nabla f_j - \frac{Z_j e}{m_j} \nabla \phi \cdot \frac{\partial f_j}{\partial \mathbf{v}} = 0. \tag{18}
\]

Most of the general studies of plasma expansion and related ion acceleration developed both before and after TNSA experiments\(^10\) as well as more specific models of TNSA\(^11\) so far proposed in the literature can be considered as suitable simplifications of the previous equations, falling into one of the two above mentioned categories (or suitable combinations of them) and obtained adding further, physically motivated assumptions. Most of these models assume a 1D geometry, consistently with the electrostatic approximation, and planar in most cases. This latter assumption, when applied to TNSA modeling, requires the rear surface to be sufficiently flat and


the electron cloud to be spatially uniform in the plane normal to the ion motion.

Note that all the models proposed to describe TNSA are, to a large extent, phenomenological, i.e., they need as input parameters physical quantities which are not precisely known. Since these descriptions give a simplified picture of the acceleration process, the best model in this context may be considered the one which provides the best fit of experimental data with the lowest set of laser and target parameters. This issue will be discussed in Sec. III.D. In principle, these difficulties could be overcome performing realistic numerical simulations, but these generally consider “model” problems due to intrinsic difficulties in the numerical study of these phenomena, such as, for example, the large variations of density from the solid target to the strongly rarefied expansion front. At present, a complementary use of simple models, presented in Secs. III.C.1, III.C.2, and III.C.3, and advanced simulations, discussed in Sec. III.C.4, seems the most suitable option to theoretically approach TNSA.

1. Quasistatic models

Static models assume, on the time scale of interest (i.e., in the sub-ps regime), immobile heavy ions, an isothermal that laser-produced hot electron population, and a sufficiently low number of light ions so that their effect on the evolution of the potential can be neglected and they can be treated as test particles. In this limit, if Eq. (15) is used to describe hot potential can be neglected and they can be treated as test laser-produced hot electron population, and a sufficiently low acceleration of a test proton which is initially at zero energy

\[ \frac{d^2 \phi}{dx^2} = 4\pi \epsilon \left[ n_{0h} e^{\epsilon \phi / T_h} - (Z_H n_{0H} - n_{0h}) \right] = 4\pi \epsilon n_{0h} \left[ e^{\epsilon \phi / T_h} - \Theta(-x) \right], \]

(19)

where we assumed the background charge to fill the \( x < 0 \) region with uniform density. The corresponding electron density and electric field can be calculated, as well as the energies of test ions moving in such potential. This can be considered the simplest self-consistent approach to describe the TNSA accelerating field. The solution of Eq. (19) in the semi-infinite region \( x > 0 \) is (Crow, Auer, and Allen, 1975)

\[ \phi(x) = -\frac{2 T_h}{\epsilon} \ln \left( 1 + \frac{x}{\sqrt{2e} \lambda_{Dh}} \right) - 1, \]

(20)

where \( \lambda_{Dh} = \sqrt{T_h / 4\pi \epsilon^2 n_{0h}} \). The field reaches its maximum at the surface and is given by

\[ E(0) = \sqrt{2} E_0, \quad E_0 = \frac{T_p}{e \lambda_{Dh}}, \]

(21)

which justifies the simple estimates used in Sec. II.C. However, the electrostatic potential (20) leads to an infinite acceleration of a test proton which is initially at zero energy in \( x = 0 \). The reason is that the apparently reasonable choice of the Boltzmann relation poses several difficulties to the analysis (Passoni and Lontano, 2004) because, in order to have an electron density equal to zero at infinity, the self-consistent electrostatic potential must diverge at large distance from the target [mathematically, \( \phi \to -\infty \) as \( x \to +\infty \), see Eq. (15)]. This is not a pathological consequence of the one-dimensional approximation but it is related instead to the fact that the Boltzmann relation implies the existence of particles with infinite kinetic energy, which is not physically meaningful [see also Sec. 38 of Landau and Lifshitz (1980)]. This unphysical behavior can be avoided by assuming an upper energy cutoff \( E_c \) in the electron distribution function, so that \( e\phi \to -E_c \) as \( x \to +\infty \) and the electric field turns to zero at a finite distance. The cutoff assumption can be justified as a consequence of the laser-solid interaction producing electrons with a maximum kinetic energy and of the escape from the system of the most energetic ones (Lontano and Passoni, 2006; Passoni and Lontano, 2008). Experimental indications of target charging due to electron escape have been found by Kar et al. (2008b) and Quinn et al. (2009a). The finite range of the electric field driving TNSA is also apparent in direct measurements (Romagnani et al., 2005).

Still using the Boltzmann relation, it can be assumed the 1D solution given by Eq. (20) to hold only up to a longitudinal distance roughly equal to the transverse size of the sheath, because at larger distances 3D effects should be taken into account (Nishiuchi et al., 2006). Alternatively, by assuming that the hot electron population occupies only a finite region of width \( h \), the solution of Eq. (19) in the vacuum region \( 0 < x < h \) together with the corresponding electric field and electron density can be determined (Passoni and Lontano, 2004).

Another possibility, explored by Schreiber et al. (2006), has been to heuristically assume that the hot electron expansion in vacuum creates a cylindrical quasistatic cloud in the vacuum, behind the target, and a circular positive surface charge on its rear face. The generated electrostatic potential is evaluated on the symmetry axis, along which the most energetic ions are accelerated. The total surface charge and the radius of the distribution are model parameters estimated from experiments (see also Sec. III.D).

In order to consistently overcome the previously discussed limits, Lontano and Passoni (2006) proposed to solve the Poisson equation by assuming that a quasistationary state is established where only those electrons (trapped electrons) with negative total energy \( W = mc^2 (\gamma - 1) - e\phi \) are retained, while those with positive total energy are lost from the system. The corresponding trapped electron density, given by \( n_{\text{tr}} = \int_{W < 0} f_e(x, p) dp \), is included in the Poisson equation and the analytical solutions are determined (Lontano and Passoni, 2006; Passoni and Lontano, 2008; Passoni, Bertagna, and Zani, 2010b). As a general feature, the potential, the electrostatic field, and the electron density distributions go to zero at a finite position \( x_f \) of the order of several hot Debye lengths.

If both electron populations, hot and cold, are considered, it is possible to find an implicit analytical solution of Eq. (19) both inside the target and in the vacuum region. Using a two-temperature Boltzmann relation to describe the electron density, that is, \( n_e = n_{0h} \exp(e\phi / T_h) + n_{0c} \exp(e\phi / T_c) \), the electric field profile turns out to be governed by the parameters \( a = n_{0c} / n_{0h} \) and \( b = T_c / T_h \), as shown in Fig. 15 (Passoni et al., 2004). The presence of the cold
2. Plasma expansion into vacuum

A description of ion acceleration over relatively long times and/or under conditions such that the quasistatic modeling of Sec. III.C.1 is not valid anymore demands for the inclusion of the ion dynamics. The description may be based either on a fluid model, using Eqs. (16) and (17), or on a kinetic one using Eq. (18).

The simplest approach is obtained using a 1D fluid approach, invoking quasineutrality, using Eq. (15) and assuming a single ion and electron population expanding in the semi-infinite space \( x > 0 \). Equation (19) is substituted by the simpler condition \( n_e = Z_i n_i \), the index \( i \) denoting the single ion component. The boundary conditions are that the electron density should remain equal to the background value well inside the plasma, so that \( n_e(-\infty) = n_0 \), and should vanish in vacuum far from the surface, i.e., \( n_e(+\infty) = 0 \). Together with Eqs. (16) and (17), the resulting system admits the classical self-similar solution first found by Gurevich, Pariiskaya, and Pitaevskii (1966),

\[
    n_i = n_0 \exp \left( -\frac{x}{c_s t} \right), \quad u_i = c_s + \frac{x}{t},
\]

where \( x/t \) is the self-similar variable, \( L = n_i/\delta x n_i = c_s t \) is the local density scale length, and the expressions are valid for \( x > -c_s t \). The profiles corresponding to Eqs. (22) are sketched in Fig. 16.

As a consequence of the quasineutral approximation, the physical quantities describing the plasma dynamics present several diverging behaviors, such as the unlimited increase of \( u_i \) with \( x \). This implies that the neutral solution must become invalid at some point, which can be estimated by equating the local density scale length \( L \) to the local Debye length \( \lambda_D \). This provides \( n_f(t) = c_s [2 \ln(\omega_{pi} t) - 1] \), the corresponding velocity \( u_f = dx_f/dt = 2c_s \ln(\omega_{pi} t) \), and the electric field at the ion front \( E_f = E(x_f) = 2E_0/\omega_{pi} t \), where \( E_0 = (4\pi n_0 T_0)^{1/2} \). This estimate gives twice the self-similar field \( E = E_0/e c_s t \). The argument also defines the front of the fastest ions moving at velocity \( u_f \) and thus gives also the high-energy cutoff in the energy spectrum of the ions in this description.

Equations (22) are also singular for \( t \to 0 \), i.e., at the earliest instants of the expansion, when quasineutrality also breaks down. In general, in the sub-ps regime

\[
    \frac{n_i}{c_s t} \ll \frac{n_i}{c_s t} \ll e c_s t \ll T_0
\]

\[
    u_f = \frac{dx_f}{dt} = 2c_s \ln(\omega_{pi} t), \quad E_f = E(x_f) = 2E_0/\omega_{pi} t
\]

\[
    x_f(t) = c_s t \Rightarrow E_f = E_0/c_s t
\]

FIG. 16. Sketch of the density and velocity profiles from the self-similar solution for isothermal plasma expansion; Eq. (22). The front of charge separation at \( x = x_f(t) \) and the rarefaction front at \( x = -c_s t \) are also indicated. The electric field is uniform in the \( -c_s t < x < x_f(t) \) region.
the inertia of ions is important and the assumption of quasi-neutrality must be abandoned. Ultimately, a self-consistent analysis can be developed through numerical simulations (see Sec. III.C.4). Still assuming, for simplicity, that only a single ion population and a single-temperature Boltzmann electron population are present, and \( n_i(t = 0) = n_0 \Theta(-x) \), Eq. (20) can be used to define the initial conditions for the electric field at the time \( t = 0 \) at which the ion acceleration process begins. The following interpolation formulas for the electric field and ion velocity at the ion front:

\[
E(t) \approx \frac{\bar{E}}{\sqrt{\tau^2 + 1}},
\]

\[
u_\parallel(t) \approx 2c_s \ln(\tau + \sqrt{\tau^2 + 1}),
\]

where \( \tau = \omega_{pi} t / \sqrt{2e} \), give the correct behavior at \( t = 0 \) for both the electric field [see Eq. (21)] and the front velocity, and reduce to previous expressions for \( \omega_{pi} \tau \gg 1 \). These formulas fit well numerical calculations by Mora (2003) using a Lagrangian fluid code. Related results of similar studies using fluid and kinetic descriptions can be found in the literature.\(^{12}\)

The major drawback of Eq. (24) is that the maximum velocity of ions, and hence the cutoff energy, diverges logarithmically with time. This is not surprising, being an unavoidable consequence of the isothermal assumption and the chosen boundary conditions: the system has an infinite energy reservoir in the electron fluid and thus it is able to accelerate ions indefinitely. Nevertheless, the simplicity of Eq. (24) has proven to be attractive; thus it has been suggested to insert a phenomenological “maximum acceleration time” \( t_{\text{acc}} \) at which the acceleration should stop. Such a formula has been used in attempts to fit experimental data (Fuchs et al., 2006b).

We return to this point in Sec. III.D. There is no easier way to remove this unphysical behavior from the 1D planar model but to give a constraint of finite energy (per unit surface). In this way, the electron temperature decays in time due to the plasma expansion and to collisional and radiative losses. The electron cooling cooperates with the effects of finite acceleration length and maximum electron energy in the determination of a finite value for the maximum energy gain.

The expansion of plasma slabs (foils) of finite thickness, and hence of finite energy, has been considered analytically and numerically. In these models the electron temperature is taken as a function of time \( T_e = T_e(t) \), determined either by the energy conservation equations (Betti et al., 2005; Mora, 2005) or with \textit{ad hoc} modeling of \( T_e(t) \) (Bychenkov et al., 2004).

Analytical solutions for the plasma expansion can be found in the quasineutral approximation, also for the kinetic Vlasov equation (18), using either the self-similar theory (Dorozhkina and Semenov, 1998) or a renormalized group theoretical approach (Kovalev, Bychenkov, and Tikhonchuk, 2001, 2002). Two-temperature electron distributions have also been considered.\(^{13}\)

3. Multispecies expansion

We now describe the expansion of a two species plasma, in which the dynamics of a heavy ion component (labeled with \( H \) in the following) is considered in addition to light ions (labeled with \( L \)). The most peculiar effect of the presence of two (or more) ion species, for appropriate parameters, is the appearance of spectral peaks, which are of interest as both a strong experimental signature and for application purposes.

