Table-Top Laser-Based Source of Femtosecond, Collimated, Ultrarelativistic Positron Beams


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The generation of ultrarelativistic positron beams with short duration (\(\tau_p \approx 30\) fs), small divergence (\(\theta_p \approx 3\) mrad), and high density (\(n_p \approx 10^{14} - 10^{15}\) cm\(^{-3}\)) from a fully optical setup is reported. The detected positron beam propagates with a high-density electron beam and \(\gamma\) rays of similar spectral shape and peak energy, thus closely resembling the structure of an astrophysical leptonic jet. It is envisaged that this experimental evidence, besides the intrinsic relevance to laser-driven particle acceleration, may open the pathway for the small-scale study of astrophysical leptonic jets in the laboratory.

The possibility of generating high density and high energy electron-positron beams is of central importance also for astrophysics due to their similarity to jets of long gamma-ray bursts [15]. These structures still present enigmatic features which are virtually impossible to address by simply relying on direct observations. A possible solution might be represented by reproducing small scale electron-positron jets (required bulk flow Lorentz factor of the order of 100–1000) in the laboratory. Although gamma-ray burst jets may have a weak large scale magnetic field [16], the external shock is exclusively mediated by self-generated microscale magnetic fields. A purely electronic jet would present toroidal magnetic fields whose strength and structure would be comparable to the microscale fields that develop in response to the filamentation instability [17] and modify the shock physics. The presence of the highly mobile positrons would reduce the overall magnetization of the jet, simplifying the interpretation of the experimental data and their comparison with the astrophysical scenario.

