Experimental and numerical study of fastener pull-through failure in GFRP laminates


Published in:
Composite Structures

Document Version:
Peer reviewed version

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Download date:11. Mar. 2019
Experimental and numerical study of fastener pull-through failure in GFRP laminates

G. Catalanotti\textsuperscript{a,*}, P.P. Camanho\textsuperscript{a}, P. Ghys\textsuperscript{b}, A.T. Marques\textsuperscript{a}

\textsuperscript{a}DEMec, Faculdade de Engenharia, Universidade do Porto, Rua Dr. Roberto Frias, 4200-465, Porto, Portugal

\textsuperscript{b}ALSTOM Transport, Rue Albert Dhalenne, 48, 93482, Saint-Ouen, France

Abstract

An experimental and numerical study of the fastener pull-through failure mode in glass-fiber reinforced plastic (GFRP) laminates using both phenolic and vinylester resins is presented. It is shown that the type of resin does not affect the mechanical response of the joint when a pull-through test is performed because similar values of the sub-critical initial and final failure loads are obtained. Moreover, considering that the joint is considering to fail when the sub-critical failure load is reached, a methodology to predict the pull-through failure mode is proposed. It is observed that the main failure mechanism is the delamination of the plies; therefore, the prediction of the sub-critical initial failure load is performed using a three-dimensional finite element model where cohesive elements are used to simulate delamination. The predictions agree remarkably well with the experimental results.

Key words: A. Hybrid structures, B. Bolted joints, C. Pull-through

* Corresponding author

Email address: giuseppe.catalanotti@fe.up.pt (G. Catalanotti).

Preprint submitted to Elsevier 18 June 2011
1 Introduction

GFRP laminates are used in marine, railway and automotive industries in non-structural parts and, more recently, in the main load-carrying structures. The use of composites leads to a reduction of the weight (and consequently of the cost of the transportation), a reduction of manufacturing costs (simplification of the design and reduction of the costs required for the assembly), and to a reduction of the recurring cost (composites require less maintenance than metals).

Due to their high specific stiffness and strength and to the flexibility in their use, GFRP are nowadays used together with metals in the design of hybrid low-cost train structures [1]. Hybrid structures are interesting for the railway industry because they may result in a mass reduction of about 12-24% and in a cost reduction of about 20% [2]. One of the main design requirements of the railway industry is the calculation of the strength of hybrid bolted joints, which correspond to the critical regions of the structures.

While the prediction of the strength of composite bolted joints under in-plane failure mechanism has been thoroughly investigated in the literature [3–7], few attempts have been made to predict out-of-plane failure mechanism, such as fastener pull-through [8–11].

Banbury and Kelly [8] investigated the pull-through failure of carbon laminates manufactured using both plane weave and unidirectional prepregs. An experimental campaign was performed to study the influence of the different parameters on the pull-through failure, namely: the geometry of the fastener head, the thickness of the laminate, and the stacking sequence. It was observed
that the failed specimens exhibit intralaminar damage similar to that shown in composite panels when a low-velocity impact is applied in the transversal direction. In fact, the damaged zones (intralaminar and interlaminar damage) are distributed conically with respect to the axis of the fastener.

Banbury et al. [9] performed numerical analysis to study the pull-through damage mechanism. The Finite Element (FE) analysis indicated that:

• shear stresses in the vicinity of the bolt head are responsible for the intralaminar matrix cracking in through-the-thickness direction;
• tensile in-plane stresses are responsible for the flexural deformation of the material in particular in low-modulus laminate;
• matrix cracking was observed to be the primary failure mechanism while delamination (caused by the high interlaminar shear and peel stress) was the secondary mechanism.

Moreover, a numerical procedure to simulate the progressive damage in the material was proposed. A progressive damage model together with the maximum principal strain criterion were used and a good agreement between the experiments and the numerical predictions, both in terms of failure load, damaged zones and damage mechanisms, was obtained.