The problem of two species expansion was studied by Gurevich, Parisiyska, and Pitaevskii (1973), Bezzerides, Forslund, and Lindman (1978), and Srivastava, Sinha, and Lawande (1988). Here we mostly follow the more recent work of Tikhonchuk et al. (2005), where a simplified description is given based on the ordering assumptions

\[
\alpha = \frac{A_H/Z_H}{A_L/Z_L} \gg 1, \quad N = \frac{Z_H n_H}{Z_L n_L} > \alpha.
\]

These conditions state that the \( H \) species is quite heavier than the \( L \) one, that the concentration of the latter is small, and that the \( L \) ion plasma frequency is higher so that the dynamics of \( L \) ions is faster. These assumptions allow one to assume that, near the rarefaction front, the effect of \( L \) ions is unimportant and that the dynamics of the \( H \) ions can be described as a single species expansion as in Sec. III.C.2, where the relevant parameter is the \( H \) ion sound speed \( c_H = \sqrt{Z_H T_h/A_H m_H} < c_L \), the \( L \) ions sound speed. \( L \) ions are treated as test particles in this region, where they are accelerated by the electric field \( E \propto c_H^{-1} \) [see Eq. (13)], which is thus stronger than what would be created in the expansion of the \( L \) ions alone. The \( L \) ion velocity and density in this region can be obtained using the 1D fluid, self-similar equations with the above given

\(^{12}\)See, e.g., Widner, Alexeff, and Jones (1971), Crow, Auer, and Allen (1975), Pearlman and Morse (1978), Denavit (1979), and Mora (2003) for the case of a single electron population and Bychenkov et al. (2004), Mora (2005), and Tikhonchuk et al. (2005) for the case of two electron components.

electric field (Tikhonchuk et al., 2005), obtaining for the velocity profile
\( v_L \approx c_L \sqrt{2(1 + x/c_H)}^{1/2} \). Noticeably, the \( L \) ions velocity and density profiles vary slowly in space compared to the \( H \) ion ones, and the \( L \) ion flux is almost constant. Beyond the \( H \) ion front, only \( L \) ions are present and they can be described again by a single species expansion with \( v_L \approx c_L + x/t \) [see Eq. (22)]. However, matching of the velocity profiles in the region behind the \( H \) ion front implies the existence of a transition region where the velocity is approximately constant. This corresponds to a plateau region in the phase space and to a peak in the \( L \) ion energy spectrum. The heuristic reason for plateau formation is that the \( L \) ions are accelerated more efficiently behind the \( H \) ion front than ahead of it. Figure 17 shows the velocity spectrum from numerical results (Tikhonchuk et al., 2005) using a Boltzmann-Vlasov-Poisson model (Bychenkov et al., 2004) based on Eqs. (14), (15), and (18), compared with analytical estimates from the self-similar solution.

According to the above model the peak energy of \( L \) ions is

\[ E_L \approx Z_L T_H \ln(4\sqrt{2}\pi A N/e). \]  

(26)

As an important indication from this model, the mass ratio and the relative concentration of the two species might be engineered to optimize the \( L \) ion spectrum. Several simulation studies\(^{14}\) have been devoted to this issue and to the modeling of observations of multispecies spectra in both planar and spherical (droplet) targets (see Sec. III.E).

4. Numerical simulations

Even in their simplest formulation TNSA models are highly nonlinear and the set of available analytical solutions is limited. A numerical approach can be used to overcome these limitations and to address additional effects.

Referring to the 1D problem of plasma expansion, an hydrodynamic two-fluid approach may be used to take charge separation effects into account as reported by Mora (2003). The hydrodynamic model, however, cannot take into account kinetic effects such as non-Maxwell distribution and breakdown of equilibrium conditions. To address these effects a numerical solution of the Vlasov equation for the distribution function of electron and ions in phase space is needed. To this aim the PIC approach (see Sec. II.D) may be used, with the drawback of much larger computational requirements compared to hydrodynamics simulations. The reason is that, in order to obtain full numerical convergence and accurate, low-noise results, a very large number of particles should be used to resolve the strong density variations in the plasma expansion.

In its simplest formulation the 1D simulation of collisionless plasma expansion takes a single ion species into account and a limited set of parameters, such as the initial electron temperature and the initial thickness of the plasma; this is equivalent to fixing the total energy of the system. Such simplified simulations already reproduce qualitative features observed in the experiment and may match measured quantities such as the ion front velocity, with a proper choice of initial parameters. As an example, Fig. 18 shows simulation results performed to support experimental observations by Romagnani et al. (2005), using both a hydrodynamics and a PIC code. The two approaches use different initial conditions, i.e., a Boltzmann equilibrium for fixed ions and a zero charge density distribution, respectively. The latter condition enables one to resolve in the PIC calculation the propagation of the electron front, resulting in the electric field vanishing at the front position and showing a strong temporal maximum at the earliest instants, in agreement with experimental observations.

The use of supercomputers allows one to perform multidimensional PIC simulations and to simulate the laser-plasma interaction and the generation of hot electrons, rather than imposing \textit{a priori} their number and temperature. The computational challenges and limitations of such large-scale simulations have been discussed in Sec. II.D. In addition, most PIC simulations do not include collisions, which may play an important role in the transport of hot electrons through the target (see Sec. II.B.3). Nevertheless, PIC simulations have been vastly used as a valuable support in the interpretation of measurements of ion acceleration and were able to reproduce at least qualitatively several observed features of the TNSA picture; see, e.g., Pukhov (2001), Wilks et al. (2001), and Fuchs et al. (2005).

As an alternative to the PIC method, Gibbon et al. (2004) used a gridless, electrostatic “tree” particle code to simulate ion acceleration from wire targets. Such a code has the advantages of an unlimited spatial region for particles and of “automatic” inclusion of collisions at the cost of being purely electrostatic so that the laser-plasma interaction may be modeled only phenomenologically and magnetic field generation is not included.

D. Comparison between models and experiments

TNSA has been thoroughly investigated in a large number of experiments, performed, in the past decade, in many laser
facilities all over the world. The maximum observed value of the ion energy $E_{\text{max}}$ has probably been the most characterizing parameter of such experiments. Another important feature, mostly in light of potential applications, is the profile of the energy spectrum.

All this effort has resulted in an extensive collection of experimental data, against which the predictive capability of the TNSA theoretical models can be tested. Moreover, a new generation of laser facilities will soon be available, and it will then be possible to investigate a wider range of experimental parameters. Therefore the challenge of satisfactorily predicting the result of a TNSA experiment, providing sufficiently reliable scaling laws to extrapolate guidelines for the future experiments, is even more important.

Experimentally, great effort has been devoted to properly addressing the correlation among the above mentioned ion properties and the main laser and target parameters. Because of the importance of the laser irradiance in establishing the regime of interaction (see Sec. II), in the literature it has become common to report the maximum ion (mainly proton) energy $E_{\text{max}}$ as a function of this parameter (see, e.g., Fig. 4). Collections of experimental data for $E_{\text{max}}$ have been reported in several papers. On the other hand, it is apparent that the irradiance is not the only laser parameter playing a role in determining $E_{\text{max}}$. In particular, it has been established by many experiments that, at fixed irradiance, more energetic pulses lead to higher $E_{\text{max}}$. Moreover, already from the early experiments the strong influence of the laser prepulse level and duration and of the target properties on $E_{\text{max}}$ has been evident. We devote Sec. III.E to a discussion of these topics, while here we point out the general difficulties which can be encountered when attempting to provide predictions of $E_{\text{max}}$ for comparison with experimental data.

For all the models introduced in Sec. III.C, $E_{\text{max}}$ can be evaluated once the required parameters of the physical system are known. This is a very delicate and often controversial issue because the input parameters are different in number, nature, and reliability. Some models use experimental laser and target parameters, which are known or controlled with well-defined precision, such as, e.g., mean irradiance, spot radius, energy and duration of the laser pulse, target thickness and chemical composition, or surface density of impurity protons in the target. Other models use, as input parameters, physical quantities determined by interaction and transport processes. We refer, in particular, to hot electron properties (see Sec. II.B.2) such as conversion efficiency $\eta_h$, temperature $T_h$, density $n_p$, cutoff energy, and beam divergence angle $\theta_{\text{div}}$. These quantities may in principle be modeled and/or measured but most times are not precisely known. Finally, some models include purely phenomenological parameters such as the ion acceleration time $t_{\text{acc}}$ (see Sec. III.C.2) and numerical parameters determined by fitting set of experimental data or numerical simulations. The experimental and theoretical uncertainties and the different nature of the model parameters inevitably impose some limitations to the conclusions that one could draw from a quantitative comparison.

We briefly touch on this problem following the work by Perego et al. (2011). The descriptions which have been selected in this paper are the fluid expansion models proposed by Mora (2003, 2005), the quasistatic approaches of Schreiber et al. (2006) and Passoni and Lontano (2008), and the “hybrid” descriptions by Albright et al. (2006) and Robinson, Bell, and Kingham (2006) (see Sec. III.C). The calculations used to implement these models and evaluate $E_{\text{max}}$ are also summarized. To perform the comparison a database containing an extensive collection of published experimental parameters and results, referring to a wide range of laser and target parameters, has been considered. This analysis shows that, despite all the uncertainties, the predictions of the TNSA models can be considered quite good, and in some cases remarkable, for a wide range of experimental parameters. In particular, quasistatic models, especially the one proposed by Passoni and Lontano (2008), appear more suitable for the prediction of $E_{\text{max}}$. These conclusions are strongly affected by the estimates of the required parameters, and a more realistic approach to evaluate these quantities could improve the predicting capability of both expansion and hybrid models.

The possibility to compare model predictions with experimental parametric studies under well-defined and controlled laser conditions, aimed at providing reliable and clear scaling laws, can significantly enhance the effectiveness of the analysis. Figure 19 shows results from a parametric study of the dependence of $E_{\text{max}}$ on laser power and duration (Zeil et al., 2010). Several other parametric investigations of the dependence of $E_{\text{max}}$ on laser pulse irradiance, duration, energy, and fluence have been reported (Fuchs et al., 2006b; Nayuki et al., 2006; Robson et al., 2007; Flippo, Workman et al., 2008; Flacco et al., 2010) as well as attempts in interpreting part of these findings (Passoni et al., 2009; Passoni, Bertagna, and Zani, 2010a; Zani, Sgattoni, and Passoni, 2011).

![FIG. 19](color online). Experimental scaling of proton energy cutoff with laser power and pulse duration. Squares are data from experiments performed with the DRACO laser at FZD (Dresden), showing a linear scaling with power in the short-pulse (30 fs) regime. Other points are data from other laboratories; see Zeil et al. (2010) for references and details. The fitting lines correspond to the static model by Schreiber et al. (2006) with different colors (labels) corresponding to different values of the pulse duration $\tau_1$ as given in the legend. From Zeil et al., 2010.)
E. Experimental optimization

After the first years of research, the combined vigorous development in both laser technology and advanced target manufacturing allowed the investigation of TNSA exploring a continuously increasing range of laser and target parameters. In most cases the two sets of parameters are intimately related. For example, the use of “extreme” geometrical target properties, such as thicknesses in the submicrometric range, requires the availability of extraordinarily clean, prepulse-free pulses to avoid early target evaporation and deformation. Such pulses can be obtained with recently developed techniques, such as plasma mirrors (Dromey et al., 2004; Fuchs et al., 2006a; Thaury et al., 2007, and references therein), optical parametric amplification (Shah et al., 2009), or crossed polarized wave (XPW) generation (Jullien et al., 2005; Zaouter et al., 2011, and references therein).

1. Energy cutoff enhancement

Mackinnon et al. (2002) studied the dependence of ion acceleration on the target thickness, with the aim of addressing the role played by the electron temporal dynamics and its effect on the formation of the accelerating sheath electric field. The experimental results showed an increase in the peak proton energy from 6.5 to 24 MeV when the thickness of the Al foil target was decreased from 100 to 3 μm. These data clearly indicate that an increase in the target thickness implies a lower mean density of the hot electrons at the surface and a consequent lowering of the peak proton energy.

The influence of the laser prepulse due to amplified spontaneous emission (ASE) on the acceleration of protons in thin-foil experiments has been investigated in detail by Kaluza et al. (2004). In this experiment Al foils of different thickness (from 0.75 to 86 μm) were used in the presence of an ASE prepulse whose duration could be controllably varied. The results indicated an optimal value for the target thickness, strongly depending on the prepulse duration, at which the TNSA process leads to the highest proton energies. For thinner targets, a prepulse-induced plasma formation at the rear side effectively suppressed TNSA, in agreement with the considerations developed in Secs. II.C and III.A. Related experimental work, where a wide range of laser parameters and different target materials have been considered, can be found in the literature (Spencer et al., 2003; Fuchs et al., 2006b).

Effective suppression of the laser prepulse level, that is, the adoption of ultrahigh laser contrast, can significantly alter the physical picture, since ultrathin targets, down to the nm level, can maintain their integrity until the interaction with the main pulse. With these conditions a more effective acceleration process can be expected because the refluxing and concentration of hot electrons in a smaller volume may lead to the establishment of a stronger electric field and, consequently, to higher ion energies. These ideas have been successfully tested by Neely et al. (2006), using Al target with thicknesses as low as 20 nm in combination with 33 fs pulses with ASE intensity contrast reaching 1010. A significant increase of both maximum proton energy and laser-to-proton energy conversion efficiency was found at an optimum thickness of 100 nm.

Similar results have been obtained by Antici et al. (2007) and Ceccotti et al. (2007). As a further interesting feature of this latter experiment, a symmetrical TNSA on both front and rear sides has been demonstrated, as shown in Fig. 20, when a sufficiently high (>1010) laser contrast is used. This result confirms the universality of the TNSA process, which may also occur at the front side (accelerating ions in the backward direction) if the density profile is sharp enough. Recently, using a laser pulse with similar contrast, 40 fs duration, 1021 W cm−2 and irradiating targets of 800 nm thickness, Ogura et al. (2012) reported proton energies up to 40 MeV, the highest value reported so far for pulse energies below 10 J.

Another possible strategy to exploit the effectiveness in the formation of the accelerating field in mass-limited targets is to reduce the lateral dimensions. Numerical investigations (Psikal et al., 2008) have shown that a reduced surface leads to higher densities of hot electrons at the rear side of the target and, thus, to higher accelerating electric fields. Buffechoux et al. (2010) experimentally confirmed these findings showing that in targets having limited transverse extent, down to tens of μm, the laser-generated hot electrons moving with a component of the velocity along the lateral direction can be reflected from the target edges during time scales of the same order of the acceleration of the most energetic ions. This transverse refluxing can result in a hotter, denser, and more homogeneous electron sheath at the target-vacuum interface. A significant increase in the maximum proton energy (up to threefold), as well as increased laser-to-ion conversion efficiency, can be obtained with these conditions, as shown in Fig. 21. Similar results,
obtained with different laser and target parameters, have been found by Tresca et al. (2011), who also measured an increase in the maximum energy of protons accelerated from the edges of the target with decreasing target area.