Here we experimentally demonstrate the possibility of producing collimated and high-density ultrarelativistic positron beams in a fully laser-driven configuration. Their low divergence and short duration (comparable to those of the incoming laser-driven electron beam) suggest the possibility of applying this generation scheme to current laser facilities towards the construction of a fully optical generator of high-quality, ultrarelativistic positron beams. Furthermore, the measured high positron Lorentz factors (\(\gamma_p \approx 200–300\), compared to \(\gamma_e \approx 40\) in Refs. [10–12]) of these beams are finally comparable to those of astrophysical leptonic jets. This, in conjunction with the low divergence, the inferred electron-positron balance, and co-propagation with intense gamma-rays, finally opens up a realistic possibility of studying the dynamics of such jets in the laboratory.
The experiment [shown schematically in Fig. 1(a)] was carried out using the HERCULES laser system at the Center for Ultrafast Optical Science at the University of Michigan [18], which delivered a laser beam with a central wavelength $\lambda_L = 0.8 \mu$m, energy $E_L = 0.8$ J, and duration $\tau_L = 30$ fs. This laser beam was focused using an $f/20$ off-axis parabola, onto the edge of a 3 mm wide supersonic He gas jet, doped with 2.5% of $\text{N}_2$, with a backing pressure of 5.5 bar. Once fully ionized, this corresponds to an electron density of $9 \times 10^{18}$ cm$^{-3}$. The focal spot size was measured to have a radius of 23 cm which contained 50% of the laser energy (peak intensity of $I_L = 6 \times 10^{18}$ W/cm$^2$). Laser power and gas-jet pressure were chosen in order to stay slightly above the threshold for ionization injection [19]. This interaction delivered a reproducible electron beam with a divergence at full width at half maximum of approximately 1.4 mrad (corresponding to a full width at total maximum of 2.5 mrad [see Figs. 1(b) and 1(c), and Fig. 1 of the Supplemental Material [20]]) Its spectrum was measured, prior to any shot with a high-Z solid target, by a magnetic spectrometer consisting of a 0.8 T, 15 cm long pair of magnets and a LANEX screen. The arrangement of the spectrometer did not allow us to resolve electron energies below 80 MeV. Typical spectra, obtained using the calibration curves reported in Ref. [21], indicated the charge carried by electrons with energy exceeding 80 MeV to be of the order of 50 pC ($N_{\gamma}$, expressed as $10^3$ positrons MeV$^{-1}$ cm$^{-2}$) constant, the positron yield $N_{e^+}$ is expected to scale as $N_{e^+} \propto (Z^2 n d)^j$, where $n$ is the number of atoms per unit volume in the material, $d$ is the thickness of the solid target, and $j = 1$ for the trident process and $j = 2$ for the two-step cascade process (we neglect here Coulomb corrections, which depend on $Z\alpha$, with $\alpha = 1/137$ being the fine-structure constant). Neglecting the difference between the proton and the neutron mass, the mass density of the solid target is $\rho = A m_p n$, with $A$ and $m_p$ being the atomic number and the proton mass, respectively. If we maintain the areal mass density ($\sigma = \rho d$) constant, we can then express the scaling as $N_{e^+} \propto (Z^2/A)^j$. We have thus performed a series of shots for different materials (Cu, Sn, Ta, Pb) adjusting the target thickness so that the areal mass density was kept constant for each material ($\sigma = 4.7$ g/cm$^2$, see the first four rows in Table I). All the measured positron spectra presented a monotonically decreasing profile with approximately $10^7$ positrons/Mev (solid lines in Fig. 2). In all cases, numerical simulations performed with the nuclear physics Monte-Carlo code FLUKA, which accounts for electromagnetic cascades during the passage of an electron beam through a solid target [28], are able to reproduce the experimental data on the IP for 4.2 mm of Ta. Due to the small difference in positron and electron stopping power (below 2% [23]), the signal recorded was absolutely calibrated by using the calibration curves reported in Ref. [24]. Plastic and Teflon shielding were inserted to reduce the noise on the IP induced by both the low-energy electrons and gamma rays generated, at wide angles, during the laser-gas and electron-solid target interactions [see Fig. 1(a)]. In these experimental conditions, the positrons inside the high-Z target are mainly generated via either direct electro-production (trident process), in which pair production is mediated by a virtual photon in the electron field [25], or via a two-step “cascade” process where the electron first emits a real photon (bremsstrahlung) [26], which then produces an electron-positron pair via the Bethe-Heitler process [27]. Keeping the parameters of the electron beam constant, the positron yield $N_{e^+}$ is expected to scale as $N_{e^+} \propto (Z^2 n d)^j$, where $n$ is the number of atoms per unit volume in the material, $d$ is the thickness of the solid target, and $j = 1$ for the trident process and $j = 2$ for the two-step cascade process (we neglect here Coulomb corrections, which depend on $Z\alpha$, with $\alpha = 1/137$ being the fine-structure constant). Neglecting the difference between the proton and the neutron mass, the mass density of the solid target is $\rho = A m_p n$, with $A$ and $m_p$ being the atomic number and the proton mass, respectively. If we maintain the areal mass density ($\sigma = \rho d$) constant, we can then express the scaling as $N_{e^+} \propto (Z^2/A)^j$. We have thus performed a series of shots for different materials (Cu, Sn, Ta, Pb) adjusting the target thickness so that the areal mass density was kept constant for each material ($\sigma = 4.7$ g/cm$^2$, see the first four rows in Table I). All the measured positron spectra presented a monotonically decreasing profile with approximately $10^7$ positrons/Mev (solid lines in Fig. 2). In all cases, numerical simulations performed with the nuclear physics Monte-Carlo code FLUKA, which accounts for electromagnetic cascades during the passage of an electron beam through a solid target [28], are able to reproduce the experimental data

FIG. 1 (color online). (a) Top view of the experimental setup. The magnet is rotated by 90° for the sake of illustration. (b) Typical positron signal as recorded by the image plate for 4.2 mm of Ta. The dark region on the upper part is predominantly exposed by the $\gamma$ rays escaping the solid target. (c) Typical signal of the electron beam as recorded on the LANEX screen, without a solid target (see Fig. 1 of the Supplemental Material [20] for a ten-shot series). (d) Extracted spectrum and relative best fit (linear + Gaussian) used as an input for FLUKA simulations.