Kelly and Hallström [10] performed an experimental and numerical investigation of a laminate subjected to transversal loads. Different geometries, materials and lay-ups were investigated. The damage onset was observed to occur at a load of approximately 20-30% of the failure load, and the different failure mechanism were identified. As mentioned in previous investigations [8], the damaged zones show both interlaminar and intralaminar matrix cracking. A three-dimensional finite element method was proposed to predict the first-ply
failure.

Elder et al. [11] proposed a simplified three-dimensional finite elements model to model pull-through failure of composite laminates. It was concluded that simplified models allow to obtain a good prediction of the pull-through failure for quasi-isotropic laminates even if additional efforts are required to properly define the cohesive parameters used in the numerical model.

Fastener pull-through is particularly important for train structures where several hybrid connections are present:

- the connection between the main frame and the floor;
- the connection between the carbody shell and the top floor (in the case of a double deck carbody shell);
- the connection between the main frame and the carbody shell;
- the connection between the carbody shell and the roof.

Figure 1 represents the connection between the main frame and the side of the carbody shell. This connection uses two different materials because the internal panel cannot be toxic, while the external panel must have a good fire resistance [12]. For this reason, the internal panel is manufactured using phenolic resin, while the external panel is manufactured using vinylester resin.

The aim of this paper is to experimentally study the fastener pull-through failure mode in GFRP laminates and to propose a numerical technique to predict the response of a bolted joints under out-of-planes loads. Taking into account that in industrial applications several resins are used to satisfy the current legislation (in particular about the fire behavior [12]) the study presented here
concerns two different resins: phenolic and vinylester.

2 Experiments

2.1 Materials

The composites investigated in this study are:

- Fiber Glass-vinylester composite (GF-V);
- Fiber Glass-phenolic composite (GF-P).

The laminates were manufactured using the technique of resin infusion and they have the quasi-isotropic lay-up reported in Table 1. The mechanical properties of these laminates are reported in Table 2 where: $E_i$ is the Young’s modulus in $i$ direction, $\nu_{ij}$ is the Poisson’s ration in $i$-$j$ directions, $G_{ij}$ is the shear modulus in $i$-$j$ directions, $X_T$ is the longitudinal tensile strength, $X_C$ is the longitudinal compressive strength, $Y_T$ is the transverse tensile strength, $Y_C$ is the transverse compressive strength, $S_T$ is the transverse shear strength, $S_L$ is the longitudinal shear strength and $\rho$ is the density.

The material was tested after a heat aging treatment according to the AFNOR norm [13].

[Table 1 about here.]

[Table 2 about here.]
2.2 Pull-through tests

The pull-through test is performed following the norm ASTM D7332 - *Standard Test Method for Measuring the Fastener Pull-Through Resistance of a Fiber-Reinforced Polymer Matrix Composite* [14].

This test method proposes two procedures, A and B. Procedure A is used to enhance the fastener design while procedure B is used to study other design variables. Both procedures use flat test specimens with a circular hole in the center where the fastener is installed. In procedure A two specimens are joined using a fastener and one plate is rotated of 45° with respect to the other. Each test specimen contains four additional holes at the corners where the fasteners are installed to connect the specimens to the test fixtures. In procedure B, the load is applied to the test specimen using a yoke as shown in Figure 2. Since procedure A is more complex and has inherent problems associated with the flexural stiffness of the specimen to test, procedure B was used.

[Fig. 2 about here.]

The test was conducted using an INSTRON-4208 test machine. Figure 3 shows the experimental set-up used. The test machine was equipped with a 100kN load cell. The speed of the machine (displacement controlled test) was 2mm/min. The temperature of the room was 23°C and the relative humidity was 50% for all the duration of the tests.

[Fig. 3 about here.]