Several other attempts have been made to increase the energy density of the hot electrons in the sheath and, consequently, the maximum proton energy. Following from the indications of Kalaza et al. (2004), McKenna et al. (2008) investigated whether there exists an optimum density profile at the front of the target which maximizes the laser absorption. The proton cutoff energy was increased by 25% with respect to a sharp interface case at “intermediate” plasma scale length (tens of μm). Under such conditions, the higher conversion efficiency into fast electrons was attributed to self-focusing of the driver pulse. Other studies of controlled prepulse effects on ion acceleration have been reported by Flacco et al. (2008) and Batani et al. (2010).

Recently, an energy cutoff increase up to 67.5 MeV, 35% higher than for comparator flat foil shots, was demonstrated by Gaillard et al. (2011) using specially devised targets, namely, flattop hollow microcones (Flippo et al., 2008), which are a modification of conical targets used in fast ignition experiments (see Sec. V.C). The laser pulse is focused inside the target and starts interacting with the walls of the cone that it grazes while focusing down toward the flattop section. The reported result, obtained with 80 J of laser energy on the Trident laser at Los Alamos National Laboratory (LANL), is attributed to an efficient mechanism of electron acceleration taking place on the inner cone walls, named “direct laser-light-pressure acceleration.” The resulting increase in the number of high-energy electrons results in the increase of the maximum proton energy.

The use of targets with various structures has also been investigated with the particular aim to increase the ion energy already at relatively low laser intensities (below $10^{18} \text{ W cm}^{-2}$), using, e.g., double layer targets (Badziak et al., 2001) and more recently nanowire-covered targets (Zigler et al., 2011) for which surprisingly high energies up to 5.5–7.5 MeV for a $5 \times 10^{17} \text{ W cm}^{-2}$, 40 fs laser pulse were reported.

2. Source spectrum manipulation

Various approaches have been proposed in order to manipulate the spectrum of TNSA protons and ions, in most cases with the intent of obtaining narrow-band peaks, in other cases with the aim to enhance proton numbers throughout the whole spectrum or in some spectral bands as required by specific applications. We first review a number of approaches in which the proton spectrum is modified at the source, leaving approaches which act on the proton beam after the initial acceleration to Sec. III.E.3.

Spectral peaks can appear as a consequence of multispecies plasma expansion (see Sec. III.C.3). This effect has been invoked to explain observations in proton beams from thin foils, where the peaks appear as modulation of a continuum exponential spectral (Allen et al., 2003) and in experiments employing droplets of heavy water, where peaks are observed in the deuterium spectrum (Ter-Avetisyan et al., 2006).

Spectral peaks have been observed in experiments employing high-Z metallic targets where a plastic layer [0.5 μm poly-methyl methacrylate (PMMA)] was coated as a dot on the rear surface of a 5 μm Ti foil (Schwoerer et al., 2006; Pfotenhauer et al., 2008). These results, obtained on the 10 TW JETI laser in Jena, were explained on the basis of the proton depletion approach first suggested by Esirkepov et al. (2002). Robinson and Gibbon (2007) suggested instead that the proton density in the multispecies plastic layer is the important factor in determining the appearance of the spectral peak. Experimental implementation required the removal of the native contaminant layer present at the surface and resulted in peaks in the proton spectra at ~2 MeV, with ~10% spread and good reproducibility (Pfotenhauer et al., 2008).

Another experiment also relied on the (partial) removal of hydrogen contaminants from the surface of a palladium target (Hegelich et al., 2006) so that protons did not appear in the spectrum. Instead, monoenergetic features appeared

FIG. 21 (color online). Experimentally observed (a) cutoff proton energies and (b) conversion efficiency (for $>1.5 \text{ MeV}$ protons) for 2 μm thick Au targets as a function of surface area, evidencing the effect of electron refluxing. The laser pulse had 400 fs duration, $2 \times 10^{19} \text{ W cm}^{-2}$ intensity, 45° incidence, and $P$ polarization. From Buffechoux et al., 2010.

FIG. 22 (color online). Ion spectra from preheated Pd substrate targets from which hydrogen contaminants have been removed (Hegelich et al., 2006). Black curve: spectrum of $C^{5+}$ ions. Blue curve: spectrum of the dominant substrate charge state $Pd^{22+}$. Green and red curves: simulated $C^{5+}$ and $Pd^{21+}$ spectra. Gray curve: spectrum of dominant $C^{4+}$ ions from a heated W target. Magenta curve: $C^{5+}$ signal from a cold Pd target. In the cases of black and blue curves, an ultrathin layer of graphite is present on the target surface, and a quasimonoenergetic spectrum appears. In the last two cases (gray and magenta curves) the targets have a thick layer of carbon contaminants and do not form a monolayer source, resulting in exponential-like spectra. From Hegelich et al., 2006.
3. Staged acceleration and beam control

Staged acceleration employing two laser pulses on two separate targets has also been investigated as a possible route to spectral manipulation of laser-driven ion beams. This idea relies on accelerating a TNSA beam from a first target and direct it through a second foil, which is irradiated by a second laser pulse at the time that a particular group of TNSA protons crosses the foil. These protons should thus experience an accelerating field as they transit through the rear surface of the second foil and gain additional energy. An experiment by Pfotenhauer et al. (2010), also carried out on the JETI laser, tested this idea. Peaks and dips in the spectrum were observed at energies of ~1 MeV which correlated well with the time of flight of protons reaching the second target as it is irradiated, showing that the field on the second target slightly boosts protons in a given energy range resulting in the spectral modification. Burza et al. (2011) reported a two-stage approach employing spherical shell targets, irradiated by a single laser pulse, in which protons accelerated by TNSA at the front of the shell experience a second accelerating field while they transit through the opposite side of the shell, which modifies the high-energy end of the spectrum. The field is due to a hot electron charge wave spreading along the target surface from the interaction point, as reported in several experiments (Toncian et al., 2006; McKenna et al., 2007; Quinn et al., 2009a).

A different type of two-stage approach was tested by Markey et al. (2010) on the VULCAN laser. Two pulses of sub-ps duration were sequentially focused, with controllable delay, on the same target in order to modify the temporal history of the hot electron source driving the TNSA, as suggested originally by Robinson et al. (2007). An optimal delay was seen to result in an increase of energy and conversion efficiency and, additionally, a modification of the slope of the spectral profile. In this case, besides an optimization of hot electron production by the main pulse in a front surface plasma gradient, similar to Kaluza et al. (2004) and McKenna et al. (2008), they suggest that an additional modification of the proton spectrum arises from the fact that proton acceleration by the main pulse takes place in an already expanding multispecies, plasma sheath at the target rear surface. Under these conditions, the electrostatic field peaks at the front separating protons from heavier species, and reaccelerates mainly the lower energy part of the spectrum. Similarly, in a recent experiment, Dollar et al. (2011) obtained spectral modifications, resulting in the appearance of narrow-band spectral peaks at ~2–3 MeV energies, by focusing a prepulse (10^{-5} of the 10^{21} W cm^{-2} peak intensity) on ultrathin foils a few tens of ps before the peak of the main pulse.

A staged technique which acts on the protons after the acceleration, but employing all-optical means, was demonstrated by Toncian et al. (2006, 2011). A transient electric field is excited at the inner surface of a metal cylinder (having ~mm diameter and length) irradiated on the outer surface by a high-intensity laser pulse while a laser-driven proton beam transits through it; see Figs. 23(a)–23(c). The field acts on the protons by modifying their divergence leading to a narrow, collimated beamlet. As the field is transient, typically lasting for ~10 ps, it affects only the proton component transiting through the cylinder within this time window, i.e., within a narrow energy band, leading to a spike in the energy spectrum, as visible in Fig. 23(f), showing a 0.2 MeV band at ~6 MeV. Further experiments have shown that the position of the spectral peak can be controlled by varying the delay between the two laser pulses (Toncian et al., 2011) and confirmed that the focusing is chromatic, i.e., the focal position varies with proton energy.

A similar approach, but employing a single pulse, was developed by Kar et al. (2008b) for reducing the proton beam divergence. Also conceptually similar to the approach described above by Burza et al. (2011), the scheme employs specially designed targets in which a thin foil is inserted in a thicker frame, so that the charge wave expanding outward from the acceleration region at the rear of the foil generates on the frames surface an electric field transverse to the expanding beam, which partially constrains its natural divergence.

Other proposed methods of optical control of proton beam properties include beam steering triggered by shock waves
locally deforming the target surface (Lindau et al., 2005; Lundh et al., 2007), an effect also reported by Zeil et al. (2010), and control of the beam homogeneity and cross section profile by focusing an annular beam around the high-intensity interaction region, which modifies the properties of hot electrons refluxing through the target (Carroll et al., 2007).

The high degree of beam laminarity, and the fact that ion emission is substantially normal to the target surface, led early on to the suggestion that by appropriately shaping the surface it should be possible to ballistically focus down the protons to a tight spot (Ruhl et al., 2001; Wilks et al., 2001), ideally recovering the properties of the virtual source. The idea is consistent with (and complementary to) observations of TNSA ions from wire targets, where the curvature of the target leads to a highly diverging beam ion with the form of an expanding disk (Beg et al., 2004). An indirect experimental demonstration of focusing was obtained via enhanced, localized heating of a secondary target, as discussed in Sec. V.B (Patel et al., 2003; Snavely et al., 2007). Recently, a more direct demonstration of proton beam focusing was obtained by mesh projection methods in experiments where, employing targets with hemicylindrical (Kar et al., 2011) or hemispherical shape (Bartal et al., 2012), beam focusing (down to 20–25 μm spots) over the whole spectrum (up to 25 MeV) was demonstrated. The data highlighted the achromatic nature of the focusing at the different energies, consistent with the energy dependent variations in divergence from a planar foil.

Several groups implemented conventional accelerator techniques for energy selection or transport of laser-accelerated protons, in view of possible downstream applications of the proton beam (see Sec. V). Besides simple energy selection with bending magnets, the range of options explored includes the use of pairs of quadrupole magnets for refocusing protons at distances in the 5–60 cm range and in ~100 μm spots (Schollmeier et al., 2008; Nishiuchi et al., 2009) or to collimate (Ter-Avetisyan et al., 2008) protons within a given spectral band up to 14 MeV as found by Schollmeier et al. (2008). A crucial parameter in this approach is the acceptance angle of the quadrupole system, which may limit the number of particles that can be focused. Large acceptance pulsed solenoids (~9 T) were also used (Roth et al., 2009; Harres et al., 2010) for collimation and transport of a large number of ~10^15 particles.

The use of synchronous rf fields for phase rotation resulted in the appearance of multiple peaks across a broadband spectrum (Ikegami et al., 2009). Although demonstrated only at relatively low energy and over low-energy bands, this technique is in principle interesting as, rather than “slicing” a portion of the spectrum, which is effectively what is done in several of the methods above, it can concentrate in a narrow spectral band protons originally contained within a larger spectral region. The phase rotation can be accompanied under the right conditions by a collimation effect.

Some of these techniques have already been implemented sequentially in test beam lines operating at 1 Hz repetition (Nishiuchi et al., 2010a) with a view to future biomedical applications (see Sec. V.D).

IV. OTHER ACCELERATION MECHANISMS

A. Radiation pressure acceleration

EM waves carry momentum, which may be delivered to a nontransparent (either absorbing or reflecting) medium. This is the origin of radiation pressure whose expression for a plane, monochromatic EM wave of intensity I and frequency ω normally incident on the plane surface of a medium at rest, is given by

\[ P_{rad} = (1 + R - T) \frac{I}{c} = (2R + A) \frac{I}{c}, \]

(27)

where R, T, and A are the reflection, transmission, and absorption coefficients (with R + T + A = 1) defined as a function of the refractive index and thus of the wave frequency, e.g., as done in the derivation of Fresnel formulas (Jackson, 1998). Radiation pressure is related to the total steady PF on the medium (see Secs. II.A and II.B.1). Being proportional to the inverse of the particle mass, the PF effectively acts on the electrons. At the surface of an overdense plasma the electrons are pushed inward by the PF, leaving a charge separation layer and creating an electrostatic, backholding field that in turn acts on the ions and leads to their acceleration.

In the case of normal incidence of a plane wave on a flat surface the PF density is the cycle-averaged value of the \( \mathbf{J} \times \mathbf{B} \) force. In the following discussion of RPA we refer to such a case unless otherwise stated and consider only the steady action of radiation pressure. As discussed in Sec. II.B.1, the oscillating component of the \( \mathbf{J} \times \mathbf{B} \) force drives a sweeping oscillation at 2ω of the density profile and causes strong absorption and hot electron generation, except in the case of circular polarization for which the oscillating component vanishes. In the latter case, on the time scale of ion motion it may be assumed that the electrons are mostly in a mechanical equilibrium so that the PF and electrostatic force locally balance each other.

1. Thick targets: Hole boring regime

The intense radiation pressure of the laser pulse pushes the surface of an overdense plasma inward, steepening the density profile. For a realistic laser beam of finite width, the radiation pressure action drives a parabolic deformation of the plasma surface allowing the laser pulse to penetrate deeply into the target; this process is commonly named hole boring, even when referring to a planar geometry, and it is associated with ion acceleration at the front side of the target. Note that in the literature different definitions, such as “sweeping acceleration” (Sentoku et al., 2003) or “laser piston” (Schlegel et al., 2009), are also used to refer to essentially the same process.