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well (dashed lines in Fig. 2). As an input for the simulation 
10^6 electrons with a spectral shape like the one depicted in 
Fig. 1(c) were used. An average over five identical runs 
was performed for each material in order to minimize any 
stochastic error arising from the random seed generator of 
the code. As theoretically predicted, the positron yield 
increases for materials with higher atomic number. This 
trend is quantitatively confirmed by integrating the experi-
mental spectra in the range 90 < E_e (MeV) < 120 (see 
Table I and Fig. 3). Within this energy range, a maximum 
positron number of (2.30 ± 0.28) × 10^5 is obtained for the 
material with the highest Z (Pb). Fitting the data keeping j 
as a free parameter, we obtain a best fit for j = 2.1 ± 0.1 
confirming the dominance of the cascade process with 
respect to the trident one [see Fig. 3(b)]. The positron yield 
over the entire positron spectrum, as extracted from match-
ing FLUKA simulations (N_f in Table I), is seen to follow a 
similar trend. A further indication as to what process 
dominates is given by the dependence of the positron yield 
upon the target thickness (N_f ∝ d for the trident and 
N_f ∝ d^2 for the two-step process). A series of shots was 
thus taken varying the thickness of the solid target d for Ta 
and Pb [second four rows in Table I and Fig. 3(a)]. As 
expected, the positron yield scales with d^2 in both cases. 
In order to support this statement theoretically, we compare, 
for each material, the radiation length L_rad with the range 
of target thicknesses d used in the experiment. The two-
step process is expected to dominate the trident one if 
d/L_rad ∼ 10^{-2} [25]. For an order-of magnitude estimate 
of L_rad, we can assume here to be in the total-screening 
regime which, for an electron with energy e emitting a 
photon with energy hω, occurs if the parameter 
S = α Z^{1/3} e (e − hω) / (hω c^2) is much larger than unity (a 
Thomas-Fermi model of the atom is assumed [29]). 
Estimating e ∼ hω ∼ 100 MeV, we have S ∼ 4 in the 
worse case of Cu, which is sufficiently large for the present 
estimate. In this regime, and by including Coulomb cor-
corrections, the radiation length is approximately given by 
[29] L_{rad} = 1/[4α(Za)^2 n^2 L_q], where n is the number of 
atoms per unit volume, λ_C = h/mc = 3.9 × 10^{-11} cm is the 
Compton wavelength, and L_0 = log(1832Z^{−1/3}) − 
f(Zα), with f(x) = ∑_{x=1}^{∞} x^2/6 (x^2 + x^2). This gives 
L_{rad}(Cu) = 15 mm, L_{rad}(Sn) = 12 mm, L_{rad}(Ta) = 
4.1 mm, and L_{rad}(Pb) = 5.6 mm. The material thicknesses 
are thus always such that the inequality d/L_{rad} ≥ 10^{-2} is 
fulfilled, in agreement with the experimental indication of 
the predominance of a two-step process for the electromag-
netic cascade. Moreover, in all the considered cases, 
except one where d = 4.2 mm for Ta, it is the case that 
d < L_{rad}, which implies that the contribution of higher-
order cascade processes can generally be neglected for an

![Image](54x128 to 297x272)

**FIG. 2 (color online).** Experimental (solid lines) and simulated 
(dashed lines) positron spectra for (a) 5.3 mm of Cu, (b) 6.4 mm 
of Sn, (c) 2.8 mm of Ta, and (d) 4.1 mm of Pb. Each experimental 
spectrum results from an average over ten consecutive shots.

![Image](332x205 to 543x330)

**FIG. 3 (color online).** (a) Measured positron yield, in the 
energy range 90 < E_e (MeV) < 120 for Ta (blue full circles) 
and Pb (red empty circles) for different target thicknesses. Lines 
give the best quadratic fits. (b) Measured positron yield, in the 
energy range 90 < E_e (MeV) < 120, for different materials but 
constant areal density as a function of Z^2/A. The dashed line 
represents the best quadratic fit. In both graphs, the values result 
from an average over ten consecutive shots and the error bars 
account for the shot-to-shot fluctuation of the primary electron 
beam (≤ 10% in overall charge, see Fig. 1 of the Supplemental 
Material [20]).