After each test the damaged specimen was examined and the type of failure was identified.
The test results depend on Clearance Hole parameter ($C_b$). This is the diameter of the plate that it is used in procedure $B$ of the test. In the tests performed $C_b$ was taken as 30mm. The dimensions of all test specimens, the ratio of the Clearance Hole Diameter $C_b$ to Fastener Hole Diameter $d$, and the ratio of the Fastener Hole Diameter to the thickness of the specimen ($h$) are reported in the following points. The test specimens are square plates with a length of 105mm. Three specimens were tested for each configuration and for each material: one with a 6mm diameter hole and the other with a 10mm diameter hole. In the following, each specimen was indicated with the denomination PT-M-D where M indicates the material (P for phenolic and V for vinylester) and D indicates the diameter in millimeters (6 or 10).

2.3 Derived properties

The load-displacement for a pull-through test is used to identify three important characteristics of the joints that are:

- the Initial Sub-Critical Failure Load: the load at the first sub-critical failure of the specimen;
- the Initial Sub-Critical Failure Displacement: the displacement at the first sub-critical failure of the specimen;
- the Failure Load: the maximum load attained in the test.

The specimen shows a first failure mode (generally delamination) at a relatively low load. After delamination, the specimen is able to support increasing loads. This point is identified in the curve by a load-drop, which is followed by a decrease of the stiffness of the test coupon.
2.4  **GF-phenolic specimens**

Table 3 reports the dimensions of the specimens and the geometric parameters of the equipment used. Figure 4 shows the load vs. displacement curves for the phenolic specimens. The derived properties for the specimens tested are reported in Tables 4-5.

It should be noted that some specimens (see Tables 4-5) exhibited bolt failure. The bolts used for these tests were general purpose bolts (D933 8.8).

[Table 3 about here.]

[Table 4 about here.]

[Table 5 about here.]

[Fig. 4 about here.]

2.5  **GF-vinylester specimens**

Table 6 reports the dimensions of the specimens and the geometric parameters of the equipment used. Figure 5 shows the load vs. displacement curves for vinylester specimens. The derived properties for the specimens tested are reported in Tables 7-8.

[Table 6 about here.]

[Table 7 about here.]

[Table 8 about here.]
2.6 Damaged zones

Figure 6 shows the photos of a specimen tested up to failure. Both sides of
the specimen are visible. The bottom side, Figure 6(b), shows delamination
near the hole. As explained before, delamination occurs at the begin of the test
when the load is relatively low (initial sub-critical failure). If the load increases,
the intralaminar fracture in the material starts and, at the end, the specimen
is totally penetrated by the washer. The delamination occurs abruptly when
the sub-critical initial load is reached. It is not possible to exactly identify the
location of the first delamination, even if it seems plausible that they occur
at the interface with the thick 0° plies due to the high interlaminar stresses
promoted by the thick plies.

2.7 Comparison of the PT test results

Figure 7 shows the failure loads of the two materials tested. As expected,
increasing the hole diameter increases both the initial sub-critical failure load
and the final failure load of the specimens. The results indicate that the two
materials tested exhibit only slight differences in the values of the two failure
loads considered.

It should be also noted that increasing the diameter also increases the ra-
tio between the initial sub-critical failure load to the ultimate failure load.
This means that larger holes exhibit an initial sub-critical failure load that is relatively lower when compared to the ultimate failure load.

The load corresponding to the first load-drop will be taken as the design load. This load corresponds to the onset of delamination that is likely to propagate under fatigue loading.

3 Numerical model

Based on the previous remarks, a numerical model, based on the Finite Element Method, is developed to predict the delamination onset load. This load is taken as the design load.

3.1 Numerical Implementation

The Finite Element model was created using Abaqus 6.8 [15]. The mesh is shown in Figure 8. The specimen and the bolt (screw and washers) are represented as deformable bodies, while the steel plate used for the pull-through test is modeled as an analytical rigid surface. Frictionless contact is considered between the different parts. Figure 9 shows the FE model as viewed from the bottom.
The test specimen, shown in Figure 10, was modeled using 8-nodes linear brick reduced integration elements (CRD8R) with a typical element size of 1mm.