The recession velocity of the plasma surface, also named the HB velocity \( v_{HB} \), may be simply estimated by balancing the EM and mass momentum flows in a planar geometry (Denavit, 1992; Wilks et al., 1992; Robinson, Gibbon, Zepf et al., 2009; 16

16The electromagnetic theory of radiation pressure is due to James Clerk Maxwell (1873). It is, however, interesting that the Italian physicist Adolfo Bartoli (1884) also independently obtained Maxwell’s result in 1875 from thermodynamic considerations.
Schlegel et al., 2009). In the instantaneous frame where the surface is at rest we observe incoming ions with density $n_i\gamma_{\text{HB}}$ and velocity $-v_{\text{HB}}$ bouncing back at the surface. The EM momentum flow, i.e., the radiation pressure, must then balance a momentum flow difference equal to $n_i\gamma_{\text{HB}}(2n_i\gamma_{\text{HB}}v_{\text{HB}})\nu_{\text{HB}}$ with $\gamma_{\text{HB}} = (1 - v_{\text{HB}}^2/c^2)^{-1/2}$. In this reference frame, the radiation pressure is $P_{\text{rad}} = (2I/c)(1 - v_{\text{HB}}/c)/(1 + v_{\text{HB}}/c)$ as demonstrated by a Lorentz transformation. The global momentum balance thus gives

$$
\frac{2I}{c} \frac{1 - v_{\text{HB}}/c}{1 + v_{\text{HB}}/c} = n_i\gamma_{\text{HB}}(2n_i\gamma_{\text{HB}}v_{\text{HB}})\nu_{\text{HB}}.
$$

(28)

Solving for $v_{\text{HB}}$ yields

$$
v_{\text{HB}} = \frac{\Pi^{1/2}}{1 + 2\Pi^{1/2}}, \quad \Pi = \frac{I}{m_i n_i c^3} = \frac{Z n_e m_e}{\lambda n_p m_p} a_0^2.
$$

(29)

The fastest ions are those bouncing back from the surface in the moving frame, resulting in a maximum energy per nucleon in the laboratory frame

$$
E_{\text{max}} = 2m_pc^2 \frac{\Pi}{1 + 2\Pi^{1/2}}.
$$

(30)

In the nonrelativistic regime where $\Pi \ll 1$ and $v_{\text{HB}} \ll c$, we obtain $v_{\text{HB}}/c = \Pi^{1/2}$ and $E_{\text{max}} \approx 2m_pc^2\Pi$. Essentially the same results are obtained with a dynamical model of ion acceleration in the charge separation region at the surface (Macchi et al., 2005). Such model and related PIC simulations show that the ions pile up at the end of the skin layer producing a sharp density spike and causing hydrodynamical breaking and collapse of the electron equilibrium. This process leads to the production of a narrow bunch of fast ions at the velocity $2v_{\text{HB}}$ which penetrates into the plasma bulk. Eventually the quasiequilibrium condition is established again and the process repeats itself as long as the laser pulse is on. HB acceleration is thus of pulsed nature, although on the average it may be described by a steady model (Schlegel et al., 2009).

Equation (30) indicates that with present-day intensities high energies may be obtained via HB acceleration if the density can be reduced to be slightly above $n_i$, which is possible if a gas jet target and a long wavelength laser, i.e., CO$_2$, is used. This scheme would be interesting for applications since it allows control of the background density, the use of a pure proton target, and high-repetition rate since the gas is flowing. In a recent experiment (Palmer et al., 2011) employing 10 $\mu$m wavelength, $\sim 6 \times 10^{15}$ W cm$^{-2}$ circularly polarized pulses ($\omega_0 \approx 0.5$), and a hydrogen gas jet with density of a few times $n_e$, protons of energy up to 1.2 MeV and a narrow energy spread were observed (see Fig. 24). The observed ion energies were fairly consistent with a linear scaling with $I/n_e$ as predicted by the HB model. The energies were actually higher than expected considering the vacuum laser intensity, suggesting that self-focusing in the underdense region could have increased the intensity in the plasma.

We note that Palmer et al. (2011) reported on protons accelerated by a shock driven by radiation pressure, similarly to several who refer to HB or piston acceleration in thick targets as acceleration in the electrostatic shock sustained by the laser pressure at the front surface (Zhang, Shen, Yu et al., 2007; Schlegel et al., 2009; Zhang et al., 2009). In the context of ion acceleration by a laser, we prefer to reserve the term “shock” for the regime described in Sec. IV.B which implies the generation of a true electrostatic shock wave, able to propagate into the plasma bulk and drive ion acceleration there. From the point of view of fluid theory, a shock wave launched with velocity $v_{\text{sho}}$ requires the sound speed, and thus the electron temperature, to be large enough to prevent the Mach number $M = v_{\text{sho}}/c_s$ from exceeding the critical value $M_{\text{cr}} = 6.5$ above which one does not have a shock but a “pure piston” (Forslund and Freidberg, 1971). Thus, formation of a true, high speed shock wave may be inhibited for circular polarization because of the reduced electron heating.

Experimental evidence of HB acceleration in solid targets is less clear at present. Badziak et al. (2004) reported a series of observations of high-density, $\sim$keV ion energy pulses (plasma “blocks”) for subrelativistic irradiation ($<10^{18}$ W cm$^{-2}$) of solid targets (but in the presence of significant preplasma). These results were interpreted using a model of ponderomotive skin-layer acceleration at the critical surface, a concept that sounds rather similar to HB-RPA. Akli et al. (2008) reported on heating of solid-density matter due to laser-driven density profile sweeping.

![FIG. 24 (color online). Hole boring acceleration by a CO$_2$ laser pulse in a gas jet. The left frame shows ion spectra for various values of the intensity $I_{15}$ (in units of 10$^{15}$ W cm$^{-2}$) and the electron density $n = n_i/n_e$: (a) $I_{15} = 6.4$, $n = 6.1$; (b) $I_{15} = 5.5$, $n = 6.1$; (c) $I_{15} = 5.9$, $n = 7.6$; (d) $I_{15} = 5.7$, $n = 8.0$. The right frame shows the observed scaling of ion energies with the ratio $4I/n_e$. From Palmer et al., 2011.](image)
and shock formation at intensities up to $5 \times 10^{20} \text{ W cm}^{-2}$, and Henig et al. (2009a) reported on ion acceleration by a converging shock in spherical targets irradiated at $1 \times 10^{20} \text{ W cm}^{-2}$. For both these experiments, the analysis of data and supporting PIC seems also compatible with HB-RPA occurring at the front surface, although the electron heating due to the use of linear polarization complicates the picture. Indications of strong radiation pressure effects were also obtained from the modeling of collimated, high-density plasma jets at the rear side of targets with a few micron thickness, at intensities up to $2 \times 10^{20} \text{ W cm}^{-2}$ (Kar et al., 2008a). It should be noted that, although the scaling of Marx (1966) used calculations based on the simple model of a spacecraft propulsion (Forward, 1984). To support this idea the LS concept, including visionary ones such as laser-driven plasma anymore.

The thin target regime of RPA has been named light sail regime. As discussed above, hole boring RPA applies to a “thick” target, i.e., much thicker than the skin layer in which ion acceleration by the space-charge field occurs. The laser pulse penetrates into the target by pushing adjacent surface layers via a repeated cycle of ion bunch acceleration. The situation changes when a target is thin enough that all the ions are accelerated before the end of the laser pulse, i.e., a complete hole boring occurs. In such a case, the laser pulse is able to further accelerate ions to higher energies since the ions are not screened by a background plasma anymore.

The thin target regime of RPA has been named light sail as the term is appropriate to refer to a thin object of finite inertia, having large surface and low mass, so that it can receive a significant boost from radiation pressure. The invention of the laser soon stimulated possible applications of the LS concept, including visionary ones such as laser-driven spacecraft propulsion (Forward, 1984). To support this idea Marx (1966) used calculations based on the simple model of a flat, perfect mirror boosted by a plane wave. The analytical solution and scaling laws provided by such basic model (Simmons and McInnes, 1993) are useful to illustrate the most appealing features of LS-RPA, such as high conversion efficiency in the relativistic limit and the possibility to reach very high energies with foreseeable laser and target technology.

The equation of motion for a moving target (sail) in the laboratory frame can be obtained with the help of a Lorentz transformation, similarly to Eq. (28). Neglecting absorption for simplicity ($A = 0$) we obtain

$$\frac{d}{dt}(\beta \gamma) = \frac{2I_{\text{ret}}}{\sigma c^2} R(\omega') \frac{1 - \beta}{1 + \beta}, \quad \frac{dX}{dt} = \beta c,$$

(31)

where $X$ is the position of the sail, $\beta = V/c$ is its velocity in units of $c$, $\gamma = (1 - \beta^2)^{-1/2}$, $\sigma = m n s \ell'$ is the mass density per unit surface, and $\omega' = \omega(1 - \beta)/(1 + \beta)^{1/2}$ is the EM wave (laser) frequency in the rest (sail) frame. Note the intensity $I$ is in general a function of the retarded time $t_{\text{ret}} = t - X/c$.

Analytical solutions to Eqs. (31) exist depending on suitable expressions for $R(\omega)$, the simplest case being that of a perfectly reflecting mirror ($R = 1$) and a pulse of constant intensity $I$ (Simmons and McInnes, 1993). The $\gamma$ factor as a function of time is given by

$$\gamma(t) = \sinh(u) + \frac{1}{4\sinh(u)} \quad u = \frac{1}{3} \text{asinh}(3\Omega t + 2),$$

(32)

where $\Omega = (Z m_e q_0^2 / A m_p) \omega$ and $\xi$ has been defined in Eq. (32). Asymptotically, $\gamma(t) = (3\Omega t)^{1/3}$ [see Fig. 25(a)].

The most significant quantities can be obtained for an arbitrary pulse shape $I(t)$ as a function of the dimensionless pulse fluence $F$ (the pulse energy per unit surface):

$$F(t_{\text{ret}}) = \frac{2}{\sigma c^2} \int_0^{t_{\text{ret}}} I(t') dt'.$$

(33)

The sail velocity $\beta$, the corresponding energy per nucleon $E = m c^2 (\gamma - 1)$, and the instantaneous efficiency $\eta$ (i.e., the ratio between the mechanical energy delivered to the sail and the incident pulse energy) are given by

$$\beta(t_{\text{ret}}) = \frac{1 + 2F(t_{\text{ret}})}{1 + F(t_{\text{ret}})},$$

(34)

$$E(t_{\text{ret}}) = \frac{m c^2 F^2(t_{\text{ret}})}{2[F(t_{\text{ret}}) + 1]},$$

(35)

$$\eta(t_{\text{ret}}) = \frac{2\beta(t_{\text{ret}})}{1 + \beta(t_{\text{ret}})} = 1 - \frac{1}{F(t_{\text{ret}}) + 1}.$$

(36)

Thus, $\eta \to 1$ when $\beta(t_{\text{ret}}) \to 1$. The final energy per nucleon $E_{\text{max}}$ is obtained from the total fluence $F_{\infty} = F(t_{\text{ret}} = \infty)$. For a constant intensity $I = \Omega \tau_p$, where $\tau_p$ is the duration of the laser pulse. In practical units $F_{\infty} = 2.2 F_{\text{ret}} \rho_1^{-1} \ell_{10}^{-1}$, where $F_{\text{ret}}$ is the fluence in units of $10^8 \text{ J cm}^{-2}$, $\rho_1 = m_{n_1}/1 \text{ g cm}^{-3}$, and $\ell_{10} = \ell/10 \text{ nm}$. The scalings for $E_{\text{max}}$ are summarized in Fig. 25(b). With present-day or near-term laser technology, fluence values of $10^9 \text{ J cm}^{-2}$ seem affordable, while target manufacturing can produce films of a few nm thickness, e.g., diamondlike carbon (DLC) foils. These values yield $F_{\infty} > 1$ allowing one to approach a regime of high efficiency, relativistic ions, and favorable scaling with the pulse energy.

The above estimates have been obtained assuming a perfectly reflecting sail ($R = 1$) that, for a given surface density parameter $\xi$, limits the laser amplitude to $a_0 < \xi$ due to the onset of relativistic transparency [Eq. (5)] that reduces the boost on the foil. This effect suggests $a_0 = \xi$ as an “optimal” condition for LS acceleration (Macchi, Veghini, and Pegoraro, 2009; Tripathi et al., 2009) which might be,

---

20 For a constant intensity $I$, Eqs. (31) are identical to those for a charge accelerating during Thomson scattering from a plane wave; see Landau and Lifshitz (1962) who leave the solution as an exercise for the reader.

21 The expression for $\eta$ also follows from “photon number” conservation and frequency downshift (see Sec. IV.A.1). In the reflection of $N$ photons from the mirror, the energy transferred to the mirror is $N h(\omega - \omega_0) = [2\beta(1 + \beta)] N h\omega_0 = \eta(N h\omega_0)$.

22 Some give a similar condition for the optimal thickness but with slightly different numerical factors (Yan et al., 2008, 2009a; Ji et al., 2009).
The interest in the LS regime was greatly stimulated by three-dimensional PIC simulations of thin-foil acceleration by Esirkepov et al. (2004) which showed that the temporal dependence and typical values of the ion energy were well described by the LS model. The simulations assumed a laser pulse with peak amplitude \( a_\omega \approx 316 \) (\( \lambda^2 = 1.4 \times 10^{20} \) W cm\(^{-2} \)) and 8 cycles duration, and a proton slab of density 49\( n_c \) and 1\( \lambda \) thickness. Most of the ions in a thin-foil target are accelerated coherently up to relativistic energies (\( \sim 1.5 \) GeV) as shown in Fig. 26. According to Esirkepov et al. (2004), in order for RPA to become the dominant acceleration mechanism the ions have to acquire relativistic energies already within one laser cycle, so that they can promptly follow electrons which are displaced in the longitudinal direction by the ponderomotive force. Later theoretical studies of such a so-called radiation pressure dominant regime (RPD) regime include Rayleigh-Taylor-like instability of the foil (Pegoraro and Bulanov, 2007) and the effects of radiation friction which play a significant role at ultrarelativistic intensities (Tamburini et al., 2010). Of particular interest is the possibility of a self-regulated regime where the transverse expansion of the foil decreases the density along the axis [while the frequency downshift in the foil frame compensates the effect of decreasing \( \xi \) on \( R(\omega') \)] allowing for an increase of the ion energy at the expense of the total number of accelerated ions (Bulanov et al., 2010a, 2010b). For a 3D expansion, theory predicts an asymptotic scaling with time of kinetic energy \( K(t)/mc^2 \approx (3\Omega t)^{2/3} \) that is more favorable than for plane acceleration. This effect has recently been confirmed by 3D simulations (Tamburini et al., 2012) showing a higher peak energy than found in lower dimensionality simulations.