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**TABLE I.** The first four rows illustrate the results from targets 
with the same areal density. The positron yield N_f and N_sim 
refer to the energy window 90 < E_e (MeV) < 120 as obtained 
from the experiment and FLUKA simulation, respectively. N_f 
refers instead to the total yield of positrons with E_e > 1 MeV, 
as extracted from matching numerical simulations. For each 
material, the positron divergence refers to the higher section 
of the positron spectrum (see Fig. 1 of the Supplemental 
Material [20]).

<table>
<thead>
<tr>
<th>Mat.</th>
<th>d (mm)</th>
<th>θ (mrad)</th>
<th>N_f × 10^5</th>
<th>N_sim × 10^5</th>
<th>N_f × 10^5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cu</td>
<td>5.3</td>
<td>2.3 ± 0.2</td>
<td>0.3 ± 0.1</td>
<td>0.3</td>
<td>31</td>
</tr>
<tr>
<td>Sn</td>
<td>6.4</td>
<td>2.7 ± 0.3</td>
<td>0.6 ± 0.1</td>
<td>0.6</td>
<td>63</td>
</tr>
<tr>
<td>Ta</td>
<td>2.8</td>
<td>2.7 ± 0.3</td>
<td>2.1 ± 0.3</td>
<td>2.1</td>
<td>190</td>
</tr>
<tr>
<td>Pb</td>
<td>4.2</td>
<td>3.5 ± 0.4</td>
<td>2.3 ± 0.3</td>
<td>2.3</td>
<td>240</td>
</tr>
<tr>
<td>Ta</td>
<td>1.4</td>
<td>2.3 ± 0.2</td>
<td>0.8 ± 0.2</td>
<td>0.8</td>
<td>78</td>
</tr>
<tr>
<td>Ta</td>
<td>4.2</td>
<td>2.7 ± 0.3</td>
<td>3.8 ± 0.3</td>
<td>3.9</td>
<td>350</td>
</tr>
<tr>
<td>Pb</td>
<td>2.2</td>
<td>3.0 ± 0.3</td>
<td>0.7 ± 0.2</td>
<td>0.7</td>
<td>60</td>
</tr>
<tr>
<td>Pb</td>
<td>2.8</td>
<td>3.3 ± 0.3</td>
<td>1.1 ± 0.3</td>
<td>1.1</td>
<td>122</td>
</tr>
</tbody>
</table>
order-of-magnitude estimate. This is also corroborated by the observed angular divergence $\theta_{\gamma^+}$ of the positron beams inferred from the transverse thickness of the positron trace on the IP detector (see the third column in Table I). In fact, according to QED [29], in our experimental conditions, $\theta_{\gamma^+}$ is expected to be of the order of $1/\gamma_{\gamma^+}$, with $\gamma_{\gamma^+} \approx 300$ being the relativistic factor of the incoming electron beam.

Due to the divergence of the positron beam, its maximum density is located at the close vicinity of the rear side of the solid target. Here, the positron beam has a transverse diameter of the order of $150 \, \mu m$ and, by assuming that the positron beam will retain the temporal duration of the initial electron beam ($d_{\gamma^+} \approx 30 \, frs$, [22]), a longitudinal length of the order of $c \tau_{\gamma^+} \approx 10 \, \mu m$. In the case of maximum yield (4.2 mm Ta, see Table I) the density of positrons with an energy between 90 and 120 MeV is of the order of $2.3 \times 10^{12} \, cm^{-3}$. FLUKA simulations indicate that this energy window contains approximately 1% of the total positron yield. For 4.2 mm of Ta, this means that the total number of positrons with energy $E_{\gamma^+} > 1 \, MeV$ will be of the order of $3.5 \times 10^7$, indicating an overall positron density of about $2 \times 10^{14} \, cm^{-3}$. The overall positron beam intensity can thus be estimated to be of the order of $10^{19} \, erg \ s^{-1} \, cm^{-2}$. FLUKA simulations show that such a positron beam co-propagates with an electron beam with an average density of about $n_{\gamma^+} \approx 2 \times 10^{15} \, cm^{-3}$. The positron contribution on the lepton beam will therefore be of the order of 10% with a null component of positive ions.