Cohesive finite elements, implemented as an Abaqus Users’ subroutines (UMAT) [15], are used to predict delamination. These elements are used in all interfaces between plies with different fiber orientation angles.

The detailed definition of the cohesive model is presented in [16]. For the sake of completeness, the main aspects of the constitutive model are outlined in the following paragraphs.

The relation between the tractions transferred along a bridged crack, \( \tau \), and the corresponding displacement jumps, \( \Delta \), reads:

\[
\tau_i = (1 - d)k\Delta_i - [\delta_{i3}d_k(-\Delta_3)]
\]

(1)

where \( d \) is a scalar damage variable and \( k \) is the penalty stiffness. The displacement jump \( \Delta_3 \) is related to mode I, whereas the displacement jumps \( \Delta_1 \) and \( \Delta_2 \) are related to shear modes of loading.

The operator \( \langle x \rangle \) is defined as \( \langle x \rangle = \frac{1}{2}(x + |x|) \), and \( \delta_{ij} \) is the Kroenecker delta.

Introducing \( \lambda \) as the norm of the displacement jump:

\[
\lambda = \sqrt{(\Delta_3)^2 + \Delta_{sh}^2}, \quad \Delta_{sh} = \sqrt{(\Delta_1)^2 + (\Delta_2)^2}
\]

(2)

The damage activation function for general mixed-mode loading is defined as:

\[
\mathcal{F}(\Delta, d) = \mathcal{L}(\Delta) - d \leq 0
\]

(3)
where:

\[
\mathcal{L}(\Delta) = \min \left\{ \frac{\Delta^f(\lambda - \Delta^o)}{\lambda(\Delta^f - \Delta^o)} - 1 \right\}
\] (4)

and:

\[
d_t = \max \left\{ 0, \max_s [\mathcal{L}(\Delta_t)] \right\} , 0 \leq s \leq t, \forall t \geq 0
\] (5)

The displacement jumps corresponding to delamination onset (\(\Delta^o\)) and to delamination propagation (\(\Delta^f\)) under mixed-mode conditions are obtained using the Benzeggagh and Kenane criterion [17] for delamination propagation under mixed-mode loading, yielding [16]:

\[
\Delta^o = \left\{ \left( \Delta^o_3 \right)^2 + \left[ \left( \Delta^o_{sh} \right)^2 - \left( \Delta^o_3 \right)^2 \right] B^\eta \right\}^{1/2}
\] (6)

\[
\Delta^f = \frac{1}{\Delta^o} \left[ \Delta^o_3 \Delta^f_3 + \left( \Delta^o_{sh} \Delta^f_{sh} - \Delta^o_3 \Delta^f_3 \right) B^\eta \right]
\] (7)

where \(\eta\) is the mixed-mode interaction parameter used in the Benzeggagh and Kenane criterion [17] and \(B\) is a local mixed-mode ratio defined as:

\[
B = \frac{G_{sh}}{G_{sh} + G_I} = \frac{\Delta^2_{sh}}{\chi^2}
\] (8)

\(\Delta^o_3\) and \(\Delta^o_{sh}\) are respectively the displacement jumps corresponding to delamination onset in mode I and in shear mode:
\[ \Delta_{o3}^\theta = \frac{\tau_{o3}^\theta}{k}; \Delta_{osh}^\theta = \frac{\tau_{osh}^\theta}{k} \quad (9) \]

where \( \tau_{o3}^\theta \) and \( \tau_{osh}^\theta \) are the pure mode interlaminar strengths.

\( \Delta_f^I \) and \( \Delta_f^{sh} \) are respectively the displacement jumps corresponding to delamination propagation under mode I and in shear mode:

\[ \Delta_f^I = \frac{2G_{IIc}}{\tau_{o3}^\theta}; \Delta_f^{sh} = \frac{2G_{IIc}}{\tau_{osh}^\theta} \quad (10) \]

To reduce the complexity of the model (and the time needed for the analysis) the cohesive elements were used only in the vicinity of the bolt as shown in Figure 10.

[Fig. 10 about here.]