![FIG. 25 (color online).](image1)

(a) Energy per nucleon vs time from the analytical solution [Eq. (32)] of the LS model with \( R = 1 \). The dashed line gives the asymptotic \( \sim t^{1/3} \) behavior. (b) Scaling of the energy per nucleon as a function of the dimensionless pulse fluence \( a_0^2\tau \) (where \( \tau \) is the pulse duration in units of the laser period) and of the surface density \( \xi \) [Eq. (5)] for \( \xi = 1 \) (black line), 3.16 (green line), 10 (blue line), 31.6 (orange line) and 100 (red line). The values on the upper horizontal axis give the fluence in J cm\(^{-2} \) corresponding to \( a_0^2\tau \) for \( \lambda = 0.8 \) \( \mu \)m.

The ultrahigh intensities needed for RPD acceleration are still above present-day laser technology. However, after the proposal of Esirkepov et al. (2004) it was realized that exploring the concept using pulses with circular polarization (CP) at normal laser incidence would enable an investigation of a RPD regime at lower intensities as theoretically discussed by Macchi et al. (2005) in thick targets. Three papers (Zhang, Shen, Li et al., 2007; Klimo et al., 2008; Robinson et al., 2008) independently showed that the use of CP allowed an optimal coupling with an ultrathin foil target as well as rather monoenergetic spectra. Much theoretical work has been devoted to LS-RPA with CP pulses, unfolding a dynamics that is much richer than what is included in the simple “accelerating mirror” model. In particular, formation of a monoenergetic ion distribution is not straightforward (Eliasson et al., 2009; Macchi, Veghini, and Pegoraro, 2009; Macchi et al., 2010) and may require one to control and engineer both the pulse and target properties (Qiao et al., 2009, 2010; T.-P. Yu et al., 2010; Grech et al., 2011).

![FIG. 26 (color online).](image2)

Three-dimensional simulations of thin-foil acceleration in the radiation pressure dominant regime (see text for parameters). Top: Snapshots at \( t = 40 \) T of ion density isosurface and Poynting vector in the \( y = 0 \) plane. Bottom: The maximum ion kinetic energy vs time and the ion phase-space projection \( x, p_x \) at \( t = 80 \) T. The solid line corresponds to the analytical calculation according to the LS model. From Esirkepov et al., 2004.

Several multidimensional simulation studies suggested using flattop transverse profiles to keep a quasi-1D geometry (Klimo et al., 2008; Liseykina et al., 2008; Robinson et al., 2008; Qiao et al., 2009) in order to avoid target deformation that would favor electron heating, to prevent early pulse breakthrough due to transverse expansion, and to keep a monoenergetic spectrum against the inhomogeneous distribution of the laser intensity; to address this last issue, a target...
FIG. 27 (color online). (a) Three typical narrow-band spectra for $Z/A = 1/2$ impurity ions observed from thin (0.1 $\mu$m) metallic targets [for parameters of shots 1–3, see the explanation in (b)]. (b) Peak energies for both ions with $Z/A = 1/2$ (filled squares) and protons with $Z/A = 1$ (empty squares) for seven shots with different polarization parameters [see, e.g., Eq. (11)]: $c_0 = 0$ (LP), 0.47 (EP), and 0.88 (CP). The peak energy is plotted as a function of the parameter $a_0^2t_p/\xi$, which corresponds to $(m_p/2m)\Omega t_p$ in our notations. The parameter set $[a_0, \text{target material, thickness (}$\mu$m), polarization] for the data points 17 is [15.5, Cu, 0.1, LP], [10, Cu, 0.05, CP], [13.8, Cu, 0.1, EP], [7.5, Al, 0.1, LP], [6.9, Al, 0.1, EP], [13.6, Al, 0.5, CP], and [14.1, Al, 0.8, LP].

Recent simulation studies characterized regimes of efficient LS-RPA for linearly polarized pulses at irradiances $\sim 10^{21}$ W cm$^{-2}$ [Dover and Najmudin, 2012; Qiao et al., 2012]. Possible indications of the onset of the LS regime have recently been provided in an experiment performed using 800 fs, 3 $\times$ 10$^{20}$ W cm$^{-2}$ high-contrast (10$^9$) pulses from the VULCAN laser and very thin ($\sim 0.1$ $\mu$m) metallic targets [Kar et al., 2012]. Narrow-band spectra with peak energies up to $\sim 10$ MeV/nucleon were observed for both proton and heavier $Z/A = 1/2$ ions present as surface impurities [see Fig. 27(a)], while heavier bulk ions had a broad spectrum at lower energies. The peak energies scaled with the fluence parameter as $\sim F_{\infty}^{2/3}a_0^2t_p/\xi$ [see Fig. 27(b)], in agreement with Eq. (35) for nonrelativistic ions, and differently from scalings as $a_0^2t_p$ or $a_0^2t_p^2$ which have been inferred for TNSA or for other mechanisms effective for ultrathin targets (see Sec. IV.C). The $Z/A = 1$ peaks are at slightly higher energy than the $Z/A = 1/2$ ones, suggesting that the LS stage is accompanied by a multispecies expansion (see Sec. III.C.5) in the sheath field where protons gain additional energy and the spectral peak separation may be further enforced.

The scaling plot in Fig. 27(b) also contains data from Henig et al. (2009c) who investigated LS using 45 fs, CP pulses at ultrahigh contrast ($\sim 10^{11}$) and $\sim 5 \times 10^{19}$ W cm$^{-2}$ intensity, and few-nm DLC foils. Experimental spectra of fully ionized C$^{6+}$ ions show a difference between linearly and circularly polarized pulses, with a broad peak at $\approx 30$ MeV appearing in the latter case, and reduced electron heating for CP. More recent experimental data by Dollar et al. (2012) using tightly focused ($f/1$) pulses with intensity up to $2 \times 10^{21}$ W cm$^{-2}$ showed a weak difference between CP and linear polarization (LP), which was attributed to the early deformation of the thin targets causing excessive electron heating. Recently, preliminary indications of a transverse instability resulting in spatial modulations of the accelerated proton beam have been reported (Palmer et al., 2012).

To summarize the experimental evidence, to date there is a confirmation of the expected LS scaling, but also indications of significant detrimental effects. The observed ion spectrum is relatively broad, suggesting that transverse inhomogeneity and heating effects need to be reduced. In perspective, the relatively slow growth of the ion energy with time (see Fig. 25) might pose the challenge to increase the acceleration length against the effect of, e.g., pulse diffraction and instabilities.

B. Collisionless shock acceleration

Acceleration of particles by shock waves (briefly, shocks) in plasmas is a problem of great interest in astrophysics (Martins et al., 2009). The existence of an ion component that is reflected by the shock front is actually integral to the formation of the collisionless, electrostatic shock waves in basic fluid theory, where the electrons are assumed to be in a Boltzmann equilibrium (Forlund and Shonk, 1970; Forslund and Freidberg, 1971; Tidman and Krall, 1971). In the frame moving at the shock velocity, ions are reflected by the shock if the height of the electrostatic potential barrier $\Phi_{\text{max}}$ at the front is such that Ze$\Phi_{\text{max}} > m_i v_i^2/2$, with $v_i$ the velocity of the ion component in the shock frame. Behind the shock front, the fields have an oscillatory behavior. Reflected ions initially at rest acquire a velocity in the laboratory frame equal to $2v_{\text{sho}}$, where $v_{\text{sho}}$ is the shock front velocity.

CSA was proposed as an ion acceleration mechanism in superintense laser interaction with an overdense plasma on the basis of PIC simulations by Denavit (1992) and Silva et al. (2004). In the latter work simulations showed the generation of shocks with high Mach numbers $M = v_{\text{sho}}/c_s = 2–3$, where the sound speed is estimated using the hot electron energy as the temperature, i.e., $T_e \approx E_p$ [Eq. (6)]. The shocks are generated at the front surface with a velocity close to $v_{\text{HB}}$ given by Eq. (29), consistently with the assumption that they are driven by the piston action of radiation pressure. By estimating $v_{\text{sho}} \approx v_{\text{HB}}$, in the


$24$ In experiments on underdense plasmas created either by using gas jet targets (Wei et al., 2004) or by the effect of long prepluses in solid targets (Habara et al., 2004b), the observation of ion acceleration along the radial direction has been attributed to radial shock generation in a laser-driven channel.

$25$ Note that $v_{\text{sho}} \approx v_{\text{HB}}$ implies that “reflected” ions directed into the bulk will have a velocity $\approx 2v_{\text{HB}}$, i.e., twice the surface recession velocity, as the fastest ions generated by the piston action in HB acceleration (see Sec. IV.A.1). This similarity may explain why HB and CSA are often confused in the literature.
strongly relativistic limit \( a_0 \gg 1 \) the condition to obtain supersonic shocks driven by radiation pressure \( (M > 1) \) can be written as \( \sqrt{2a_0} > n_e/n_c \). The reflected ions may get further acceleration by the transient sheath field at the rear surface as in TNSA, eventually producing a plateau in the ion spectrum. A similar signature was observed experimentally by Zepf et al. (2003) and thus interpreted as evidence of the front side contribution to ion acceleration, in contrast to pure TNSA at the rear side of the target. Under particular conditions, the staged CSA-TNSA acceleration might produce the highest energy component in the ion spectrum as observed in simulation studies (d’Humières et al., 2005; Chen et al., 2007) which, however, also suggest lower efficiency and brilliance with respect to pure TNSA.

Recently, CSA has been indicated as the mechanism responsible for monoenergetic acceleration of protons up to 22 MeV (see Fig. 28) in the interaction of CO\(_2\) laser pulses with hydrogen gas jets at intensities up to \( 6.5 \times 10^{16} \) W cm\(^{-2} \) corresponding to \( a_0 = 2.5 \) (Haberberger et al., 2012). The particular temporal structure of the laser pulse, i.e., a 100 ps train of 3 ps pulses, was found to be essential for the acceleration mechanism, since no spectral peaks were observed for a smooth, not modulated pulse. Comparison with PIC simulations suggested that the multiple pulses lead to efficient generation of suprathermal electrons, and that this process (rather than radiation pressure) drives the shocks which eventually accelerate protons. Simulations also suggest that the process could scale in order to produce 200 MeV protons at \( 10^{18} \) W cm\(^{-2} \) that may be foreseeable with future CO\(_2\) laser development. Such a scheme based on gas lasers and gas jet target would have the advantage of high-repetition rate operation, but the efficiency per shot might be low with respect to other approaches: in the experiment of Haberberger et al. (2012) the number of ions \( (\sim 2.5 \times 10^5) \) in the narrow spectral peak at \( \approx 22 \) MeV for a 60 J pulse energy implies a conversion efficiency of \( \sim 10^{-8} \).

In addition to collisionless shocks, the standard fluid theory also predicts solitons (Tidman and Krall, 1971) propagating at the velocity \( v_{sol} \) with \( 1 < v_{sol}/c_s \leq 1.6 \). These solitons are characterized by \( Z e F_{\Phi, max} < m_i v_{sol}^2/2 \) and are thus transparent to background ions “by construction.” However, the generation of electrostatic solitons may lead to ion acceleration in some circumstances, e.g., when the soliton breaks in the expanding rear sheath due to the effect of the plasma flow (Zhidkov et al., 2002). Additional simulation studies of shock and solitary wave acceleration have been reported by He et al. (2007), Liu et al. (2009), and Macchi, Nindrayog, and Pegoraro (2012).

C. Transparency regime: Breakout afterburner

If ultrathin foils are used as targets (which requires ultrahigh-contrast, prepulse-free conditions), the expansion of the foil may lead to the onset of transparency during the short-pulse interaction, when the electron density \( n_e \) is further decreased down to the cutoff value (of the order of \( \gamma n_c \) due to relativistic effects, see Sec. II.A). While this effect limits the energy attainable via RPA (see Sec. IV.A.2), it can lead to enhanced ion acceleration via different mechanisms.

Several related experiments were performed at the TRIDENT laser facility at LANL, using pulse durations in the 500–700 fs range. C\(^{6+}\) ions with energies up to 15 MeV per nucleon were observed by irradiating DLC foils with \( \sim 40 \) J, \( \sim 7 \times 10^{19} \) W cm\(^{-2} \) pulses, for an optimal thickness of 30 nm that is determined by the condition that relativistic transparency occurs at the pulse peak (Henig et al., 2009b). Figure 29 shows spectra for different polarizations. For more energetic and intense pulses \( (\sim 80 \) J, \( 10^{21} \) W cm\(^{-2} \) and thicker targets (140 nm), broad C\(^{6+}\) spectra with higher cutoff energies beyond 40 MeV/nucleon were observed, and the inferred conversion efficiency was \( \sim 10\% \) (Hegelich et al., 2011). Narrower C\(^{6+}\) spectra \( (\Delta E_i/E_i \approx 15–20\%) \) at lower energies \( (\sim 3–10 \) MeV) were observed using either loose focusing or circular polarization (Hegelich et al., 2011; Jung et al., 2011b). Recently, energies up 80 MeV/nucleon for carbon and 120 MeV/protons have been communicated (Hegelich, 2011). The onset of relativistic transparency in these conditions was recently investigated in detail with ultrafast temporal resolution (Palantyappan et al., 2012).