We compare now our experimental results with the electron-positron astrophysical jets. Even though a debate is still open as to whether these jets are predominantly constituted by an electron-proton plasma or by electron-positron pairs, an element in favor to the latter is the power-law continuum spectra of the gamma-ray bursts associated with these structures [30]. Despite the different generation mechanism (pair production from gamma-gamma instead of gamma-nucleus collisions), their composition would be similar to the jets reported here, also thanks to their co-propagation with a high-density gamma-ray beam of similar size and duration (FLUKA simulations indicate a gamma-ray brilliance of the order of $10^{19} - 10^{20} \, ph/s/mm^2/mrad^2/0.1\%BW$). For our experimental parameters, the excess of electrons in the beam implies a net current density of the order of $J_{\gamma^+} = -(n_{\gamma^+} - n_e) \gamma_{\gamma^+} \leq -10^{11} \, A/m^2$ (assuming $n_e \approx 2 \times 10^{15} \, cm^{-3}$) inducing an azimuthal magnetic field of the order of $B_{\phi} \approx 30 \, T$. However, FLUKA simulations indicate that, by varying the electron beam characteristics and target thickness, it is possible to significantly modify this percentage. For instance, the interaction of a 1 nC, giga-electron-volt-like electron beam with a thicker tantalum target ($d = 2 \, cm$) is expected to generate a high-density, purely neutral electron-positron jet with a leptonic density of $10^{16} - 10^{17} \, cm^{-3}$. In this case, the toroidal magnetic fields would be virtually zero, allowing one to unveil the microphysics induced by the presence of small-scale magnetic fields generated by filamentation instability [17]. The high leptonic density would in fact allow for the laboratory study of the propagation of astrophysical jets in the interstellar medium.

The proposed mechanism for the generation of ultrarelativistic positron beams, applied to the near-term developments in laser technology, might also be relevant to the construction of all-optical electron-positron colliders. FLUKA simulations of the interaction of a pencil-like monoenergetic electron beam ($E_{\gamma^+} = 100 \, GeV$, overall charge of 1 nC, see Ref. [7]) with a 2 cm thick Ta target indicate the production of a positron beam with an exponentially decreasing energy spectrum (maximum energy of $E_{\gamma^+} = 80 \, GeV$, with approximately $10^9$ positrons with energy between 70 and 80 GeV), a divergence of the order of $\theta_{\gamma^+} \approx 10 \, \mu rad$, and an overall charge comparable to that of the incoming electron beam. Plasma wakefield accelerators can also be subsequently employed to increase the positron energy in a meter-scale device [8]. The low-divergence achievable with our generation mechanism would prove fundamental for efficient injection of the positrons into such devices. The normalized emittance of such a positron beam can be estimated as $\epsilon_n = \gamma_{\gamma^+} \xi_{\gamma^+} \theta_{\gamma^+}$, where $\gamma_{\gamma^+}$, $\xi_{\gamma^+}$, and $\theta_{\gamma^+}$ are the typical values of the Lorentz factor, of the transversal size, and of the divergence of the positron beam itself. The experimentally measured divergence of the positron beam and corresponding simulations with FLUKA (see Fig. 2 of the Supplemental Material [20]) indicate that the product $\gamma_{\gamma^+} \theta_{\gamma^+}$ is of the order of 1 rad independently of the positron energy. Thus, it results that $\epsilon_n \sim \xi_{\gamma^+} \approx 30\pi \, mm \, mrad$, in the conservative case of a 100 micron source transversal size. This is comparable to the positron emittance measured after the injection stage of LEP ($\epsilon_{\gamma^+} \approx 60\pi \, mm \, mrad$ [31]). It must also be noted that the positron beam would be inherently synchronized with the laser, allowing for the possibility of both electron-laser and positron-laser interactions. Direct comparison between these two experimental scenarios might allow for the testing of possible matter or antimatter asymmetries in a highly nonlinear regime.

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[20] See Supplemental Material at http://link.aps.org/supplemental/10.1103/PhysRevLett.110.255002 for ten spectra of the laser-accelerated electron beam, as recorded on the LANEX screen, before the insertion of the solid target (Fig. 1) and for the product between the Lorentz factor and the divergence of the positron beam, as a function of the positron energy, for 4.2 mm of Ta (Fig. 2).