The relevant parameters for the definition of the cohesive elements are obtained using experimental data previously measured for a similar material [18]. The material properties used are shown in Table 9.

[Table 9 about here.]

Using these values the exponent for the B-K criterion [17] is calculated using the least-squares method as \( \eta = 1.98 \). The penalty stiffness, \( k \), is taken as \( 10^6 \text{N/mm}^3 \). The interface strengths are calculated using the engineering solution proposed by Turon et al. [19] resulting in \( \tau_{o3}^\theta = 28.8 \text{MPa} \) and \( \tau_{osh}^\theta = 48.8 \text{MPa} \).
3.2 Numerical results

Taking into account that no major differences were found between the delamination onset loads for the two materials tested, the numerical simulations are conducted only for the GF-P specimens.

Figure 11 shows the load-displacement relation predicted by the numerical model. The predictions for the initial sub-critical failure load and the experimental values are reported in Table 10. A reasonable agreement between the numerical predictions and the experimental data is obtained. The maximum error, -10%, is obtained for the PT-P-10 specimen. It is also observed that the load-drop identified in the experiments is also captured by the numerical model.

[Fig. 11 about here.]

[Table 10 about here.]

4 Concluding remarks

An experimental and a numerical study of the pull-through damage in GFRP laminates is presented in this paper. Two different material system (GF-phenolic and GF-vinylester) and two geometries (diameter of the hole 6mm and 10mm) are investigated. It is concluded that:

• increasing the diameter of the bolt increases both the sub-critical initial failure load and the failure load;
• larger holes exhibit a sub-critical initial failure load that is relatively lower
when compared to the ultimate failure load;

- the interlaminar damage is the predominant phenomenon for damage onset;
- using three-dimensional finite element models using linear elastic elements together with cohesive elements it is possible to predict the value of the sub-critical initial failure load with a reasonable accuracy.

Acknowledgements

The first author acknowledges the financial support of the European Commission under Contract No. MRTN-CT-2005-019198.

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(a) intralaminar fracture
(b) delamination at sub-critical failure
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Table 1
Orientation pattern for GF-vinylester / phenolic composite.

<table>
<thead>
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<th>ply</th>
<th>type of product</th>
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</tr>
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<td>±45° − 610 g/m²</td>
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<td>7</td>
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<td>GCI S90000 VM10 SAF 1</td>
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31
Table 2
Mechanical properties of GF-V and GF-P UD laminate.

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<th>GF-phenolic</th>
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<td>$E_2 = E_3$ (MPa)</td>
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Table 3
GF-P specimens’ dimensions.

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Table 4
Pull-through test, results for PT-P-6 specimens.

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<th>Failure load (N)</th>
<th>In. Sub-crit. failure displ. (mm)</th>
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(*) bolt failure
Table 5
Pull-through test, results for PT-P-10 specimens.

<table>
<thead>
<tr>
<th>Specimen</th>
<th>In. Sub-crit. failure load (N)</th>
<th>Failure load (N)</th>
<th>In. Sub-crit. failure displ. (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>PT-P-10-1</td>
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<td>7.00</td>
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(*) bolt failure
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<th>Failure load (N)</th>
<th>In. Sub-crit. failure displ. (mm)</th>
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<td>PT-V-10-3</td>
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<td>Test</td>
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<td>( G_{IIc}^{\phi} )</td>
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<td>MMB</td>
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<td>MMB</td>
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<td>0.75</td>
<td>MMB</td>
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<td>ENF</td>
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Table 10
Initial sub-critical failure load: experiments and predictions.

<table>
<thead>
<tr>
<th>Specimens</th>
<th>Experimental value (N)</th>
<th>Numerical prediction (N)</th>
<th>Error (%)</th>
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<tr>
<td>PT-P-6</td>
<td>12158</td>
<td>11922</td>
<td>-2%</td>
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<td>PT-P-10</td>
<td>18548</td>
<td>16700</td>
<td>-10%</td>
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