Simulation studies of this regime show that the increase of the cutoff energy is related to enhanced and volumetric
heating of electrons as the target becomes transparent, leading to a stronger accelerating field for ions; the name "break-out afterburner" was proposed for such regime by the Los Alamos group (Yin et al., 2007). 3D PIC simulations of BOA have been reported by Yin et al. (2011a). Modeling of BOA is not simple as the process appears to involve different stages. Analytical descriptions of BOA have been reported by Albright et al. (2010) and Yan et al. (2010) and a scaling of the maximum ion energy \( E_{\text{max}} \approx (1 + 2\alpha)ZT_e \), with \( T_e \) the electron temperature and \( \alpha \) a phenomenological parameter (estimated to be \( \approx 3 \) from simulations), has been proposed. A fast growing relativistic Buneman instability, excited due to the relative drift between electron and ions, has been invoked as a mechanism enhancing the coupling with ions (Albright et al., 2007). Theoretical explanations for narrow \( C^{+6} \) spectra, based on an electromagnetic "ion-soliton" model (fundamentally different from electrostatic solitons described in Sec. IV.B), have been discussed by Yin et al. (2011b).

D. Acceleration in near-critical and underdense plasmas

A number of studies have been devoted to ion acceleration in near-critical plasmas with electron density close to the cutoff value \( (n_e \approx n_c) \), in order to allow a more efficient generation of hot electrons to drive TNSA. Production of a low-density plasma by a laser prepulse has been investigated for laser and target parameters such that at the time of interaction with the main short pulse the preplasma was either underdense (Matsukado et al., 2003) or slightly overdense (Yogo et al., 2008); in the latter experiment, protons up to 3.8 MeV are observed at \( 10^{19} \) W cm\(^{-2} \) intensity and directed slightly off the normal to the target rear side. Analysis of these experiments gave indication of a regime where the pressure due to a self-generated magnetic field at the rear surface strongly contributes to charge separation.

An alternative strategy to reduce the electron density is to use special target materials such as foams, which may be manufactured in order to have an average value of \( n_e \) slightly larger, or even lower than \( n_c \) (the average is meant over a length larger than the typical submicrometric scale of inhomogeneity). Experimentally, proton acceleration in low-density foams \( [n_e = (0.9 - 30)n_c] \) has been investigated by Willingale et al. (2009, 2011a) at intensities up to \( 10^{21} \) W cm\(^{-2} \), showing that the proton energy is close to that obtained for solid foils and the same laser pulse for the lowest density value \( n_c \approx 0.9n_c \). In this experiment, proton acceleration has mostly been investigated as an indication of the onset of relativistic transparency, leading to enhanced laser penetration and collimation of hot electrons and ions by self-generated magnetic fields. Recent simulation studies of ion acceleration in a solid target covered with foam layers (Zani et al., 2013) have also been reported (Nakamura et al., 2010; Sgattoni et al., 2012).

Experimental investigations of ion acceleration using gas jet targets, with typical densities below \( 10^{20} \) cm\(^{-3} \), have also been performed. These experiments include the already described investigations of hole boring RPA (see Sec. IV.A.1) and shock acceleration (see Sec. IV.B) using CO\(_2\) lasers for which gas jets are near-critical targets. Using optical or near-infrared lasers, several experiments of high-intensity laser interaction with underdense gas jets have reported observations of energetic ions accelerated in the radial direction with respect to the laser pulse propagation axis (Krushelnick et al., 1999; Sarkisov et al., 1999; Wei et al., 2004) by the electric field created by the electron displacement in the channel drilled by the ponderomotive force. The ion spectrum may provide information on the self-focusing and channeling dynamics of the laser pulse and the acceleration mechanism shows indeed some similarity with those active in the interaction with solid targets (Macchi, Ceccherini et al., 2009). However, radial acceleration of ions is of modest interest for applications since the ions are not collimated at all.

A collimated emission in the forward direction from an underdense He gas jet was reported by Willingale et al. (2006). Using a laser pulse of 1 ps duration, energy up to 340 J, and intensity up to \( 6 \times 10^{20} \) W cm\(^{-2} \), He ions up to 40 MeV were observed collimated in a beam with <10° aperture. The data were interpreted by assuming that a large electric field was generated at the rear side of the gas jet by escaping hot electrons. Different from TNSA in solid targets, the mechanism was considered to be effective despite the relatively long density scale length at the rear surface because a larger fraction of hot electrons was generated by electron acceleration in the underdense plasma. Further analysis of simulations of the experiment (Willingale et al., 2007) also showed a significant contribution due to the generation of a quasistatic magnetic field at the rear surface, which in turn enhances the accelerating electric field via magnetic pressure and induction effects according to the model by Bulanov and Esirkepov (2007) that was also used to explain the above mentioned experimental results by Yogo et al. (2008) in a near-critical plasma. Figure 30 shows a sketch of such a mechanism.

Acceleration sustained by a magnetic field was also indicated as the dominant mechanism in an experiment by Fukuda et al. (2009), where ions in a 10–20 MeV range and collimated in a 3.4° aperture cone were observed in the interaction of a \( 7 \times 10^{17} \) W cm\(^{-2} \), 40 fs laser pulse with an underdense gas jet where CO\(_2\) clusters were formed.

![FIG. 30 (color online). Sketch of magnetic field sustained acceleration of ions, showing the topology of the magnetic and electric fields and the flows of escaping and returning electron currents. From Bulanov and Esirkepov, 2007.](image)
The role of the clusters was apparently that of enhancing the self-channeling and focusing of the laser pulse, leading to an increase of the intensity in the plasma, rather than contributing to ion acceleration via cluster explosions.

The generation of collimated ions from underdense plasmas at ultrahigh intensities ($>10^{23} \text{ W cm}^{-2}$) was investigated theoretically and with numerical simulations more than a decade ago (Esirkepov et al., 1999; Bulanov et al., 2000; Sentoku et al., 2000). In particular, in these papers it was predicted that, for $a_0 > (m_i/m_e)^{1/2} \approx 43A_0^{1/2}$, the effective inertia of the highly relativistic electrons in the laser field becomes comparable to those of ions. As a consequence the ions closely follow the electron displacement due to the ponderomotive action and the acceleration process may become similar to what is observed in an overdense plasma. A few more recent simulation studies investigated a regime where a small ion target is placed in an underdense plasma (Shen et al., 2009; L.-L. Yu et al., 2010). The superintense laser pulse accelerates and overruns the ion target and then generates a wakefield in the underdense plasma, where ions may be trapped and accelerated in a way similar to the well-known scheme for laser acceleration of electrons (Esarey, Schroeder, and Leemans, 2009). In those simulations GeV energies were reached, but the required laser pulses should have mult petawatt power and multi-kJ energy, still far beyond present-day laser technology.

E. Resistively enhanced acceleration

Already during the “front versus rear side acceleration” debate related to experiments reported in 2000 (see Sec. I), it was suggested that protons may also be accelerated in the target bulk through a mechanism depending on the target resistivity $\eta$ (Davies, 2002). The electric field generated in the target bulk to provide the return current $E = j_\eta/\eta$ (see Sec. II.B.3) increases for low $\eta$ reducing the penetration of hot electrons through the target and at the same time favoring acceleration in the front and bulk regions versus TNSA. The mechanism was theoretically investigated by Gibbon (2005a) using a collisional tree-code approach.

Indications of dominant front side acceleration due to resistivity effects have been reported in solid plastic targets (Lee et al., 2008, 2011) and also in low-density foams (Li et al., 2005), where an anomalously high resistivity might be due to spatially localized fields in the locally inhomogenous material.

V. CURRENT AND FUTURE APPLICATIONS

A. Proton radiography

The use of ion beams, and particularly proton beams, for radiographic applications was first proposed in the 1960s (Koehler, 1968). Quasimonochromatic beams of ions from conventional accelerators have been used for detecting areal density variations in samples via modifications of the proton beam density cross section, caused by differential stopping of the ions, or by scattering. Radiography with very high-energy protons ($\sim 1$–$10 \text{ GeV}$) is being developed as a tool for weapon testing (King et al., 1999). Ion beams from accelerators have also been employed on some occasions for electric field measurements in plasmas, via the detection of the proton deflection, e.g., by Mendel and Olsen (1975). In practice, the difficulties and high cost involved in coupling externally produced particle beams of sufficiently high energy to laser-plasma experiments (or indeed magnetic confinement experiments) and the relatively long duration of ion pulses produced from conventional accelerators have limited the application of such diagnostic techniques.

The unique properties of protons from high-intensity laser-matter interactions, particularly in terms of spatial quality and temporal duration, have opened up a totally new area of application of proton probing or radiography. As seen in Sec. III.B, TNSA protons from a laser-irradiated foil can be described as emitted from a virtual, pointlike source located in front of the target (Borghesi et al., 2004). A point-projection imaging scheme is therefore automatically achieved with magnification $M$ set by the geometrical distances at play. Backlighting with laser-driven protons has intrinsically high spatial resolution, which, for negligible scattering in the investigated sample, is determined by the size $d$ of the virtual proton source and the width $\delta s$ of the point spread function of the detector (mainly due to scattering near the end of the proton range), offering the possibility of resolving details with spatial dimensions of a few $\mu \text{m}$. As discussed in Sec. I.E multilayer detector arrangements employing RCFs or CR39 layers offer the possibility of energy-resolved measurements despite the broad spectrum. Energy dispersion provides the technique with an intrinsic multi-frame capability. In fact, since the sample to be probed is situated at a finite distance from the source, protons with different energies reach it at different times. As the detector performs spectral selection, each RCF layer contains, in a first approximation, information pertaining to a particular time, so that a movie of the interaction made up of discrete frames can be taken in a single shot. Depending on the experimental conditions, 2D proton deflection map frames spanning up to 100 ps can be obtained. The ultimate limit of the temporal resolution is given by the duration of the proton burst at the source, which is of the order of the laser pulse duration.

Several radiographic applications of laser-produced protons have been reported to date and radiographs of objects for various size and thickness (down to a few $\sim \mu \text{m}$) have been obtained (Cobble et al., 2002; Roth et al., 2002; Borghesi et al., 2004; Mackinnon et al., 2006). Density diagnosis via proton radiography has potential application in ICF. A preliminary test studying the compression of empty CH shells under multibeam isotropic irradiation at the moderate irradiance of $10^{13} \text{ W cm}^{-2}$ has been carried out at the Rutherford Appleton Laboratory (Mackinnon et al., 2006). Radiographs of the target at various stages of compression were obtained. Modeling of proton propagation through a target and a detector carried out using Monte Carlo codes permits the retrieval of density and core size at maximum compression (3 g/cm$^3$, 80 $\mu \text{m}$) in good agreement with hydrodynamic simulations. Radiographic analysis of cylindrically compressed matter (Volpe et al., 2011) and of shock wave propagation (Ravasio et al., 2010) has also been carried out, although the available detail with low energy protons is limited.
The most successful applications to date of proton probing are related to the detection of electric and magnetic fields in plasmas (Borghesi et al., 2002b; Mackinnon et al., 2004). Jointly with a parallel technique using monoenergetic protons from fusion reactions driven from laser-driven compressions (Li et al., 2006), proton probing with laser-accelerated protons has provided in this way novel and unique information on a broad range of plasma phenomena. The high temporal resolution is here fundamental in allowing the detection of highly transient fields following short-pulse interaction.

Two main arrangements have been explored. In proton imaging, i.e., simple backlighting projection of the sample (Borghesi et al., 2001, 2002b), the deflections cause local modulations in the proton density \( n_p \) across the proton beam cross section, which, under the approximation of small deflections, can be written as

\[
\frac{\delta n_p}{n_p} \approx - \frac{eL}{2e_p M} \int_{-b/2}^{+b/2} \nabla \cdot \left( \mathbf{E} + \frac{\mathbf{v}_p}{c} \times \mathbf{B} \right) \, dx, \tag{37}
\]

where \( v_p \) and \( e_p \) are the proton velocity and energy, \( M \) is the projection magnification, \( L \) is the distance between the plasma and the detector, and the integral is along the trajectory of the protons, crossing a region \( |x| < b/2 \), where the fields \( \mathbf{E} \) and \( \mathbf{B} \) to be probed are present. Under simplified assumptions the above formula can be used to yield line-averaged values of the fields (Sarri et al., 2010a). In proton deflectometry, thin meshes are inserted in the beam between the proton source and the object as “markers” of the different parts of the proton beam cross sections (Mackinnon et al., 2004). The meshes impress a modulation pattern in the beam before propagating through the electric field configuration to be probed. The beam is in this way effectively divided in a series of beamlets, and their deflection can be obtained directly from the pattern deformation. A technique employing two grids to generate a set of moiré fringes has also been proposed as a way to increase the sensitivity to small electric fields (Mackinnon et al., 2003).

The proton probing technique has provided uniquely detailed information on nonlinear phenomena in high-intensity laser-plasma interactions, such as ion acoustic solitons and collisionless shock waves (Romagnani et al., 2008), phase-space electron holes (Sarri et al., 2010b), self-organized field structures in counterstreaming plasmas (Kugland et al., 2012), the charge-displacement channel formation dynamics following relativistic self-focusing of laser pulses (Kar et al., 2007; Sarri et al., 2010c; Willingale et al., 2011b), and the evolution of remnants of coherent electromagnetic structures and instabilities of various types (Borghesi et al., 2002a, 2005; Romagnani et al., 2010; Sarri et al., 2010d, 2011b).

Application to ns laser-produced plasmas of ICF interest has also allowed one to investigate laser filamentation in underdense plasmas (Lancia et al., 2011; Sarri et al., 2011a), plasma expansion inside hohlraums (Sarri et al., 2010a), and self-generation of magnetic fields (Nilson et al., 2006; Cecchetti et al., 2009; Willingale et al., 2010; Sarri et al., 2011a). As an example of the use of a time-resolved proton diagnostic, Fig. 13 reports data from an experiment where the protons are used to probe the rear of a foil following ultra-intense irradiation of the front of the foil (Romagnani et al., 2005). The probe proton pattern is modified by the fields appearing at the target rear as a consequence of the interaction, and the technique effectively allows spatially and temporally resolved mapping of the electrostatic fields associated with TNSA acceleration from the foil (see Sec. III.A). Figure 13(a) shows the setup for both imaging and deflectometry measurements. Figures 13(b)–13(g) correspond to proton images at different times taken in a single shot, resolving the expansion of the plasma sheath and highlighting the multiframe capability of this diagnostic.

It should be noted then on the basis of Eq. (37) it may not be possible in principle to unambiguously attribute the measured deflections to the sole action of either electric or magnetic fields. Confidence in the interpretation of observed patterns can be increased by supporting the analysis method of both imaging and deflectometry data with particle tracing codes. Such codes simulate the propagation of the protons through a given space- and time-dependent field configuration, which can be modified iteratively until the computational proton profile reproduces the experimental ones. State-of-the-art tracers allow realistic simulations including experimental proton spectrum and emission geometry, as well as detector response. Moreover, in some specific experiments it was possible to provide evidence of magnetic fields, discriminating their effect on probe protons from that due to electric fields, by using different probing directions (Cecchetti et al., 2009) or even exploiting the divergence of the probe beam (Romagnani et al., 2010). An example is given in Fig. 31 where the presence of an azimuthal \( \mathbf{B} \) field appearing at the target rear as a consequence of the interaction, and the technique effectively allows spatially and temporally resolved mapping of the electrostatic fields associated with TNSA acceleration from the foil (see Sec. III.A). Figure 13(a) shows the setup for both imaging and deflectometry measurements. Figures 13(b)–13(g) correspond to proton images at different times taken in a single shot, resolving the expansion of the plasma sheath and highlighting the multiframe capability of this diagnostic.

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![Image](https://example.com/image.png)

FIG. 31. Proton probing of magnetic fields. (a), (c) Probing deflectogram of a laser-irradiated foil (ns pulse, \( 10^{15} \text{ W cm}^{-2} \) on a \( 6 \mu \text{m Al foil} \) obtained with a 5.5 MeV proton beam facing the foil, entering from the nonirradiated side in (a) and from the opposite, laser-irradiated side in (c). The inversion of the deflection pattern reveals the effect of a toroidal \( \mathbf{B} \) field [the asymmetrical pattern in (c) is due to a nonideal intensity distribution in the focus]. (b), (d) Particle tracing simulations for the conditions of (a) and (c) assuming a suitably parametrized \( \mathbf{B} \) field. From Cecchetti et al., 2009.)
has been revealed with mesh deflectometry by either a compression or outward dilation of the mesh lines, depending on whether the B field has clockwise or counterclockwise direction compared to the propagation direction of the probe beam.

The divergence of the probe beam also implies that the effective probing time is a function of the position on the image plane because of the different time of flight for protons at different angles. This effect has to be taken into account for measurement of field structures propagating at relativistic speeds (Karl et al., 2007; Quinn et al., 2009a) and actually may improve the capability to characterize such structures, as it was obtained by a slightly modified arrangement (Quinn et al., 2009b). This allowed one to observe the ultrafast, transient field front associated with the early stage of TNSA where electromagnetic effects come into play (see Fig. 32). A proton streak deflectometry technique for obtaining continuous temporal mapping (but only one spatial dimension is resolved) has also been proposed in which the energy resolution is achieved by means of magnet dispersion (Sokollik et al., 2008).

**B. Production of warm dense matter**

Laser-driven ions have found application in a number of experiments aimed to heat up solid-density matter via isochoric heating, and create so-called warm dense matter (WDM) states, i.e., matter at 1–10 times solid density and temperatures up to 100 eV (Koenig et al., 2005) of broad relevance to material, geophysical, and planetary studies (Ichimaru, 1982; Lee et al., 2003). The high-energy flux and short temporal duration of laser-generated proton beams are crucial parameters for this class of applications. WDM states can be achieved by several other means, e.g., x-ray heating (Tallents et al., 2009) and shock compression (Kritcher et al., 2008). However, when studying fundamental properties of WDM, such as the equation of state (EOS) or opacity, it is desirable to generate large volumes of uniformly heated material; ion beams, which can heat the material in depth, are in principle better suited to this purpose than the methods described above.

Heating of solid-density material with ions can be achieved with accelerator-based or electrical-pulsed ion sources; see, e.g., Bailey et al. (1990), Hoffmann et al. (2000), and Tahir et al. (2006). However, the relatively long durations of ion pulses from these sources (1–10 ns) imply that the materials undergo significant hydrodynamic expansion already during the heating period. On the contrary, laser-generated proton beams, emitted in ps bursts, provide a means of very rapid heating, on a time scale shorter than the hydrodynamic time scale. By minimizing the distance between the ion source and the sample to be heated, it is possible to limit the heating time to tens of ps. The target then stays at near-solid density before significant expansion occurs, and the WDM properties can be investigated within this temporal window.

The first demonstration of laser-generated proton heating was obtained by Patel et al. (2003). In this experiment a 10 J pulse from the 100 fs JanUSP laser at LLNL was focused onto an Al foil producing a 100–200 mJ proton beam used to heat a second Al foil. Target heating was monitored via time-resolved rear surface emission, as shown in Fig. 33. A focused proton beam, produced from a spherically shaped target (see Sec. III.E.3), was seen to heat a small target region to a temperature (of ~23 eV). With a similar ion focusing arrangement on a higher energy laser system, Gekko at ILE Osaka, Snavely et al. (2007) demonstrated secondary target heating up to 80 eV by imaging both visible and extreme-ultraviolet Planckian emission from the target’s rear surface.

Subsequent experiments have investigated the properties of the WDM produced with this approach with a number of diagnostics, either passive or in pump-probe configurations, combined to self-consistent modeling of sample heating and expansion. Warm solid Al at temperatures up to 15–20 eV (Dyer et al., 2008; Mančić et al., 2010b) and carbon up to ~2 eV (Roth et al., 2009) have been produced in this manner. Dyer et al. (2008) reconstructed the EOS of the heated material by measuring the temperature and expansion rate of the heated...
target, via streaked thermal emission and chirped pulse interferometry.

Pump-probe arrangements have been used in recent, more sophisticated experiments, which have provided novel information on the transition phase between cold solid and plasmas in isochorically heated Al and C targets. Mančić et al. (2010a) investigated the short range disordering of warm Al at solid density by applying time-resolved x-ray absorption near-edge spectroscopy (see Fig. 34). Progressive smoothing of spectral features near the K edge allowed one to place an upper bound on the onset of ion lattice disorder within the heated solid-density medium of 10 ps. Pelka et al. (2010) recently diagnosed ultrafast melting of carbon samples, by x-ray scattering techniques, which allowed determination of the fraction of melted carbon in the heated sample. Comparison to predictions based on different theoretical descriptions of the EOS of carbon indicates a departure from existing models, with implications for planetary core studies.

In all the experiments mentioned above the isochoric heating by the protons is volumetric, but not uniform (Brambrink et al., 2007); see, e.g., Fig. 34(c). Uniform heating requires some degree of proton energy selection, and choosing the sample thickness so that the Bragg peak of the selected protons does not fall within the sample, as suggested, for example, by Schollmeier et al. (2008).}

C. Fast ignition of fusion targets

The traditional route to ICF (Atzeni and Meyer-ter-Vehn, 2004) relies on the driven implosion of a pellet of thermonuclear fuel (a DT mixture). Ignition occurs in a central “hot spot” following pulse compression. This approach requires an extremely high symmetry and is prone to hydrodynamics instabilities, making ICF a historically difficult goal.

In the fast ignition (FI) concept [see Key (2007) for a compact review] ignition is driven by an external trigger, creating the hot spot in a time much shorter than the typical fuel disassembly time. Hence, ignition is separated from pulse compression. The FI approach might relax symmetry and stability requirements, reduce the energy need for ignition, and allow fuel burn in a isochoric regime with high fusion gain.

In the original FI proposal by Tabak et al. (1994), the ignitor beam consisted of multi-MeV electrons accelerated by a petawatt laser pulse via the mechanisms described in Sec. II.B. Subsequent research showed that, besides generating an electron beam with enough power to ignite, most problematic were the issues of energy transport and deposition in the core. Concerning the latter issue, the energy deposition profile of electrons is a smooth function, making it difficult to produce a localized hot spot.

Observation of efficient generation of multi-MeV proton beams in petawatt experiments (Hatchett et al., 2000; Snively et al., 2000) soon stimulated the proposal of the use of such protons as the ignitor beam (Roth et al., 2001). The most promising features of proton beam ignition as claimed were the highly localized energy deposition profile (see Fig. 3), the low emittance of the beam, and its focusability, for instance, by parabolically shaping the rear side of the proton-producing target as suggested by numerical simulations (Ruhl et al., 2001; Wilks et al., 2001).

Detailed calculations by Atzeni, Temporal, and Honrubia (2002) and Temporal, Honrubia, and Atzeni (2002) addressed, in particular, the effects of the quasithermal energy distribution typical of TNSA protons, and of the related temporal dispersion. The latter could be beneficial for energy deposition since the proton stopping range increases with plasma temperature. Hence, heating due to the more energetic protons favors energy deposition by the less energetic ones which arrive later in the dense fuel region. A fit of simulations for a proton temperature of 5 MeV provided the following estimate of the ignition energy

\[ \mathcal{E}_{\text{ig}} \approx 90(d/\text{mm})^{0.7}(\rho/100\,\text{g}\,\text{cm}^{-3})^{-1.3} \, \text{kJ}. \]  

Integration of the foil inside the cone of conical ICF targets already designed for electron FI was then proposed in order to reduce \( d \) and thus \( \mathcal{E}_{\text{ig}} \). This raised the issue of shielding the foil from preheating caused, e.g., by external radiation, which may jeopardize efficient TNSA (see Sec. III.E.1); a preliminary analysis was mentioned by Geissel et al. (2005). Figure 35 sketches the target and foil assembly and summarizes suitable parameters for proton FI with cone targets. Temporal (2006) and Temporal, Honrubia, and Atzeni (2008) investigated a similar scheme but used two proton beams with suitably shaped radial profiles, obtaining a 40% reduction of the ignition energy.

\[ \mathcal{E}_{\text{ig}}^{26} \text{ includes only the energy of the proton beam. The total energy of the laser driver is } \mathcal{E}_{\text{L}}/\eta_p \text{ with } \eta_p < 1 \text{ the conversion efficiency into protons.} \]
Independent from Roth et al. (2001), fast ignition by laser-accelerated light ion beams was proposed by Bychenkov, Rozmus et al. (2001). The use of deuterons and beryllium ions was investigated, and it was suggested that using ions with $Z > 1$ could be advantageous because of their higher stopping power with respect to protons. Calculations by Honrubia et al. (2009) showed that, different from the proton-based scheme, ions with a narrow energy spread $dE/E$ would allow one to lower the ignition threshold: for $dE/E = 0.1$, $E_{ig} < 10 \text{ kJ}$ might be obtained. This feature might also relieve the need to place the ion producing foil in a reentrant cone, yielding a simpler target design (Fernández et al., 2009). The estimated parameters for a C ignitor beam are 400–500 MeV energy per ion, $\geq 10\%$ efficiency, and $dE/E < 0.2$. To achieve such values, mechanisms such as RPA (see Sec. IV.A) or BOA (see Sec. IV.C) might be more suitable than TNSA. Progress in related research was recently reported by Hegelich et al. (2011), where separate experiments approaching the three above mentioned requirements are described. A fourth and so far unexplored issue might be the need to focus the ion beam.

Another approach (Naumova et al., 2009) to ion-driven FI is based on RPA in the hole boring regime (see Sec. IV.A.1). In such a scheme, different from the above described ones, ion acceleration occurs in situ by direct interaction of an ultraintense, circularly polarized laser with the corona of the fusion plasma. Tikhonchuk et al. (2010) reported calculations with this scheme, assuming direct acceleration of deuterons and characterizing possible high gain regimes with $E_{ig} \approx 12–17 \text{ kJ}$. This corresponds to an overall ignition energy $>100 \text{ kJ}$ and a required laser intensity exceeding 10$^{22}$ W cm$^{-2}$. FI by laser-accelerated ions was investigated theoretically in several other works.\textsuperscript{27} Integrated FI studies, on the route to ignition-class experiments, could be performed in either the electron or the ion approach in facilities to be developed, equipped with petawatt-class laser systems.

D. Biomedical applications

Hadron therapy is the radiotherapy technique that uses protons, neutrons, or carbon ions to irradiate cancer tumors. The use of ion beams in cancer radiotherapy\textsuperscript{28} exploits the advantageous energy deposition properties of ions as compared to more commonly used x rays (see Fig. 3): the range for a proton or ion is fixed by its energy, which avoids irradiation of healthy tissues at the rear side of the tumor, while the well-localized Bragg peak leads to a substantial increase of the irradiation dose in the vicinity of the stopping point. The proton energy window of therapeutic interest ranges between 60 and 250 MeV, depending on the location of the tumor (the required carbon ion range extends up to 400 MeV/nucleon). The typical dose of a treatment session is in the 1–5 gray range, and typical currents are 10 nA for protons and 1.2 nA for singly charged carbon ions.

Ion beam therapy has proven to be effective and advantageous in a number of tumors and several clinical facilities, employing mainly protons from synchrotron, cyclotron, or linac accelerators are operational and routinely treating a significant number of patients. While protons are the most widespread form of ion treatment, facilities using carbon ions also exist, as their higher biological effectiveness makes them suitable to treating radioresistant and hypoxic tumors (Schardt, 2007). In treatment centers, magnetic steering systems (Gantries) are employed for multidirectional irradiation of a lying patient. Gantries are costly, large, and massive, with a weight exceeding 100 tons for proton systems, and 500 tons for carbon systems (Enghardt et al., 2011).

The use of laser-based accelerators was proposed as an alternative to rf accelerators in proton and ion therapy systems (Bulanov et al., 2002; Bulanov and Khoroshkov, 2002; Fourkal, Li, Xiong et al., 2003; Malka et al., 2004), with potential advantages in terms of compactness and costs. Proposed options range from using laser-driven protons as high quality injectors in a rf accelerator (Antici et al., 2011) to all-optical systems, in which ion beam acceleration takes place in the treatment room itself and ion beam transport and delivery issues are thus minimized (Bulanov et al., 2002). It is recognized that there are significant challenges ahead before laser-driven ion beams meet therapeutic specifications, in terms of maximum energy, energy spectrum, repetition rate, and general reliability, to the levels required by the medical and therapeutic standards, as reviewed by Linz and Alonso (2007), where specific issues are mentioned and a comparison with existing accelerator technologies is made. At present, the ion beam parameters are still far from the requirements and it is clear that an extensive, long term activity will be needed to ascertain if and how laser-driven ion beams may become a


\textsuperscript{28}The use of energetic protons in radiology was first proposed by Wilson, (1946) and demonstrated by Lawrence (1957). Recent reviews on the state of the art in ion beam therapy are given by Amaldi and Kraft (2005), Smith (2009), and Schardt, Elsässer, and Schulz-Ertner (2010). Focus on research and possible improvements in therapy with heavy ions is given by Kraft and Kraft (2009).
competitive option. Several projects are currently active worldwide to explore the potential of laser-driven proton and ion sources for biomedical applications; see, e.g., Bolton et al. (2010), Borghesi et al. (2011), and Enghardt et al. (2011). In view of future applications, several authors have started to design possible delivery systems, including target chamber and shielding (Ma et al., 2006), particle energy selection, and beam collimation systems to enable operation with the broadband and diverging laser-driven beams (Fourkal, Li, Ding et al., 2003; Nishiuchi et al., 2010b; Hofmann et al., 2011).

While currently a relative energy spread $\Delta E/E \approx 10^{-2}$ is required for optimal dose delivery over the tumor region, many have also modeled approaches in which the native broad spectrum of laser-accelerated ions is used to directly obtain the spread out Bragg peak distributions which are normally used to cover the tumor region (Fourkal et al., 2007; Luo et al., 2008) and more in general advanced methods exploiting the properties of laser-accelerated beams (Schell and Wilkens, 2010).

An important step in view of their future medical use is to assess the biological effect of laser-driven ions and highlight any peculiarity associated with their pulsed, ultrashort temporal profile. Yogo et al. (2009) first demonstrated the feasibility of cell irradiation studies using laser-driven protons, employing a suitable beam transport setup and then applied a refined technique to infer, via a clonogenic assay, the relative biological effectiveness (RBE) of ~2 MeV laser-accelerated protons, as compared to irradiation with a standard x-ray source (Yogo et al., 2011), in human cancer cells. The RBE observed (1.2 ± 0.1) is comparable with literature results employing rf-accelerated protons of comparable linear energy transfer (LET) (Folkard, 1996). The dose required to cause significant cell damage (typically 1 to several gray) was obtained in several irradiations taking place at 1 Hz repetition rate. Kraft et al. (2010) also carried out proton irradiations of cells, highlighting dose-dependent incidence of a double-strand DNA break in the cells (see Fig. 36).

The peculiar characteristics of laser-driven protons have required the development of innovative dosimetric approaches, as described, for example, by Fiorini et al. (2011) and Richter et al. (2011). In all these experiments, the dose [1–10 grays (Gy)] is delivered to the cells in short bursts of ~ns duration. In experiments by Kraft et al. (2010) and Yogo et al. (2011) the dose is fractionated and the average dose rate is comparable to the one used in irradiations with conventional accelerator sources (~0.1 Gys$^{-1}$). In a recent experiment (Fiorini et al., 2011; Doria et al., 2012) employing a high-energy ps laser system, it was possible to reach up to 5 Gy in a single exposure, reaching dose rates as high as $10^9$ Gys$^{-1}$. This allows access to a virtually unexplored regime of radiobiology, where, in principle, nonlinear collective effects (Fourkal et al., 2011) on the cell due to the high proton density in the bunch may become relevant.

Besides cancer therapy, application of laser-driven ion beams in medical diagnosis has also been proposed. Multi-MeV proton beams can induce nuclear reactions in low-Z materials (see Sec. V.E) in order to produce neutrons of possible interest for boron neutron capture therapy for cancer, or short-lived positron emitting isotopes which may be employed in positron emission tomography (PET). PET has proven to be extremely useful in medical imaging of blood flow and amino acid transport and in the detection of tumors. Usually, reactions for PET are carried out by using up to 20 MeV protons or similar energy deuterons from cyclotrons with the concomitant problems of large size and cost and extensive radiation shielding. Production of short-lived isotopes via laser-driven proton beams may be feasible in the near future with the possibility of employing moderate energy, ultrashort, high-repetition tabletop lasers. Extrapolations based on present results point to the possibility of reaching the gigaBecquerel (GBq) activities required for PET if laser systems capable of delivering 1 J, 30 fs pulses focused at $10^{20}$ W cm$^{-2}$ with kHz repetition will become available (Fritzler et al., 2003; Lefebvre et al., 2006) and economically competitive with existing technologies.

E. Nuclear and particle physics

The interaction of laser-driven high-energy ions with secondary targets can initiate nuclear reactions of various types, which as mentioned (see Sec. I.E) can be used as a tool to diagnose the beam properties. This also presents the opportunity of carrying out nuclear physics experiments in laser laboratories rather than in accelerator or reactor facilities, and to apply the products of the reaction processes in several areas. Reactions initiated by laser-accelerated high-Z ions have been studied in a number of experiments, McKenna et al. (2003a, 2003b, 2004) showed that reactions between fast heavy ions from a laser-produced plasma and stationary atoms in an adjacent “activation” sample create compound nuclei in excited states, which deexcite through the evaporation of protons, neutrons, and $\alpha$ particles. A similar experiment...
with protons driving nuclear reactions and excitations in a Cu target was reported by Hannachi et al. (2007). Nuclear reactions of interest for spallation physics have also been investigated by employing multi-MeV proton beams (McKenna et al., 2005). The broad energy distribution of the beams is in this case advantageous for the determination of residual nuclide generation arising from specific spallation processes such as evaporation. In addition, MeV proton interaction with low-Z materials can produce short-lived isotopes29 of medical interest, e.g., for PET diagnostic (see Sec. V.D).

Recently, a scheme of a “fission-fusion” process driven by RPA (see Sec. IV.A) was also proposed to produce neutron-rich nuclei in the range of the r process (Habs et al., 2011); such studies, of relevance for astrophysical nucleosynthesis, would require intensities above $3 \times 10^{22}$ W cm$^{-2}$ that may be available with next-generation short-pulse laser facilities.

Neutrons are an important product of the above mentioned nuclear reactions, with potential applications in cancer therapy, neutron radiography, radiation damage of materials, and transmutation of nuclear waste. The potential for laser-driven neutron sources is considerable and offers advantages over accelerator- and reactor-driven sources in terms of cost, compactness, brightness, and short duration for applications such as fast neutron radiography (Lancaster et al., 2004) and studies of impulse damage of matter (Perkins et al., 2000). This has motivated several experiments on the production of neutrons initiated by laser-driven proton beams on secondary targets. Experiments carried out at the VULCAN laser facility revealed neutron yields up to $4 \times 10^9$ sr$^{-1}$ per pulse at a laser intensity of $3 \times 10^{20}$ W cm$^{-2}$ (Yang et al., 2004a), produced via the $^{11}$B$(p, n)^{11}$C and $^7$(Li$(p, n)^7$Be reactions. The latter was also investigated by Youssef, Kodama, and Tampo (2006) as a diagnostic of proton acceleration. Neutron production was also observed in interactions with solid targets containing deuterium (typically deuterated plastic), which can be either directly irradiated by high-intensity laser pulses (Norreys et al., 1998; Disdier et al., 1999; Habara et al., 2003, 2004b; Willingale et al., 2011a) or irradiated by ions accelerated on a separate target (Fritzler et al., 2002; Karsch et al., 2003). In both cases the neutrons are produced in the course of fusion reactions of the type $D(d, n)^{10}$He involving laser-accelerated deuterium ions as also observed in gaseous targets (Ditmore et al., 1997; Grillon et al., 2002). Numerical modeling and theoretical investigations of laser-driven neutron production have been carried out; see, e.g., Toupin, Lefebvre, and Bonnaud (2001), Macchi (2006), Davis and Petrov (2008, 2011), and Ellison and Fuchs (2010).

Application of laser-accelerated ions in particle physics requires “by definition” the ions to be relativistic, i.e., their total energy must exceed the rest energy whose value per nucleon is $\sim m_p c^2 \approx 0.94$ GeV. Presently, observed cutoff energies are more than an order of magnitude below this threshold. Nevertheless, the scalings inferred from either experiments or theoretical models and the foreseen availability of higher laser powers in a few years suggests that GeV ions may eventually be produced and applied in selected particle physics experiments. Moreover, it should be noted that the very low emittance that can be obtained for laser-accelerated ions makes them suitable for postacceleration, e.g., as an injection source for heavy ion accelerators (Krushelnick et al., 2000). Specific advantages might be the high number of ions produced per shot combined with the short duration.

Bychenkov, Sentoku et al. (2001) estimated the threshold for production of pions by protons accelerated in a solid target, obtaining that at intensities above $10^{21}$ W cm$^{-2}$ the flux of pions may be much higher than obtained with conventional accelerator techniques. It should be noted that the prompt laser-driven, high field-gradient acceleration of pions is of much interest because of the finite lifetime of such particles; a related discussion was given by Mourou, Tajima, and Bulanov (2006).

Pakhomov (2002) proposed the use of laser-accelerated protons at intensities of $\approx 10^{23}$ W cm$^{-2}$ to drive, via pion generation and decay, pulses of 20 MeV muon neutrinos of interest for, e.g., studies of neutrino oscillations. Bulanov et al. (2005) further explored this concept suggesting the radiation pressure dominated acceleration regime (see Sec. IV.A.2) as suitable for this class of experiments. A more general discussion of the required laser developments was given by Terranova et al. (2006).

VI. CONCLUSIONS AND OUTLOOK

We reviewed about 12 years of research on ion acceleration driven by superintense laser pulses. The most investigated acceleration mechanism, namely, the so-called target normal sheath acceleration, has been extensively discussed, surveying both the main experimental achievements and the underlying theoretical interpretation. In addition, we provided an outlook to other proposed acceleration schemes, such as radiation pressure acceleration, shock acceleration, breakout afterburner, acceleration in near-critical and underdense plasmas, and resistively enhanced acceleration. For these mechanisms, the fundamental theoretical ideas have been presented, together with the most promising experimental results. A brief presentation of promising possible applications of the laser-generated ion beams has been given. While we were completing our work, another extended review on this topic was published (Daido, Nishiuchi, and Pirozhkov, 2012), which we recommend as complementary reading.

This field of research has attracted much interest and has shown unique potential both for innovative investigations and for applicative purposes. The development in laser technology and the increasing use of advanced methods of material science for target manufacturing has resulted in a high level of sophistication of current experiments, with new physical issues continuously emerging from experimental investigations. At the same time, theory and simulation have naturally found a fertile field, which poses original problems and suggests unexplored paths for reaching their solution. The vitality of this research area is well demonstrated by the need for frequent updates during the preparation of this review, as new significant results continuously appeared in the literature.

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29Typical short-lived positron emitters include $^{11}$B, $^{11}$C, $^{13}$N, $^{15}$O, $^{18}$O, and $^{38}$F. Related experiments have been reported by Nemoto et al. (2001), Fritzler et al. (2003), Ledingham, McKenna, and Singhal (2003), Clarke et al. (2006), Fujimoto et al. (2008, 2009), and Ogura et al. (2009).
As discussed in the Introduction, future developments and achievements are naturally linked to foreseen developments in laser technology, providing for the first time extreme laser intensities close to or even beyond the limit at which the ions become relativistic. Emerging laser projects will enable one to verify the scaling of ion acceleration physics in the ultra-high-intensity regimes and its suitability for proposed applications, as well as to test theoretical ideas and provide to fundamental physics an example of “relativity in action” in a macroscopic, many-body system. The expected progress is not exclusively related to further developments of the solid state laser technology which has been so far the preferred route to producing high-intensity laser pulses, as, for example, recent experiments have attracted novel interest also in old technology such as CO₂ laser systems. Smart and advanced target engineering, e.g., development of multilayer, low-density, microstructured, and nanostructured targets, will also play an important role in establishing future directions of ion acceleration.

The successful developments in this first period lead to a series of open questions, which will inform research in this field over the coming years. Will it be possible to reach and break the GeV/nucleon threshold? Will researchers achieve an active and satisfactory experimental control on the physics of laser ion acceleration by working on the detailed properties of laser pulses and of target material and structure? Is there hope to pursue front-edge nuclear and particle physics research in small-scale laboratories thanks to the use of laser-driven ion beams? Will the research on ion acceleration result in practical, technological applications of direct societal benefit? We leave to the future experimental and theoretical research the answer to these and many other questions, some of which we probably do not even imagine today.

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